

Computability Assignment

Year 2012/13 - Number 1

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1 Question

Define a binary property $p(x, y)$ over natural numbers such that we have both

1. $\forall x \in \mathbb{N}. \exists y \in \mathbb{N}. p(x, y)$
2. $\neg \exists y \in \mathbb{N}. \forall x \in \mathbb{N}. p(x, y)$

Provide a definition for p , and a proof for the above claims.

1.1 Answer

$$p(x, y) = \begin{cases} true & y = 2x \\ false & o.w. \end{cases}$$

1. Obvious, all even numbers are natural numbers. **OK - RZ**

2. Equivalent to $\forall y \in \mathbb{N}. \exists x \in \mathbb{N}. \neg p(x, y)$. **OK - RZ**

Apparently, for an odd number y we don't have a natural number x s.t. $y = 2x$.

I don't understand: the above proves $\forall y \in Odd. \neg \exists x. y = 2x$, which is not the same thing as $\forall y \in \mathbb{N}. \exists x \in \mathbb{N}. \neg p(x, y)$.