

# Computability Assignment

## Year 2013/14 - Number 1

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### 1 Question

Define a binary property  $p(x, y)$  over natural numbers that satisfies both the requisites:

1.  $\forall x \in \mathbb{N}. \exists y \in \mathbb{N}. p(x, y)$  and
2. *it is false that*  $\forall y \in \mathbb{N}. \exists x \in \mathbb{N}. p(x, y)$

Provide a definition for  $p$ , and a proof for the above claims.

#### 1.1 Answer

We take a binary property  $p$  expressed as  $x < y$ .

In this way we are going to prove that exist a binary property that satisfies both the requisites.

So we have that:

Case 1)

Taking  $x=z$  and  $y=z+1$  (so the successor) we have that the property is always satisfied.

Case 2)

The counterexample to prove the second case is defining  $y$  equal to 0. The consequence is that will never exist an  $x$  s.t.  $x < y$ .