Computability Assignment Year 2013/14 - Number 1

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1 Question

Define a binary property p(x, y) over natural numbers that satisfies both the requisites:

- 1. $\forall x \in \mathbb{N} . \exists y \in \mathbb{N} . p(x, y)$ and
- 2. it is false that $\forall y \in \mathbb{N} . \exists x \in \mathbb{N} . p(x, y)$

Provide a definition for p, and a proof for the above claims.

1.1 Answer

1.1.1 Property

$$p(x, y) := x < y$$

1.1.2 Proof

- 1. The set \mathbb{N} is an infinite set and $\forall x.x \in \mathbb{N} \Rightarrow \exists y.y = x + 1, y \in \mathbb{N}$
- 2. $y \in \mathbb{N}, y = 0 \Rightarrow \neg \exists x. x \in \mathbb{N}, x < y$