

Course “**Fundamentals of Artificial Intelligence**”
EXAM TEXT

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1

Given the following symbols, representing concept, relation and individual names in the alien language of the remote planet **Sgotz**:

- a set of primitive $\mathcal{ALCQ}$ concept names: {Perun, Malle, Feale, Dotot, Egier}
- a set of $\mathcal{ALCQ}$ relation names: {haCidod}
- a set of $\mathcal{ALCQ}$ individual names: {Lok, Bek, Mop, Dib, Ate, Jud, Etu, Gop}

and the following $\mathcal{ALCQ}$ $\mathcal{T}$ -box $\mathcal{T}$ and $\mathcal{A}$ -box $\mathcal{A}$:

$\mathcal{T}$	$\mathcal{A}$
Perun $\langle \text{primitive concept} \rangle$	Mop : Woana; Etu : Woana; Gop : Woana; Lok : Woana;
Feale $\langle \text{primitive concept} \rangle$	
Malle $\langle \text{primitive concept} \rangle$	Bek : Mnana; Ate : Mnana; Jud : Mnana; Dib : Mnana;
Dotot $\langle \text{primitive concept} \rangle$	
Egier $\langle \text{primitive concept} \rangle$	Ate : Dotot; Mop : Dotot
Woana $\equiv \text{Perun} \sqcap \text{Feale}$	
Mnana $\equiv \text{Perun} \sqcap \text{Malle}$	Etu : Egier; Gop : Egier; Lok : Egier
Moeth $\equiv \text{Woana} \sqcap \exists \text{haCidod}.\text{Perun}$	
Faeth $\equiv \text{Mnana} \sqcap \exists \text{haCidod}.\text{Perun}$	$\langle \text{Bek}, \text{Mop} \rangle : \text{haCidod}; \langle \text{Bek}, \text{Ate} \rangle : \text{haCidod};$
Panet $\equiv \text{Perun} \sqcap \text{haCidod}.\text{Perun}$	$\langle \text{Bek}, \text{Etu} \rangle : \text{haCidod};$
Gamae $\equiv \text{Moeth} \sqcap \text{haCidod}.\text{Panet}$	
Gafae $\equiv \text{Faeth} \sqcap \text{haCidod}.\text{Panet}$	$\langle \text{Mop}, \text{Gop} \rangle : \text{haCidod}; \langle \text{Mop}, \text{Jud} \rangle : \text{haCidod};$
Gapan $\equiv \text{Panet} \sqcap \text{haCidod}.\text{Panet}$	$\langle \text{Mop}, \text{Dib} \rangle : \text{haCidod}; \langle \text{Mop}, \text{Lok} \rangle : \text{haCidod};$

For each of the following $\mathcal{ALCQ}$ queries to $\mathcal{T} \cup \mathcal{A}$, say if it is true or false.

- Mop : Moeth $\sqcap (\geq 3)\text{haCidod}.\text{Egier}$
- Bek : Faeth $\sqcap (\geq 2)\text{haCidod}.\text{Dotot}$
- Bek : Faeth $\sqcap \exists \text{haCidod}.\text{Panet}$
- Bek : Gapan $\sqcap \forall \text{haCidod}.\text{Moeth}$

[SCORING [0...100]:

- +25pts for each correct answer
- -25pts for each incorrect answer
- 0pts for each unanswered question

]

2

For each of the following facts about conditional independence, say if it is true or false.

- (a) If D and E are conditionally independent given F, then $\mathbf{P}(D, F|E) = \mathbf{P}(D, F)$
- (b) If D and E are conditionally independent given F, then $\mathbf{P}(D, E|F) = \mathbf{P}(D, E)$
- (c) If D and E are conditionally independent given F, then $\mathbf{P}(D, E, F) = \mathbf{P}(D)\mathbf{P}(E)\mathbf{P}(F)$
- (d) If D and E are conditionally independent given F, then $\mathbf{P}(D, E, F) = \mathbf{P}(D|F)\mathbf{P}(E|F)\mathbf{P}(F)$

[SCORING [0...100]:

- +25pts for each correct answer
- -25pts for each incorrect answer
- 0pts for each unanswered question

]

3

Given a generical search problem, assume time and space complexity are measured in terms of

b : maximum branching factor of the search tree

m : maximum depth of the state space (assume m is finite)

d : depth of the shallowest solution

Assume also that all steps cost are 1.

For each of the following facts, say if it is true or false

- (a) Breadth-First Search requires $O(b^m)$ memory to find a solution.
- (b) Breadth-First Search is optimal
- (c) Depth-First Search with loop-prevention requires $O(b^d)$ steps to find a solution.
- (d) Depth-First Search with loop-prevention requires $O(b^d)$ memory to find a solution.

[SCORING [0...100]:

- +25pts for each correct answer
- -25pts for each incorrect answer
- 0pts for each unanswered question

]

4

Consider propositional logic (PL); let F, C, D, E, B, A, G be atomic propositions. We adopt the set notation for resolution rules, s.t. Γ denotes a set of clauses.

For each of the following statements, say if it is true or false.

(a) The following is a correct application of the PL unit-resolution rule:

$$\frac{\Gamma, (\neg D), (\neg A \vee \neg D \vee F)}{\Gamma, (\neg D), (\neg A \vee F)}$$

(b) The following is a correct application of the PL clause-subsumption rule:

$$\frac{\Gamma, (\neg A \vee F), (\neg A \vee \neg D \vee F)}{\Gamma, (\neg A \vee \neg D \vee F)}$$

(c) The following is a correct application of the PL general resolution rule:

$$\frac{\Gamma, (\neg D \vee \neg E \vee \neg A), (\neg F \vee \neg D \vee \neg E)}{\Gamma, (\neg E \vee \neg F \vee \neg A)}$$

(d) The following is a correct application of the PL general resolution rule:

$$\frac{\Gamma, (\neg A \vee \neg D \vee F), (\neg A \vee \neg F \vee E)}{\Gamma, (\neg D \vee E)}$$

[SCORING [0...100]:

- +25pts for each correct answer
- -25pts for each incorrect answer
- 0pts for each unanswered question

]

5

In the following FOL formulas, let R , P , Q , and $>$, $\leq$, $<$, $\geq$ denote predicates,

h , f , g , F_1 , F_2 , F_3 and $+$, $-$, $\cdot$, $/$ denote functions,

x , y , z , x_1 , x_2 , x_3 denote variables,

A , B , C , C_1 , C_2 , C_3 and 0 , 1 , 2 , 3 , 4 denote constants.

For each of the following facts, say if it is true or false.

(a) The FOL formula $(\forall x_2 \exists x_1. R(x_1, x_2)) \rightarrow (\exists x_1 \forall x_2. R(x_1, x_2))$ is valid.

(b) The FOL formula $(\exists x_1. \neg R(x_1)) \leftrightarrow (\neg \forall x_1. R(x_1))$ is valid

(c) The FOL formula $\forall x. ((x > 2) \rightarrow (x > 1))$ is valid.

(d) The FOL formula $(2 > 4)$ is unsatisfiable.

[SCORING [0...100]:

- +25pts for each correct answer
- -25pts for each incorrect answer
- 0pts for each unanswered question

]

6

Consider the following CNF formula in PL:

$$\begin{aligned}
 &(\neg E \vee B \vee N) \wedge \\
 &(\neg A \vee H \vee C) \wedge \\
 &(\neg H \vee I \vee A) \wedge \\
 &(\neg L \vee C \vee \neg M) \wedge \\
 &(\neg G \vee \neg A \vee E) \wedge \\
 &(\neg E \vee \neg G \vee A) \wedge \\
 &(\neg E \vee \neg F \vee \neg A) \wedge \\
 &(\neg I \vee L \vee M) \wedge \\
 &(\neg N \vee L \vee M)
 \end{aligned}$$

Consider the WalkSAT algorithm, with probability parameter $p = 0.2$. Suppose at a given step the current assignment is

$$\{A, \neg B, C, D, E, \neg F, G, \neg H, I, \neg L, \neg M, \neg N\}.$$

Assuming the most-likely event happens, describe what the assignment is after the next step.

[SCORING: [0...100], 100 pts for a correct answer, no penalties for wrong answers.]

7

An experienced doctor has to cope with an epidemic of covid19, where 60% of people of the area have been infected. She considers the following possible symptoms:

Symptom #1: headache;

Symptom #2: nausea;

Symptom #3: fever.

She models the cause-effect relation as a **Naive Bayes Model scenario**, s.t the effects are considered conditionally independent given the cause, and she knows from statistics the following data: ¹

$P(headache covid19)$	$= 0.8$
$P(headache \neg covid19)$	$= 0.1$
$P(nausea covid19)$	$= 0.4$
$P(nausea \neg covid19)$	$= 0.2$
$P(fever covid19)$	$= 0.6$
$P(fever \neg covid19)$	$= 0.3$

She is informed that one patient has nausea and fever but not headache. Compute the probability that such patient has contracted covid19.

Notice: *the problem must be solved my using the Naive Bayes Model scenario. Any attempt to use any other technique will be considered incorrect.*

[SCORING: [0...100], 100 pts for correct answer, no penalties for wrong answers.]

¹The data here are pure fantasy and are not supposed to correspond to actual medical data.

8

- (a) Describe as Pseudo-Code the Depth-Limited Search and Iterative-Deepening procedures.
- (b) calling B the branching factor and D the depth of the shallowest solution,
- what is the time complexity of the Iterative-Deepening procedure?
 - what is the memory complexity of the Iterative-Deepening procedure?

[SCORING: [0...100], 75 pts for a correct answer to question (a), 25 pts for correct answer to question (b); no penalties for wrong answers.]

9

- (a) Describe as Pseudo-Code the specialized solving procedure for tree-structured CSPs.
- (b) Say if the following sentence is true or false, and briefly explain why.
- It requires polynomial time in worst-case if the input constraint graph has no loops.

[SCORING: [0...100], 75 pts for a correct answer to question (a), 25 pts for correct answer to question (b); no penalties for wrong answers.]

10

Given the following Sudoku scenario:

1	2	3	4	5	6	7	8	9	
1		8							A
2				6					B
3						4	5		C
8								5	D
7								4	E
6								9	F
5	8	1							G
	7	2		9					H
		3							I

- (a) Apply the AC-3 algorithm. Describe in the right sequence the domains of unassigned nodes whose domains become unary after one run of AC-3. (E.g.:
 $D_{A1} := \{3\}$,
 $D_{B1} := \{7\}$,
 ...)
- (b) Can AC-3 reduce to unary the domains of nodes $B3$ and $C3$?
- (c) After one run of AC-3, is the resulting graph arc-consistent?

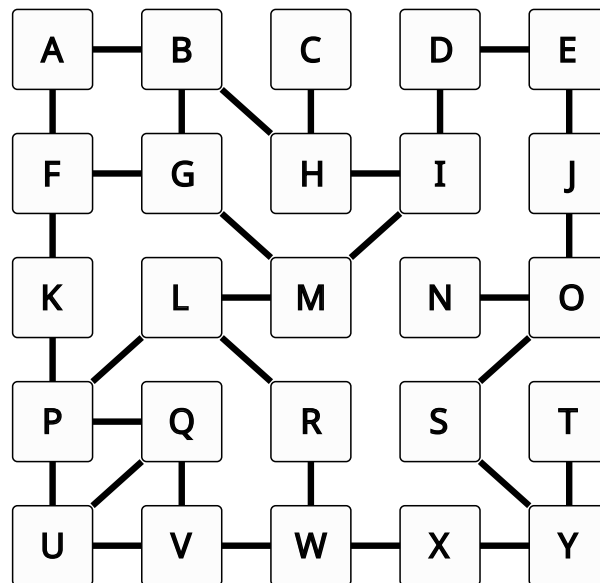
[SCORING: [0...100], 50pts for correct answer (a), 25pts each for correct answer (b) and (c). No penalties for wrong answers..]

11

In the following state graph, apply *breadth-first search* and report for each step:

- the node extracted from the frontier;
- the nodes added to the frontier in the current step.

Actions are sorted according to the (ascending) alphabetical order of the destination.



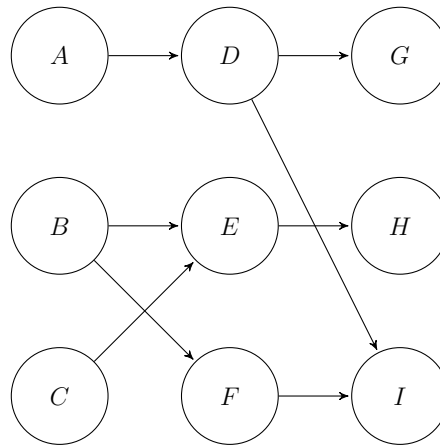
Start: M - Goal: X

[SCORING: [0...100], 100pts for a fully correct solution, -10pts for each error in the resolution process. The score cannot go below 0..]

12

Consider the following actions with durations / dependencies:

a	duration(a)
A	1
B	2
C	1
D	2
E	2
F	3
G	3
H	1
I	2



1) Compute the earliest / latest possible start time (ES/LS) for each action using the Critical Path method. [40pts.]

Assume that completing each action requires one unit of a reusable resource:

- 2) Report an optimal schedule given 2 reusable resources in the grid below. [40pts.]
- 3) What would be the optimal execution time given 1 reusable resource? [10pts.]
- 4) What would be the optimal execution time given infinite resources? [10pts.]

R1:

--	--	--	--	--	--	--	--	--	--	--

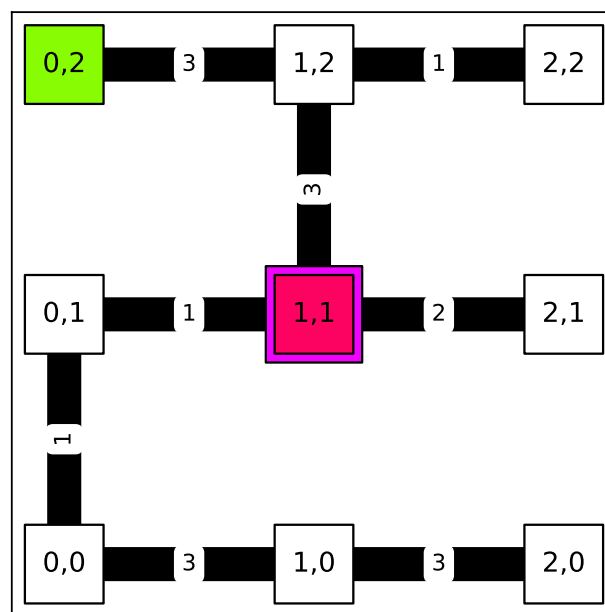
R2:

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[SCORING: [0...100], 100pts for a fully correct solution. The score cannot go below 0..]

13

In the following state graph, apply *LRTA** and report the list of visited states, including repetitions (e.g. $(0, 1) \rightarrow (0, 0) \rightarrow (0, 1) \rightarrow \dots$). The order of (untried) actions is $[up, right, down, left]$.

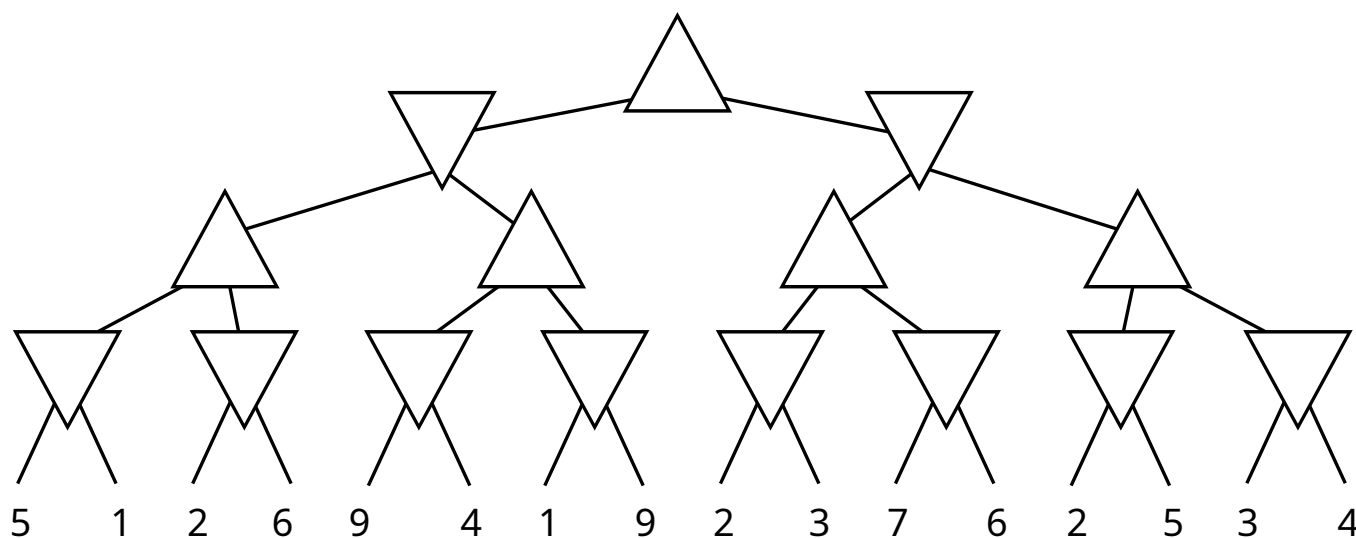


Start: (1, 1) - Goal: (0, 2)

[SCORING: [0...100], 100pts for a fully correct solution, -10pts for each error in the resolution process. The score cannot go below 0..]

14

Use *Minimax with α, β -pruning* to propagate the utilities from the leaves to the root of the tree.



For each node report the values of α , β , as well as its returned value v **when the recursive calls ends**. Use the following format:

$$\begin{array}{c} \alpha \\ \beta \end{array} \triangle v$$

Additionally, clearly mark in the tree the pruned branches.

[SCORING: [0...100], 100pts for a fully correct solution, -20pts for each error in the resolution process. The score cannot go below 0..]

15

Use *hill climbing* for solving the maximization problem over (x, y) with the following objective function:

y								
7	0	2	3	4	4	2	1	0
6	1	1	4	5	5	3	2	1
5	2	3	5	8	6	4	2	3
4	3	5	6	9	10	6	5	1
3	3	4	7	10	9	6	4	1
2	2	2	4	6	7	5	4	3
1	1	1	3	5	4	3	1	1
0	0	1	2	3	4	2	2	0
	0	1	2	3	4	5	6	7
	x							

The next state is selected among the neighbors with strictly higher objective function value with *probability proportional to their objective function value*. Neighbors of (x, y) are sorted as follows:

$$(x-1, y-1), (x, y-1), (x+1, y-1), (x-1, y), (x+1, y), (x-1, y+1), (x, y+1), (x+1, y+1)$$

The choice vector is: $[1/4, 3/4]$.

The *initial state* is: $(0, 7)$.

For each step in the resolution process report (1) the current state; (2) the list of candidate next states.

[SCORING: [0...100], 100pts for a fully correct solution, -20pts for each error in the resolution process. The score cannot go below 0..]