Fundamentals of Artificial Intelligence Chapter 12: **Knowledge Representation**

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Outline

- Ontologies and Ontological Engineering
- Categories and Objects
- Reasoning about Knowledge
- Reasoning about Categories
 - Semantic Networks (hints)
 - Description Logics

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Generalities

Q: What content do we put into an agent's KB?

- how do we organize such content?
- how do we represent facts about the world?
- A whole Al field: Knowledge Representation, KR
 - often combined with Automated Reasoning on KB
 - ⇒ Knowledge Representation & Reasoning, KRR
- KR: use logics (e.g. FOL) to represent the most important aspects of the real world, such as: action, space, time, knowledge, belief
- Topics:
 - ontologies and ontological engineering
 - objects and categories, composite objects, measurements, ...
 - actions and change, events, temporal intervals, ...
 - reasoning about knowledge & beliefs
 - reasoning about categories
 - default reasoning
 - ...

Knowledge Engineering and Ontological Engineering

Knowledge Engineering

- The activity to formalize a specific problem or task domain
- Relevant questions to be addressed:
 - What are the relevant facts, objects, relations ... ?
 - Which is the right level of abstraction?
 - What are the queries to the KB (inferences)?

Ontological Engineering

- The activity to build general-purpose ontologies
 - should be applicable in any special-purpose domain (with the addition of domain-specific axioms)
 - In non trivial domains, reasoning and problem solving could involve several areas of knowledge simultaneously
 - ⇒ different areas of knowledge must be combined
- Several attempts to build general-purpose ontologies
 - CYC, DBpedia, TextRunner, ...
 - not very successful so far

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Categories and Objects

Categories, Objects, Members and Subclasses

- KR requires the organisation of objects into categories
 - interaction at the level of the object
 - reasoning at the level of categories
 - ex: typically we want to buy a basketball, rather than a particular basketball instance
- Categories play a role in predictions about objects
 - agent infers the presence of certain objects from perceptual input
 - infers category from the perceived properties of the objects,
 - uses category information to make predictions about the objects
- Categories can be represented in two ways by FOL
 - predicates (ex Basketball(x)): relations
 - reification of categories into objects (ex Basketballs): sets
 - ⇒ allows categories to be argument of predicates/functions
- Membership of a category as set membership
 - ex: Member(b, Basketballs) (abbr. $b \in Basketballs$)
- Subcategories (aka subclasses) are (strict) subsets
 - ex: Subset(Basketballs, Balls) (abbr. Basketballs ⊂ Balls)

Categories and Objects [cont.]

Inheritance and Taxonomies

- A subcategory inherits the properties of the category
 - ex:

```
if \forall x.(x \in Food \rightarrow Edible(x)), Fruit \subset Food, Apples \subset Fruit then \forall x.(x \in Apple \rightarrow Edible(x))
```

- A member inherits the properties of the category
 - if a ∈ Apples, then Edible(a)
- Subclass relation organize categories into taxonomies (aka taxonomic hierarchies)
 - ex: taxonomy of >10M living&extinct species
 - ex: Dewey Decimal System: taxonomy of all fields of knowledge

Categories and Objects [cont.]

FOL Reasoning about Categories

- FOL allows to state facts about categories:
 - an object is a member of a category
 BB₉ ∈ Basketballs
 - a category is a subclass of another category Basketballs ⊂ Balls
 - all members of a category have some properties
 ∀x.(x ∈ Basketballs → Spherical(x))
 - members of a category can be recognized by some properties
 ∀x.((Orange(x) ∧ Round(x) ∧ Diameter(x) = 9.5" ∧ x ∈ Balls)
 → x ∈ Basketballs)
 - category as a whole has some properties
 Dogs ∈ DomesticatedSpecies
- New categories can be defined by providing necessary and sufficient conditions for membership
 - $\forall x.(x \in Bachelors \leftrightarrow (Unmarried(x) \land x \in Adults \land x \in Males))$

Categories and Objects [cont.]

Derived relations

Two or more categories in a set s are disjoint iff they have no members in common

```
• \textit{Disjoint}(s) \leftrightarrow (\forall c_1 c_2. \ ((c_1 \in s \land c_2 \in s \land c_1 \neq c_2) \rightarrow \textit{Intersection}(c_1, c_2) = \emptyset)
```

- ex:
 Disjoint({Animals, Vegetables}), Disjoint({Insects, Birds, Mammals, Reptiles}),
- A set of categories s is an exhaustive decomposition of a category c iff all members of c are covered by categories in s
 - ExaustiveDecomposition $(s, c) \leftrightarrow \forall i. (i \in c \leftrightarrow (\exists c_2. (c_2 \in s \land i \in c_2)))$
 - ex: E.D.({Americans, Canadians, Mexicans}, NorthAmericans)
- A disjoint exhaustive decomposition is a partition
 - $Partition(s, c) \leftrightarrow (Disjoint(s) \land ExhaustiveDecomposition(s, c))$
 - ex: Partition({NorthernItalians, CentralItalians, SouthernItalians, InsularItalians}, Italians)

Digression: Natural Kinds

- Many categories have no clear-cut definition (ex: chair, bush, ...)
 - Ex: tomatoes are sometimes green, red, yellow, black; they are mostly round
- One useful solution: category "Typical(.)", s.t. Typical(c) $\subseteq c$
 - most knowledge about natural kinds will actually be about their typical instances
 - ex: $\forall x.(x \in \mathit{Typical}(\mathit{Tomatoes}) \rightarrow (\mathit{Red}(x) \land \mathit{Round}(x)))$
- ⇒ We can write down useful facts about categories without providing exact definitions

Note

Quine (1953) challenged the utility of the notion of strict definition.

- Ex: "bachelor": is the Pope a bachelor?
 - ⇒ technically yes, but misleading

Physical Composition

- PartOf(.,.) relation: One object may be part of another
 - PartOf(Bucharest, Romania)
 - PartOf(Romania, EasternEurope)
 - PartOf(EasternEurope, Europe)
- *PartOf*(.,.) is reflexive and transitive:
 - ∀x.PartOf(x,x)
 - $\forall x, y, z.((PartOf(x, y) \land PartOf(y, z)) \rightarrow PartOf(x, z))$
 - ⇒ PartOf(Bucharest, Europe)
- Categories of composite objects are often characterized by structural relations among parts.
 Ex: Biped

$$\begin{array}{lll} Biped(a) & \Rightarrow & \exists \, l_1, l_2, b \; Leg(l_1) \land Leg(l_2) \land Body(b) \; \land \\ & & PartOf(l_1, a) \land PartOf(l_2, a) \land PartOf(b, a) \; \land \\ & & Attached(l_1, b) \land Attached(l_2, b) \; \land \\ & & l_1 \neq l_2 \land [\forall \, l_3 \; Leg(l_3) \land PartOf(l_3, a) \; \Rightarrow \; (l_3 = l_1 \lor l_3 = l_2)] \end{array}$$

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Other concepts & relations: PartPartition, BunchOf...

Measurements

Quantitative Measurements

- Objects may have "quantitative" properties
 - e.g. height, mass, cost, ...
- Values that we assign to these properties are measures
- Can be represented by unit functions
 - ex $Length(L_1) = Inches(1.5) \land Inches(1.5) = Centimeters(3.81)$
- Conversion between units:
 - $\forall i. \ Centimeters(2.54 \times i) = Inches(i)$
- Measures can be used to describe objects:
 - ex: Diameter(Basketball₁₂) = Inches(9.5)
 - ex: ListPrice(Basketball₁₂) = \$(19)
 - ex: $\forall d.(d \in \textit{Days} \rightarrow \textit{Duration}(d) = \textit{Hours}(24))$

Measurements [cont.]

Qualitative Measurements

- Some measures have no scale
 - ex: beauty, deliciousness, difficulty,...
- Most important aspect of measures: they are orderable
 - Ex: Deliciousness(SacherTorte) > Deliciousness(BrussellSprout)
 - Ex: Beauty(PaulNewmann) > Beauty(MartyFeldman)
 - Ex: Difficulty(Prove_P≠NP) > Difficulty(SolvePuzzle)
- Allow for reasoning by exploiting transitivity of monotonicity:

```
 \forall e_1e_2.((e_1 \in Exercises \land e_2 \in Exercises \land \textit{Wrote}(\textit{Norvig}, e_1) \land \textit{Wrote}(\textit{Russell}, e_2)) \\ \rightarrow \textit{Difficulty}(e_1) > \textit{Difficulty}(e_2)) \\ \forall e_1e_2.((e_1 \in Exercises \land e_2 \in Exercises \land \textit{Difficulty}(e_1) > \textit{Difficulty}(e_2)) \\ \rightarrow \textit{ExpectedScore}(e_1) < \textit{ExpectedScore}(e_2)) \\ \forall e_1e_2.(ExpectedScore(e_1) < ExpectedScore(e_2) \rightarrow \textit{Pick}(e_1, e_2) = e_2 \\ \text{Then: } (\textit{Wrote}(\textit{Norvig}, E_1) \land \textit{Wrote}(\textit{Russell}, E_2)) \models \textit{Pick}(E_1, E_2) = E_2
```

 Qualitative physics: a subfield of AI that investigates how to reason about physical systems without numerical computations

Objects vs Stuff

- There are countable objects
 - e,g, apples, holes, theorems, ...
- ... and mass objects, aka stuff or substances
 - e.g. butter, water, energy, ...
- → Intuitive meaning "an amount/quantity of..."
 - ex: b ∈ butter: "b is an amount/quantity of butter"
 - Any part of stuff is still stuff:
 - ex: $\forall b, p.((b \in Butter \land PartOf(p, b)) \rightarrow p \in Butter)$
 - Can define sub-categories, which are stuff
 - ex: UnsaltedButter ⊂ Butter
 - Stuff has a number of intrinsic properties, shared by its subparts
 - e.g., color, fat content, density ...
 - ex: $\forall b.(b \in Butter \rightarrow MeltingPoint(b, Centigrade(30)))$
 - Stuff has no extrinsic properties
 - e.g., weight, length, shape, ...

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Agents' Attitudes

- Intelligence is intrinsically social: agents need to negotiate and coordinate with other agents
- In multi-agents scenarios, to predict what other agents will do, we need methods to model mental states of other agents
 - representations of other agents' knowledge (and beliefs, goals)
- Agent's Propositional attitudes: Knows, Believes, Wants,...
 - ex "Lois Knows that Superman can fly"

Problem

Propositional attitudes do not behave as regular predicates

issue: Referential opacity vs. referential transparency

Referential opacity vs. Referential transparency

- Consider the assertion "Lois knows that Superman can fly"
- Consider the FOL formalization: *Knows(Lois, CanFly(Superman))*
- Minor Problem: CanFly(Superman) is a formula
 - ⇒ cannot occur as argument of a predicate
 - → must apply reification → make it a term
- Major Problem (Referential Transparency of FOL):
 - since Superman is Clark Kent (but Lois doesn't know it!), FOL allows to conclude "Lois knows that Clark Kent can fly":

```
\textit{Superman} = \textit{Clark} \land \textit{Knows}(\textit{Lois}, \textit{CanFly}(\textit{Superman}))
```

- $\models_{FOL} Knows(Lois, CanFly(Clark))$
- ⇒ Wrong inference! (Lois doesn't know Clark Kent can fly!)
- Hint: FOL predicates transparent to equality reasoning:

```
t = s \land P(s, ...) \models_{FOL} P(t, ...)
```

Need a logic which is opaque to equality reasoning (aka Referential Opacity):
 Modal Logics

Modal Logics

- Modal logics include special modal operators that take formulas (not terms!) as arguments
 - "A knows P" is represented with K_AP (P formula, not term!)
 - ex: "Lois knows that Superman can fly": K_{Lois} CanFly(Superman)
 - ex: "Lois knows Clark Kent knows if he is Superman or not": $K_{Lois}(K_{Clark}|dentity(Superman, Clark)) \lor K_{Clark} \neg Identity(Superman, Clark))$
- Properties in all modal logics:
 - $K_A(P \wedge Q) \iff K_AP \wedge K_AQ$
 - $K_AP \vee K_AQ \models K_A(P \vee Q)$, but $K_A(P \vee Q) \not\models K_AP \vee K_AQ$ (e.g. $K_A(P \vee \neg P) \not\models K_AP \vee K_A \neg P$)
- The following axiom holds in all (normal) modal logics:

```
K: (K_A\phi \land K_A(\phi \to \psi) \to K_A\psi (distribution axiom): "A is able to perform propositional inference"
```

- The following axioms hold in some (normal) modal logics:
 - $T: K_A \varphi \to \varphi$ (knowledge axiom): "A knows only true facts"
 - 4: $K_{A}\varphi \to K_{A}K_{A}\varphi$ (positive-introspection axiom): "If A knows fact φ , then [s]he knows [s]he knows it"
 - 5 : $\neg K_A \varphi \rightarrow K_A \neg K_A \varphi$ (negative-introspection axiom):
 - "If A doesn't know φ , then [s]he knows [s]he doesn't know it"
- Referential Opacity: Superman = Clark \land K_{Lois} CanFly(Superman) $\not\models$ K_{Lois} CanFly(Clark)
- Reasoning in (propositional) Modal logics is NP-hard (most often even PSPACE-hard)

Semantics of Modal Logics

- A model (Kripke model) is a collection of possible world states w_i (aka worlds, states)
 - possible states are connected in a graph by accessibility relations
 - ullet one relation for each distinct modal operator K_A
- w_1 is accessible from w_0 wrt. K_A if everything which holds in w_1 is consistent with what A knows in w_0 (written " $Acc(K_A, w_0, w_1)$ " or " $w_0 \stackrel{K_A}{\longmapsto} w_1$ ")
 - \implies $K_A \varphi$ holds in w_o iff φ holds in every state w_i accessible from w_0
 - the more is known in w_0 , the less states are accessible from w_0
 - remark: two possible states may differ also for what an agent knows there
- Different modal logics differ by different properties of $Acc(K_A,...)$
 - $T: K_A \varphi \to \varphi$ holds iff $Acc(K_A, ...)$ reflexive: $w \stackrel{K_A}{\longmapsto} w$
 - 4 : $K_A \varphi \to K_A K_A \varphi$ holds iff $Acc(K_A, ...)$ transitive: $w_0 \stackrel{K_A}{\longmapsto} w_1$ and $w_1 \stackrel{K_A}{\longmapsto} w_2 \Longrightarrow w_0 \stackrel{K_A}{\longmapsto} w_2$
 - 5: $\neg K_A \varphi \to K_A \neg K_A \varphi$ holds iff $Acc(K_A, ...)$ euclidean: $w_0 \stackrel{K_A}{\longmapsto} w_1$ and $w_0 \stackrel{K_A}{\longmapsto} w_2 \Longrightarrow w_1 \stackrel{K_A}{\longmapsto} w_2$

4: transitive

$$w_0$$
 w_1 w_2

5: euclidean

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Semantics of Modal Logics: Some Remarks

Assume the knowledge of *A* is correct: $T: K_A \varphi \to \varphi$ ("Everything which *A* knows holds")

- $\not\models \varphi \to K_A \varphi$: A does not know everything which holds!
- The less states are accessible, the more precise is the knowledge of A
 - uncertainty on some information makes accessible states different
 A does not know the state [s]he is
 - complete knowledge: current state is the only successor of itself
 A knows exactly the state [s]he is

$$w_0$$
 w_1 w_0 w_0 Uncertainty w Complete knowledge

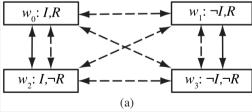
Notice the difference:

- $K_A \neg P$: agent A knows that P does not hold (in all accessible states P is false)
- $\neg K_A P$: agent A does not know if P holds (in some accessible states P is false)

$$\implies K_A \neg P \models \neg K_A P$$
, but $\neg K_A P \not\models K_A \neg P$

Accessibility relations: $K_{Superman}$ (solid arrows) and K_{Lois} (dotted arrows).

- Legenda:
 - R: "the weather report says tomorrow will rain"
 - I: "Superman's secret identity is Clark Kent."
 - Ex: $K_{Lois}(K_{Clark}I \vee K_{Clark} \neg I)$: "Lois Knows that Clark Knows if he is Superman or not."
- Superman knows his own identity: $K_{Superman}I \lor K_{Superman}\neg I$, and
 (a) neither Superman nor Lois has seen the weather report, she knows Superman knows if he is Clark $(\neg K_{Lois}R \land \neg K_{Lois}\neg R) \land (\neg K_{Superman}R \land \neg K_{Superman}\neg R) \land K_{Lois}(K_{Superman}I) \lor K_{Superman}\neg I)$

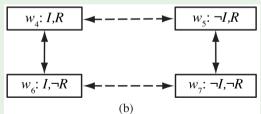


(self-loop arrows not reported)

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- Superman knows his own identity: $K_{Superman}I \lor K_{Superman}I$, and (b) Lois has seen the weather report, Superman has not, but he knows that Lois has seen it $(K_{Lois}R \lor K_{Lois}\neg R) \land (\neg K_{Superman}R \land \neg K_{Superman}\neg R)$ $K_{Lois}(K_{Superman}I \lor K_{Superman}\neg I) \land K_{Superman}(K_{Lois}R \lor K_{Lois}\neg R)$



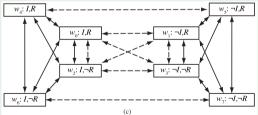
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• Superman knows his own identity: $K_{Superman}I \lor K_{Superman}\lnot I$, and (c) Lois may or may not have seen the weather report, Superman has not: $((\lnot K_{Lois}R \land \lnot K_{Lois}\lnot R) \lor (K_{Lois}R \lor K_{Lois}\lnot R)) \land (\lnot K_{Sup}.R \land \lnot K_{Sup}.\lnot R) K_{Lois}(K_{Superman}I \lor K_{Superman}\lnot I)$



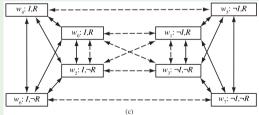
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• Superman knows his own identity: $K_{Superman}I \lor K_{Superman}I$, and (c) Lois may or may not have seen the weather report. Superman has not: $((\neg K_{Lois}R \land \neg K_{Lois}\neg R) \lor (K_{Lois}R \lor K_{Lois}\neg R)) \land (\neg K_{Sup.}R \land \neg K_{Sup.}\neg R) K_{Lois}(K_{Superman}I \lor K_{Superman}I)$



(self-loop arrows not reported)

Consider the previous example.

• For each scenario (a), (b) and (c) define doubly-nested knowledge in terms of

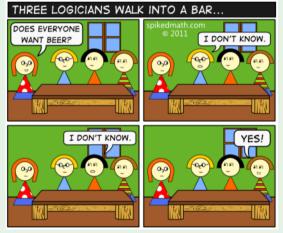
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 \begin{array}{l} [\neg] K_{Lois} [\neg] K_{Lois} [\neg] I, \\ [\neg] K_{Lois} [\neg] K_{Lois} [\neg] R, \\ [\neg] K_{Sup.} [\neg] K_{Sup.} [\neg] I, \\ [\neg] K_{Sup.} [\neg] K_{Sup.} [\neg] R \end{array}
```

Consider (normal) modal logics (i.e., axioms K, T, 4 and 5 hold).

Let IsRed(Pen), IsOnTable(Pen) be possible facts, let Mary, John be agents and let K_{Mary} , K_{John} denote the modal operators "Mary knows that..." and "John knows that..." respectively. For each of the following facts, say if it is true or false.

- If $K_{Mary} \neg IsRed(Pen)$ holds, then $\neg K_{Mary} IsRed(Pen)$ holds
- If $\neg K_{Mary}$ IsRed(Pen) holds, then K_{Mary} \neg IsRed(Pen) holds
- If K_{John}IsRed(Pen) and IsRed(Pen) ↔ IsOnTable(Pen) hold, then K_{John}IsOnTable(Pen) holds
- If K_{Mary} IsRed(Pen) and K_{Mary} (IsRed(Pen) \to K_{John} IsRed(Pen)) hold, then $K_{Mary}K_{John}$ IsRed(Pen)) holds

- Why does the third logician answers "Yes"?
- Formalize and solve the problem by means of modal logic (K+T+4+5)



(Courtesy of Maria Simi, UniPI)

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Reasoning Systems for Categories

Q. How to organize and reason with categories?

- Semantic Networks
 - allow to visualize knowledge bases
 - efficient algorithms for category membership inference
 - limited expressivity
 - many variants
- Description Logics (DLs)
 - formal language for constructing and combining category definitions
 - (relatively) efficient algorithms to decide subset and superset relationships between categories
 - many DLs
 - up to very high expressivity
 - up to very high complexity (e.g., DOUBLY-EXPTIME)

Semantic Networks

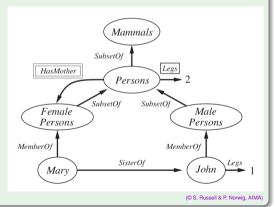
- Allow for representing individual objects, categories of objects, and relations among objects
- A Semantic Network is a graph where:
 - nodes, with a label, correspond to concepts
 - arcs, labelled and directed, correspond to binary relations between concepts (aka roles)
- Two kinds of nodes:
 - Generic concepts, corresponding to categories/classes
 - Individual concepts, corresponding to individuals
- Two special relations are always present, with different names
 - IS-A, aka SubsetOf/SubclassOf (subclass)
 - InstanceOf aka MemberOf (membership)
- Inheritance detection straightforward
- Ability to represent default values for categories
- Limited expressive power: cannot represent negation, disjunction, nested function symbols, existential quantification

Semantic Networks: Example

Notice

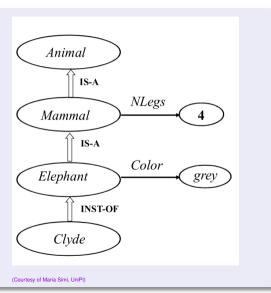
- "HasMother" is a relation between persons (individuals) (categories do not have mothers)
- "HasMother" (double-boxed notation) means $\forall x. (x \in Persons \rightarrow [\forall y. (HasMother(x, y) \rightarrow y \in FemalePersons)])$
- "Legs" is a property of single persons (individuals)
- "Legs" (single-boxed notation) means:

$$\forall x.(x \in Persons \rightarrow Legs(x, 2))$$



Inheritance in Semantic Networks

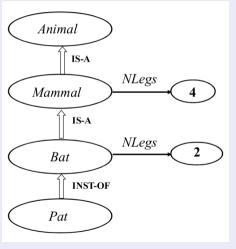
- Inheritance conveniently implemented as link traversal
- Q. How many legs has Clyde?
- follow the INST-OF/IS-A chain until find the property NLegs



Inheritance with Exceptions

The presence of exceptions does not create any problem with S.N.

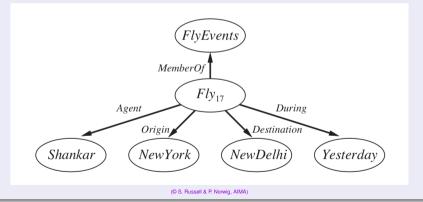
- How many legs has Pat?
- Just take the most specific information: the first that is found going up the hierarchy
- ability to represent default values for categories



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Encoding N-Ary Relations

- Semantic networks allow only binary relations
- Q. How to represent n-ary relations?
- ⇒ Reify the proposition as an event belonging to an appropriate event category
 - ex "Fly₁₇" for Fly(Shankar, NewYork, NewDelhi, Yesterday)



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Description Logics

- Designed to describe definitions and properties about categories
- Principal inference tasks:
 - Subsumption: check if one category is a subset (sub-category) of another
 - Classification: check whether an object belongs to a category
 - Consistency: check if category membership criteria are satisfiable
- Defaults and exceptions are lost

Concepts, Roles, Individuals

- Concepts, corresponding to unary relations
 - T, ⊥: universal and empty concepts
 - atomic concepts: ex: Female, Male, Article, Journalist,...
 - operators for the construction of complex concepts: and (\Box) , or (\sqcup) , not (\neg) , all (\forall) , some (\exists) , atleast $(\geq n)$, atmost $(\leq n)$, ...
 - ex: mothers (i.e., women who have children) of at least three female children: $Woman \sqcap \exists hasChildren.Person \sqcap \geq 3 \ hasChild.Female$
 - ex: articles that have authors and whose authors are all journalists:
 Article □ ∃hasAuthor. □ ∀hasAuthor. Journalist
- Roles corresponding to binary relations
 - ex: hasAuthor, hasChild
 - can be combined with operators for constructing complex roles
 - $hasChildren \equiv hasSon \sqcup hasDaughter$
- Individuals (used in assertions only)
 - ex: Mary, John

T-Boxes and A-Boxes

```
    Terminologies (T-Boxes): sets of

     • concepts definitions (C_1 \equiv C_2)
        ex: Father = Man \sqcap \exists hasChild.Person
     • or concept generalizations (C_1 \sqsubseteq C_2)
        ex: Woman 

□ Person
Assertions (A-Boxes): assert
     • individuals as concept members i : C,
        where i is an individual and C is a concept
        ex: marv : Person, john : Father
     • individual pairs as relation members \langle i, j \rangle : R,
        where i.i are individuals and R is a relation
        ex: (john, mary): hasChild
```

T-Box: Example (Logic ALCN)

```
Woman ≡ Person □ Female
                           Person □ ¬ Woman
                   Man
                            Woman □ ∃hasChild Person
                Mother
                            Man □ ∃hasChild.Person
                 Father
                 Parent
                            Father | | Mother
           Grandmother =
                            Mother □ ∃hasChild. Parent
MotherWithManyChildren
                             Mother \square \geqslant 3 has Child Person
                        MotherWithoutDaughter
                             Mother □ ∀hasChild.¬ Woman
                   Wife
                         ■ Woman □ ∃hasHushand Man
```

(Courtesy of Maria Simi, UniPI)

Reasoning Services for DLs

- Design and management of ontologies
 - consistency checking of concepts, creation of hierarchies
- Ontology integration
 - Relations between concepts of different ontologies
 - Consistency of integrated hierarchies
- Queries
 - Determine whether facts are consistent wrt ontologies
 - Determine if individuals are instances of concepts
 - Retrieve individuals satisfying a query (concept)
 - Verify if a concept is more general than another (subsumption)

Querying a DL Ontology: Example

All the children of John are females. Mary is a child of John. Tim is a friend of professor Blake. Prove that Mary is a female.

- A ^{def} = {john : ∀hasChild.female, (john, mary) : hasChild, (blake, tim) : hasFriend, blake : professor}
- Query: mary: female (or: is $A \sqcap mary$: $\neg female$ unsatisfiable?)
- Yes

Given:

- a set of basic concepts: {Person, Male, Doctor, Engineer}
- a set of relations: {hasChild}

with their obvious meaning. Write a \mathcal{T} -box in \mathcal{ALCN} defining the following concepts

- (a) Female, Man, Woman (with their standard meaning)
- (b) femaleDoctorWithoutChildren: female doctor with no children
- (c) fatherOfFemaleDoctor: father of at least two female doctors
- (d) motherOfDoctorsOrEngineers: woman whose children are all engineers or ^a doctors

anon-exclusive or.