

Formal Method Mod. 2 (Model Checking) Laboratory 7

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- 1. Introduction
- 2. nuXmv interactive shell
- 3. nuXmv Modeling
- Modules
- 5. Homework



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History of nuXmv

SMV

Symbolic Model Verifier developed by McMillan in 1993.

NuSMV

Open-source symbolic model checker for SMV models. It has been developed by FBK, Carnegie Mellon University, University of Genoa and University of Trento.

nuXmv

Extends NuSMV for infinite state and timed (since v2) systems. Binary available for non-commercial or academic purposes only. Developed and maintained by the Embedded Systems unit of FBK.



Application of nuXvm

- nuXmv allows for the verification of:
 - finite-state systems through SAT and BDD based algorithms;
 - infinite-state systems (e.g. systems with real and integer variables) through SMT-based techniques running on top of MathSAT5;
 - timed systems (e.g. allows clock type) via reduction to infinite state model checking.
- nuXmv supports synchronous systems;
- asynchronous systems are no longer supported!

Outline

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- nuXmv Modeling
- 4. Modules
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Interactive shell [1/3]

- ▶ nuXmv -int (or NuSMV -int) activates an interactive shell
- help shows the list of all commands (if a command name is given as argument, detailed information for that command will be provided). note: option -h prints the command line help for each
 - command.
- reset resets the whole system (in order to read in another model and to perform verification on it).
- read_model [-i filename] sets the input model and reads it.
- go, go_bmc, go_msat initialize nuXmv for verification or simulation with a specific backend engine.



Interactive shell [2/3]

- pick_state [-v] [-a] [-r | -i] picks a state from the set
 of initial states.
 - -v prints the chosen state.
 - -r picks a state from the set of the initial states randomly.
 - -i picks a state from the set of the initial states interactively.
 - -a displays all state variables (requires -i).
- simulate [-p | -v] [-a] [-r | -i] -k N generates a sequence of at most N transitions starting from the current state.
 - -p prints the changing variables in the generated trace;
 - v prints changed and unchanged variables in the generated trace;
 - -a prints all state variables (requires -i);
 - -r at every step picks the next state randomly.
 - -i at every step picks the next state interactively.
- print_current_state [-h] [-v] prints out the current state.
 - ► -v prints all the variables.



Interacting Shell [2/3] - Output Example

```
nuXmv > reset
nuXmv > read_model -i example01.smv ; go
nuXmv > pick_state -v; simulate -v
Trace Description: Simulation Trace
Trace Type: Simulation
  -> State: 1.1 <-
    b0 = FALSE
****** Simulation Starting From State 1.1
Trace Description: Simulation Trace
Trace Type: Simulation
  -> State: 1.1 <-
    b0 = FALSE
  -> State: 1.2 <-
    b0 = TRUE
  -> State: 1.3 <-
    b0 = FALSE
  -> State: 1.4 <-
    b0 = TRUE
  -> State: 1.5 <-
    b0 = FALSE
  -> State: 1.6 <-
    b0 = TRUE
```



Interacting Shell [3/3]

- show_vars [-s] [-f] [-i] [-t] [-v] prints the variables content and type
 - -s print state variables;
 - -f print frozen variables;
 - -i print input variables;
 - -t prints the number of variables;
 - -v prints verbosely;
- quit stops the program.



- 1. Introduction
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- 3. nuXmv Modeling

Basic Types

Expressions

Transition Relation

Miscellany

Constraint Style Modeling

- 4. Modules
- 5. Homework



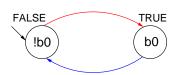
First SMV model

- an SMV model is composed by a number of modules;
- each **module** can contain:
 - state variable declarations;
 - formulae defining the valid initial states;
 - formulae defining the transition relation;

Example:

```
MODULE main
VAR
b0 : boolean;

ASSIGN
init(b0) := FALSE;
next(b0) := !b0;
```



Basic Types [1/3]

```
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```

```
boolean: TRUE, FALSE, ...
    x : boolean;
enumerative:
    s : {ready, busy, waiting, stopped};
bounded integers* (intervals):
    n : 1..8;
*: integer numbers must be within C/C++ INT_MIN and INT_MAX bounds
```

Basic Types [2/3]

```
integers*: -1, 0, 1, ...
```

n : integer;

rationals: 1.66, f'2/3, 2e3, 10e-1, ...

r : real;

words: used to model arrays of bits supporting bitwise logical and arithmetic operations.

- unsigned word[3];
- signed word[7];
- * : integer numbers must be within C/C++ INT_MIN and INT_MAX bounds

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Basic Types [3/3]

arrays:

declared with a couple of lower/upper bounds for the index and a type

VAR

```
-- array of 11 elements
x : array 0..10 of boolean;
-- array of 3 elements
y : array -1..1 of {red, green, orange};
-- array of array
z : array 1..10 of array 1..5 of boolean;
ASSIGN
init(x[5]) := bool(1);
-- any value in the set
init(y[0]) := {red, green};
init(z[3][2]) := TRUE;
```

Array indexes must be constants;



Adding a state variable

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```
MODULE main

VAR

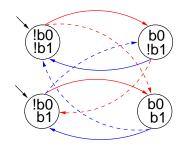
b0 : boolean;

b1 : boolean;

ASSIGN

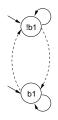
init(b0) := FALSE;

next(b0) := !b0;
```



Remarks:

- the FSM is the result of the synchronous composition of the "subsystems" for b0 and b1
- the new state space is the cartesian product of the ranges of the variables.



Initial States [1/2]

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Example:

```
init(x) := FALSE;    -- x must be FALSE
init(y) := {1, 2, 3}; -- y can be either 1, 2 or 3
init(<variable>) := <simple_expression>;
```

```
Department the initial value of constant and any
```

- constrains the initial value of <variable> to satisfy the <simple_expression>;
- the initial value of an unconstrained variable can be any of those allowed by its domain;

set of initial states

is given by the set of states whose variables satisfy all the init() constraints in a module.



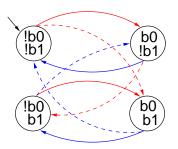
Initial States [2/2]

Example:

```
MODULE main
VAR
  b0 : boolean;
  b1 : boolean;

ASSIGN
  init(b0) := FALSE;
  next(b0) := !b0;

init(b1) := FALSE;
```



Expressions [1/3]

arithmetic operators:

```
+ - * / mod - (unary)
```

comparison operators:

logic operators:

bitwise operators:

set operators: {v1,v2,...,vn}

in: tests a value for membership in a set (set inclusion)

union: takes the union of 2 sets (set union)

count operator: counts number of true boolean expressions count(b1, b2, ..., bn)



Expressions [2/3]

> case expression:

if-then-else expression:

```
cond_expr ? basic_expr1 : basic_expr2
```

- conversion operators: toint, bool, floor, and
 - swconst, uwconst: convert an integer to a signed and an unsigned word respectively.
 - word1 converts boolean to a single word bit.
 - unsigned and signed convert signed word to unsigned word and vice-versa.

Expressions [3/3]

expressions in SMV do not necessarily evaluate to one value. In general, they can represent a set of possible values.

```
init(var) := \{a,b,c\} union \{x,y,z\};
```

- ► The meaning of := in assignments is that the lhs can non-deterministically be assigned to any value in the set of values represented by the rhs.
- ► A constant c is considered as a syntactic abbreviation for {c} (the singleton containing c).



Transition Relation [1/2]

Transition Relation

specifies a constraint on the values that a variable can assume in the *next state*, given the value of variables in the *current state*.

```
next(<variable>) := <next_expression>;
```

<next_expression> can depend both on "current" and "next" variables:

```
next(a) := { a, a+1 } ;
next(b) := b + (next(a) - a) ;
```

- <next_expression> must evaluate to values in the domain of <variable>;
- the next value of an unconstrained variable evolves non-deterministically;

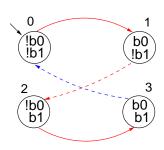


Transition Relation [2/2]

Example:

modulo-4 counter

```
MODULE main
 VAR
   b0 : boolean;
   b1 : boolean;
 ASSIGN
   init(b0) := FALSE;
   next(b0) := !b0;
   init(b1) := FALSE;
   next(b1) := case
       b0
            : !b1;
       TRUE : b1;
     esac;
```





Output Variable [1/2]

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output variable

A variable whose value deterministically depends on the value of other "current" state variables and for which no init() or next() are defined.

```
<variable> := <simple_expression>;
```

- <simple_expression> must evaluate to values in the domain of the <variable>.
- used to model outputs of a system;



Output Variable [2/2]

next(b1) := ((!b0 & b1) | (b0 & !b1));

out := toint(b0) + 2*toint(b1);

Example:

```
MODULE main
VAR
b0 : boolean;
b1 : boolean;
```

```
ASSIGN
  init(b0) := FALSE;
  next(b0) := !b0;
  init(b1) := FALSE;
```

out : 0..3;

```
2 3
```



Assignment Rules (:=)

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▶ single assignment rule – each variable may be assigned only

```
once; | llegal examples:

init(var) := ready; var := ready; next(var) := ready;

init(var) := busy; var := busy; var := busy;

next(var) := ready; init(var) := ready;

next(var) := busy; var := busy;
```



Assignment Rules (:=)

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▶ single assignment rule – each variable may be assigned only

```
once; | llegal examples:

init(var) := ready; var := ready; next(var) := ready;

init(var) := busy; var := busy; var := busy;

next(var) := ready; init(var) := ready;

next(var) := busy; var := busy;
```

circular dependency rule – a set of equations must not have "cycles" in its dependency graph, unless broken by delays; Illegal examples:

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DEFINE declarations

```
DEFINE <id> := <simple_expression>;
```

- ▶ similar to C/C++ macro definitions: each occurrence of the defined symbol is replaced with the body of the definition
- provide an alternative way of defining output variables;

Example:

```
MODULE main
 VAR.
   b0 : boolean;
   b1 : boolean;
 ASSTGN
   init(b0) := FALSE;
   next(b0) := !b0;
   init(b1) := FALSE;
   next(b1) := ((!b0 & b1) | (b0 & !b1));
 DEFINE
   out := toint(b0) + 2*toint(b1);
```

3. nuXmv Modeling



Example: modulo 4 counter with reset

The counter can be reset by an external "uncontrollable" signal.

```
b0 : boolean; b1 : boolean; reset : boolean;
ASSIGN
 init(b0) := FALSE;
 init(b1) := FALSE:
 next(b0) := case
                reset = TRUE : FALSE:
                reset = FALSE : !b0;
              esac:
 next(b1) := case
                reset : FALSE;
                TRUE : ((!b0 & b1) | (b0 & !b1)):
              esac;
DEFINE
 out := toint(b0) + 2*toint(b1);
```

Exercise:

simulate the system with nuXmv and draw the FSM.

```
MODULE main
VAR
  request : boolean;
  state : { ready, busy };

ASSIGN
  init(state) := ready;
  next(state) :=
    case
      state = ready & request : busy;
    TRUE : { ready, busy };
  esac;
```



Exercise 1

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Exercise:

simulate the system with nuXmv and draw the FSM.

```
MODULE main

VAR

request : boolean;
state : { ready, busy };

ASSIGN

init(state) := ready;
next(state) :=
case
state = ready & request : busy;
TRUE
: { ready, busy };
```

Constraint Style Modeling [1/4]

```
MODULE main
VAR
request : boolean; state : {ready,busy};
ASSIGN
  init(state) := ready;
  next(state) := case
      state = ready & request : busy;
      TRUE : {ready,busy};
  esac;
```

Every program can be alternatively defined in a constraint style:

```
MODULE main
VAR
  request : boolean; state : {ready,busy};
INIT
  state = ready
TRANS
  (state = ready & request) -> next(state) = busy
```



Constraint Style Modeling [2/4]

- ▶ a model can be specified by zero or more constraints on:
 - initial states:

```
INIT <simple_expression>
```

- transitions:
 TRANS <next_expression>
- invariant states:
 INVAR <simple_expression>
- constraints can be mixed with assignments;
- any propositional formula is allowed as constraint;
- not all constraints can be easily rewritten in terms of assignments!

```
TRANS
next(b0) + 2*next(b1) + 4*next(b2) =
(b0 + 2*b1 + 4*b2 + tick) mod 8
```

Constraint Style Modeling [3/4]

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assignment style

:

- by construction, there is always at least one initial state;
- by construction, all states have at least one next state;
- non-determinism is apparent (unassigned variables, set assignments...).



Constraint Style Modeling [4/4]

constraint style

- ▶ INIT constraints can be inconsistent ⇒ no initial state!
 - ▶ any specification (also SPEC 0) is vacuously true.
- ► TRANS constraints can be inconsistent: ⇒ deadlock state!

Example:

```
MODULE main

VAR b : boolean;

TRANS b -> FALSE;
```

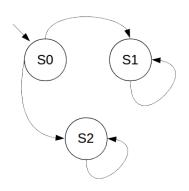
- tip: use check_fsm to detect deadlock states
- non-determinism is hidden:

```
TRANS (state = ready & request) -> next(state) = busy
```



Example: Constraint Style & Case

```
MODULE main()
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   state : {S0, S1, S2};
 DEFINE
   go_s1 := state != S2;
   go_s2 := state != S1;
 TNTT
   state = S0;
 TRANS
 case
   go_s1 : next(state) = S1;
   go_s2 : next(state) = S2;
 esac;
```

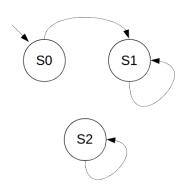


Q: does it correspond to the FSM?



Example: Constraint Style & Case

```
∃MODULE main()
NAKATA DE LA VINNERSITÀ DE LA VINNERSITÀ
                                      state : {S0, S1, S2};
          DEFINE
                                      go_s1 := state != S2;
                                      go_s2 := state != S1;
            TNTT
                                    state = S0;
          TRANS
            case
                                      go_s1 : next(state) = S1;
                                      go_s2 : next(state) = S2;
```



• Q: does it correspond to the FSM? No: cases are evaluated in order!

esac;



Example: Constraint Style & Swap

```
on Section ()
AA A A
    arr: array 0..1 of {1,2};
    i : 0..1;
 ASSTGN
   init(arr[0]) := 1;
   init(arr[1]) := 2;
   init(i) := 0;
   next(i) := 1-i;
```

```
S0 S1

arr[0] = 1 arr[0] = 2
arr[1] = 2 arr[1] = 1
i = 0 i = 1
```

TRANS

```
next(arr[i]) = arr[1-i] &
next(arr[1-i]) = arr[i];
```

Q: does it correspond to the FSM?



Example: Constraint Style & Swap

```
∃MODULE main()
NA VENTOR
   arr: array 0..1 of {1,2};
    i : 0..1;
 ASSIGN
   init(arr[0]) := 1;
   init(arr[1]) := 2;
   init(i) := 0;
   next(i) := 1-i;
TRANS
   next(arr[i]) = arr[1-i] &
   next(arr[1-i]) = arr[i];
```

```
S0 S1

arr[0] = 1 arr[0] = 1
arr[1] = 2
i = 0 i = 1
```

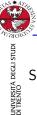
Q: does it correspond to the FSM? No: everything inside the next() operator is evaluated within the next state, indexes included!
3. nuXmy Modeling

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Modules Definition Modules Composition

5. Homework

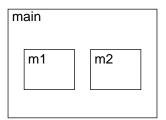


Modules [1/3]

SMV program = main module + 0 or more other modules

- ▶ a module can be instantiated as a VAR in other modules
- dot notation for accessing variables that are local to a module instance (e.g., m1.out, m2.out).

Example:





Modules [2/3]

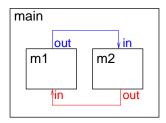
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A module declaration can be parametric:

- a parameter is passed by reference;
- ▶ any expression can be used as parameter;

Example:

```
MODULE counter(in)
VAR out: 0..9;
...
MODULE main
VAR m1 : counter(m2.out);
m2 : counter(m1.out);
```



Modules [3/3]

- modules can be composed
- modules without parameters and assignments can be seen as simple records

Example:

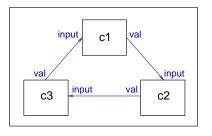


Synchronous composition [1/2]

The composition of modules is **synchronous** by default: *all modules move at each step*.

```
MODULE cell(input)
VAR
  val : {red, green, blue};
ASSIGN
  next(val) := input;

MODULE main
VAR
  c1 : cell(c3.val);
  c2 : cell(c1.val);
  c3 : cell(c2.val);
```





Synchronous composition [2/2]

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A possible execution:

step	c1.val	c2.val	c3.val
0	red	green	blue
1	blue	red	green
2	green	blue	red
3	red	green	blue
4			
5	red	green	blue

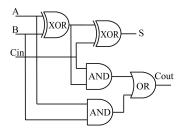


Exercise: Adder [1/3]

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Exercise 7.1: implementing adder

Implement a binary adder that takes into account two 4-bits numbers and returns their sum using an output variable. Implement both a bit-adder and the general adder as two separate modules.





Exercise: Adder [2/3]

```
MODULE bit-adder(in1, in2, cin)
VAR.
  sum : boolean:
  cout : boolean:
ASSIGN
  next(sum) := (in1 xor in2) xor cin;
  next(cout) := (in1 & in2) | ((in1 xor in2) & cin);
MODULE adder(in1, in2)
VAR.
  bit[0] : bit-adder(in1[0], in2[0], bool(0));
  bit[1] : bit-adder(in1[1], in2[1], bit[0].cout);
  bit[2] : bit-adder(in1[2], in2[2], bit[1].cout);
  bit[3] : bit-adder(in1[3], in2[3], bit[2].cout);
DEFINE
  sum[0] := bit[0].sum;
  sum[1] := bit[1].sum:
  sum[2] := bit[2].sum;
  sum[3] := bit[3].sum;
  overflow := bit[3].cout:
```



Exercise: Adder [3/3]

```
MODULE main
 VAR.
    in1: array 0..3 of boolean;
    in2 : array 0..3 of boolean;
    a : adder(in1, in2);
 ASSIGN
   next(in1[0]) := in1[0]: next(in1[1]) := in1[1]:
   next(in1[2]) := in1[2]; next(in1[3]) := in1[3];
   next(in2[0]) := in2[0]; next(in2[1]) := in2[1];
   next(in2[2]) := in2[2]; next(in2[3]) := in2[3];
 DEFINE
    op1 := toint(in1[0]) + 2*toint(in1[1]) + 4*toint(in1[2]) +
         8*toint(in1[3]):
    op2 := toint(in2[0]) + 2*toint(in2[1]) + 4*toint(in2[2]) +
         8*toint(in2[3]):
    sum := toint(a.sum[0]) + 2*toint(a.sum[1]) + 4*toint(a.sum[2]) +
         8*toint(a.sum[3]) + 16*toint(a.overflow);
```

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Homework 7.1: playing with Adder

- Simulate a random execution of the "adder" system;
- ► After how many steps the adder stores the computed final sum value? Is this number constant? Can you explain its behaviour?
- What happens if we initialize both sum and cout inside the bit-adder as FALSE? Can you explain which is the main difference with respect to the original algorithm?
- Can you modify the file in a simple way so that the sum is obtained after a single iteration? (PS: simple means you must modify/add less than 5 lines of code)
- Add a reset control which changes the values of the operands and restarts the computation of the sum



Homework

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Homework 7.2: random calculator

Use nuXmv to create a "random" calculator: it creates two random arrays of 3 integers numbers in the range [1,10], then it randomly choose what operator apply for each pair of elements in the arrays (among sum, subtraction and multiplication) and store it in an output array of 3 elements called *res*. The results must be defined in 3 steps: in the first iteration you'll store the random operation between elements with index 0, in the second iteration the random operation between elements with index 1 and the same for the last index. Use an additional variable, *index*, to take into account this evolution.