

# Computability Assignment

## Year 2013/14 - Number 1

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### 1 Question

Define a binary property  $p(x, y)$  over natural numbers that satisfies both the requisites:

1.  $\forall x \in \mathbb{N}. \exists y \in \mathbb{N}. p(x, y)$  and
2. *it is false that*  $\forall y \in \mathbb{N}. \exists x \in \mathbb{N}. p(x, y)$

Provide a definition for  $p$ , and a proof for the above claims.

#### 1.1 Answer

$p(x, y) : x^2 - y = 0$

Let choose an arbitrary  $x \in \mathbb{N}$ , we can always find  $y = x^2 \in \mathbb{N}$  that satisfies  $p(x, y)$ . So the requisites (1) holds

We choose  $y = 3 \in \mathbb{N}$ , then according to the above  $p(x, y)$ ,  $x^2 - 3 = 0$ . We cannot find  $x \in \mathbb{N}$  that satisfies that equation. So (2) holds.