# SPIN: Exercises\*

## Patrick Trentin patrick.trentin@unitn.it http://disi.unitn.it/~trentin

# Formal Methods Lab Class, Mar 10, 2015



Università degli Studi di Trento

\*These slides are derived from those by Stefano Tonetta, Alberto Griggio, Silvia Tomasi, Thi Thieu Hoa Le, Alessandra Giordani for FM lab 2005/14



### • Reliable FIFO Communication

• Leader Election

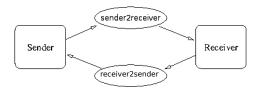
.∋...>

A B A A B A A B A A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A

Goal: design a reliable FIFO communication over a non-reliable channel.

## Alternating Bit Protocol:

- Sender and Receiver communicate over a couple of channels sender2receiver and receiver2sender
- the channels *sender2receiver* and *receiver2sender* are unreliable: messages might be lost or duplicated



```
mtype = { MESSAGE, ACK };
chan sender2receiver = [2] of { mtype, bit, int};
chan receiver2sender = [2] of { mtype, bit, int};
active proctype Sender () {
....
}
active proctype Receiver () {
....
}
```

### Sender specs:

- the Sender tags the messages with an alternating bit (e.g. it sends (msg1, 0), (msg2, 1), (msg3, 0), ... ).
- the *Sender* repeatedly sends a message with a tag value until it receives an acknowledgment from the *Receiver*.
- Suppose Sender has sent (msg, out\_bit) and receives in\_bit as acknowledgment:
  - if in\_bit is equal to out\_bit, then it means that *Receiver* has received the right message, so it sends a new message with a different value for out\_bit.
  - otherwise it sends (msg, out\_bit) again.
- the Sender attaches to each message a sequence\_number, which is increased each time the tag value is changed.

```
active proctype Sender () {
    bit in_bit, out_bit;
    int seq_no;
```

#### do

od

}

```
:: sender2receiver!MESSAGE(out_bit, seq_no) ->
    receiver2sender?ACK(in_bit, 0);
    if
        :: in_bit == out_bit ->
            out_bit = 1 - out_bit;
            seq_no++;
        :: else ->
            skip
fi
```

### **Receiver specs:**

- suppose *Receiver* receives (msg, tag):
  - if tag is different from the last received bit, then it means that it is a new message;
  - otherwise, the message is old.
- When the *Receiver* receives a message, it sends the tag back to the *Sender* to communicate the correct receival of the message.

```
active proctype Receiver () {
    bit in_bit, old_bit;
    int seq_no;
   do
        :: sender2receiver?MESSAGE(in_bit, seq_no) ->
            if
                :: in bit != old bit ->
                    printf("received: %d\n", seq_no);
                    old_bit = in_bit;
                :: else ->
                    skip
            fi
            receiver2sender!ACK(in_bit, 0);
    od
```

}

```
inline unreliable_send(channel, type, tag, seqno) {
    bool loss = false;
    bool duplicate = true;
    if
        :: channel!type(tag, seqno);
            if
                :: channel!type(tag, seqno);
                :: duplicate = false;
            fi
        :: loss = true;
    fi
}
// + modify Sender and Receiver to use this function
```

Q: what happens with the unreliable channel? (why?)

```
inline unreliable_send(channel, type, tag, seqno) {
    bool loss = false;
    bool duplicate = false;
   if
        :: channel!type(tag, seqno);
            if
                :: channel!type(tag, seqno);
                :: duplicate=true;
            fi
        :: loss=true;
    fi
}
// + modify Sender and Receiver to use this function
```

Q: what happens with the unreliable channel? (why?) deadlock

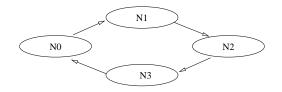


• Reliable FIFO Communication

Leader Election

э.

- *N* processes are the nodes of a unidirectional ring network: each process can send messages to its clockwise neighbor and receive messages from its counterclockwise neighbor.
- The requirement is that, eventually, **only one** process will output that it is the **leader**.
- We assume that every process has a **unique id**.
- The leader must have the **highest id**.



The algorithm:

- Initially, every process passes its identifier to its successor.
- When a process receives an identifier from its predecessor, then:
  - if it is greater than its own, it keeps passing on the identifier.
  - if it is smaller than its own, it discards the identifier.
  - if it is equal to its own identifier, it declares itself leader:
    - the leader communicates to its successor that now it is the leader.
    - after a process relayed the message with the leader id, it exits.

## **Complexity:** at worst, $n^2$ messages.

The algorithm:

- If a process is "active", it compares its identifier with the two couterclockwise predecessors:
  - if the highest of the three is the counterclock neighbor, the process proposes the neighbor as leader,
  - otherwise, it becomes a "relay".
- If the process is in "relay" mode, it keeps passing whatever incoming message.

## **Complexity:** at worst, $n \cdot log(n)$ messages.

- configure Sender and Receiver to use unreliable\_send().
- fix the *Alternating Bit Protocol* so that there is no more **deadlock** and the input specification is still respected.

# Exercise 2: Leader Election

```
mtype = { candidate, leader };
chan c[N] = [BUFSIZE] of { mtype, byte };
                                                       Implement a leader
                                                          election algorithm
proctype node(chan prev, next; byte id) { ... }
                                                          of your choice.
init {
                                                       • Verify that there is
    byte proc, i;
                                                          at most one leader.
    atomic {
        // TODO: set i random in [0,N]
         . . .
        do
             :: proc < N \rightarrow
                 run node(c[proc], c[(proc+1)%N], (N+i-proc)%N);
                 proc++
             :: else ->
                 break
                                                     \rightarrow strong solution hint!
        od
    }
}
                                                             - 4 3 6 4 3 6
```

- will be uploaded on course website later this week
- send me an email if you need help or you just want to propose your own solution for a review

• learning programming languages requires practice: try to come up with your own solutions first!