

Computability Assignment

Year 2012/13 - Number 3

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More information about assignments at <http://disi.unitn.it/~zunino/teaching/computability/assignments>

Please do not submit a file containing only the answers; edit this file, instead, filling the answer sections.

1 Question

Let A, B be sets, and let id_A, id_B denote the identity functions over A and B respectively. Assume $f \in (A \rightarrow B)$ and $g \in (B \rightarrow A)$ be functions satisfying $g \circ f = \text{id}_A$ and $f \circ g = \text{id}_B$. Prove that f is a bijection (i.e., injective and surjective).

1.1 Answer

Write your answer here.

2 Question

Let A, B be sets, and let $f \in (A \leftrightarrow B)$ be a bijection. Define a bijection $g \in (\mathcal{P}(A) \leftrightarrow \mathcal{P}(B))$ and prove it is such.

2.1 Answer

Write your answer here.

3 Question

Let A, B be two sets, and let $b \notin B$. Define a bijection f between the set of partial functions $(A \rightsquigarrow B)$ and the set of total functions $(A \rightarrow B \cup \{b\})$. Prove that is is such.

3.1 Answer

Write your answer here.

Note.

The exercises below are harder. Feel free to skip them if you find them too hard.

4 Question

Define a bijection $f \in [(\mathcal{P}(A) \times \mathcal{P}(B)) \leftrightarrow \mathcal{P}(A \uplus B)]$. Prove that is is such.

4.1 Answer

Write your answer here.

5 Question

Define a bijection $f \in [((A \uplus B) \rightarrow C) \leftrightarrow ((A \rightarrow C) \times (B \rightarrow C))]$. Prove that is is such.

5.1 Answer

Write your answer here.

6 Question

Define a bijection $f \in [((A \rightarrow (B \times C)) \leftrightarrow ((A \rightarrow B) \times (A \rightarrow C)))]$. Prove that is is such.

6.1 Answer

Write your answer here.