# Fundamentals of Artificial Intelligence Chapter 12: Knowledge Representation

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## Outline



- 2 Categories and Objects
- Reasoning about Knowledge
- Reasoning about Categories
  - Semantic Networks (hints)
  - Description Logics

# Outline

### Ontologies and Ontological Engineering

- Categories and Objects
- B Reasoning about Knowledge
- Reasoning about Categories
   Semantic Networks (hints)
  - Description Logics

### Generalities

#### Q: What content do we put into an agent's KB?

- how do we organize such content?
- how do we represent facts about the world?
- A whole AI field: Knowledge Representation, KR
  - often combined with Automated Reasoning on KB
  - $\implies$  Knowledge Representation & Reasoning, KRR
- KR: use logics (e.g. FOL) to represent the most important aspects of the real world, such as: action, space, time, knowledge, belief
- Topics:
  - ontologies and ontological engineering
  - objects and categories, composite objects, measurements, ...
  - actions and change, events, temporal intervals, ...
  - reasoning about knowledge & beliefs
  - reasoning about categories
  - default reasoning
  - ...

# Knowledge Engineering and Ontological Engineering

### Knowledge Engineering

- The activity to formalize a specific problem or task domain
- Relevant questions to be addressed:
  - What are the relevant facts, objects, relations ... ?
  - Which is the right level of abstraction?
  - What are the queries to the KB (inferences)?

#### **Ontological Engineering**

- The activity to build general-purpose ontologies
  - should be applicable in any special-purpose domain (with the addition of domain-specific axioms)
  - In non trivial domains, reasoning and problem solving could involve several areas of knowledge simultaneously
    - $\implies$  different areas of knowledge must be combined
- Several attempts to build general-purpose ontologies
  - CYC, DBpedia, TextRunner, ...
  - not very successful so far

# Outline

Ontologies and Ontological Engineering

### 2 Categories and Objects

B Reasoning about Knowledge

Reasoning about Categories
 Semantic Networks (hints)

Description Logics

# Categories and Objects

Categories, Objects, Members and Subclasses

- KR requires the organisation of objects into categories
  - interaction at the level of the object
  - reasoning at the level of categories
  - ex: typically we want to buy a basketball, rather than a particular basketball instance
- Categories play a role in predictions about objects
  - · agent infers the presence of certain objects from perceptual input
  - infers category from the perceived properties of the objects,
  - uses category information to make predictions about the objects
- Categories can be represented in two ways by FOL
  - predicates (ex Basketball(x)): relations
  - reification of categories into objects (ex Basketballs): sets
     allows categories to be argument of predicates/functions
- Membership of a category as set membership
  - ex: Member(b, Basketballs) (abbr.  $b \in Basketballs$ )
- Subcategories (aka subclasses) are (strict) subsets
  - ex: Subset(Basketballs, Balls) (abbr.  $\textit{Basketballs} \subset \textit{Balls}$ )

# Categories and Objects [cont.]

Inheritance and Taxonomies

- A subcategory inherits the properties of the category
  - ex:

if  $\forall x.(x \in Food \rightarrow Edible(x))$ ,  $Fruit \subset Food$ ,  $Apples \subset Fruit$ then  $\forall x.(x \in Apple \rightarrow Edible(x))$ 

- A member inherits the properties of the category
  - if  $a \in Apples$ , then Edible(a)
- Subclass relation organize categories into taxonomies (aka taxonomic hierarchies)
  - ex: taxonomy of >10M living&extinct species
  - ex: Dewey Decimal System: taxonomy of all fields of knowledge

# Categories and Objects [cont.]

#### FOL Reasoning about Categories

- FOL allows to state facts about categories:
  - an object is a member of a category BB<sub>9</sub> ∈ Basketballs
  - a category is a subclass of another category *Basketballs* ⊂ *Balls*
  - all members of a category have some properties  $\forall x.(x \in Basketballs \rightarrow Spherical(x))$
  - members of a category can be recognized by some properties ∀x.((Orange(x) ∧ Round(x) ∧ Diameter(x) = 9.5" ∧ x ∈ Balls) → x ∈ Basketballs)
  - category as a whole has some properties Dogs ∈ DomesticatedSpecies
- New categories can be defined by providing necessary and sufficient conditions for membership
  - $\forall x.(x \in Bachelors \leftrightarrow (Unmarried(x) \land x \in Adults \land x \in Males))$

# Categories and Objects [cont.]

#### **Derived relations**

- Two or more categories in a set s are disjoint iff they have no members in common
  - $Disjoint(s) \leftrightarrow (\forall c_1 c_2, ((c_1 \in s \land c_2 \in s \land c_1 \neq c_2)))$

 $\rightarrow$  *Intersection*( $c_1, c_2$ ) =  $\emptyset$ )

• ex:

Disjoint({Animals, Vegetables}), Disjoint({Insects, Birds, Mammals, Reptiles}),

- A set of categories s is an exhaustive decomposition of a category c iff all members of c are covered by categories in s
  - ExaustiveDecomposition(s, c)  $\leftrightarrow \forall i.(i \in c \leftrightarrow (\exists c_2.(c_2 \in s \land i \in c_2)))$
  - ex: E.D.({Americans, Canadians, Mexicans}, NorthAmericans)
- A disjoint exhaustive decomposition is a partition
  - $Partition(s, c) \leftrightarrow (Disjoint(s) \land ExhaustiveDecomposition(s, c))$
  - ex: Partition({NorthernItalians, CentralItalians, SouthernItalians, InsularItalians}, Italians)

# **Digression: Natural Kinds**

- Many categories have no clear-cut definition (ex: chair, bush, ...)
  - Ex: tomatoes are sometimes green, red, yellow, black; they are mostly round
- One useful solution: category "Typical(.)", s.t. Typical(c)  $\subseteq c$ 
  - $\implies$  most knowledge about natural kinds will actually be about their typical instances
    - ex:  $\forall x.(x \in Typical(Tomatoes) \rightarrow (Red(x) \land Round(x)))$
- → We can write down useful facts about categories without providing exact definitions

#### Note

Quine (1953) challenged the utility of the notion of strict definition.

- Ex: "bachelor": is the Pope a bachelor?
  - $\implies$  technically yes, but misleading

# **Physical Composition**

- PartOf(.,.) relation: One object may be part of another
  - PartOf(Bucharest, Romania)
  - PartOf(Romania, EasternEurope)
  - PartOf(EasternEurope, Europe)
- *PartOf*(.,.) is reflexive and transitive:
  - $\forall x. PartOf(x, x)$
  - $\forall x, y, z.((PartOf(x, y) \land PartOf(y, z)) \rightarrow PartOf(x, z))$
  - ⇒ PartOf(Bucharest, Europe)
- Categories of composite objects are often characterized by structural relations among parts. Ex: Biped

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• Other concepts & relations: PartPartition, BunchOf...

### Measurements

#### **Quantitative Measurements**

- Objects may have "quantitative" properties
  - e.g. height, mass, cost, ...
- Values that we assign to these properties are measures
- Can be represented by unit functions
  - ex  $Length(L_1) = Inches(1.5) \land Inches(1.5) = Centimeters(3.81)$
- Conversion between units:
  - $\forall i. \ Centimeters(2.54 \times i) = Inches(i)$
- Measures can be used to describe objects:
  - ex: Diameter(Basketball<sub>12</sub>) = Inches(9.5)
  - ex: *ListPrice*(*Basketball*<sub>12</sub>) = \$(19)
  - ex:  $\forall d.(d \in Days \rightarrow Duration(d) = Hours(24))$

# Measurements [cont.]

#### **Qualitative Measurements**

- Some measures have no scale
  - ex: beauty, deliciousness, difficulty,...
- Most important aspect of measures: they are orderable
  - Ex: Deliciousness(SacherTorte) > Deliciousness(BrussellSprout)
  - Ex: Beauty(PaulNewmann) > Beauty(MartyFeldman)
  - Ex: Difficulty(Prove\_P \ne NP) > Difficulty(SolvePuzzle)
- Allow for reasoning by exploiting transitivity of monotonicity: ∀e<sub>1</sub>e<sub>2</sub>.((e<sub>1</sub> ∈ Exercises ∧ e<sub>2</sub> ∈ Exercises ∧ Wrote(Norvig, e<sub>1</sub>) ∧ Wrote(Russell, e<sub>2</sub>)) → Difficulty(e<sub>1</sub>) > Difficulty(e<sub>2</sub>))
   ∀e<sub>1</sub>e<sub>2</sub>.((e<sub>1</sub> ∈ Exercises ∧ e<sub>2</sub> ∈ Exercises ∧ Difficulty(e<sub>1</sub>) > Difficulty(e<sub>2</sub>)) → ExpectedScore(e<sub>1</sub>) < ExpectedScore(e<sub>2</sub>))
   ∀e<sub>1</sub>e<sub>2</sub>.(ExpectedScore(e<sub>1</sub>) < ExpectedScore(e<sub>2</sub>) → Pick(e<sub>1</sub>, e<sub>2</sub>) = e<sub>2</sub>
   Then: (Wrote(Norvig, E<sub>1</sub>) ∧ Wrote(Russell, E<sub>2</sub>)) ⊨ Pick(E<sub>1</sub>, E<sub>2</sub>) = E<sub>2</sub>
- Qualitative physics: a subfield of AI that investigates how to reason about physical systems without numerical computations

# **Objects vs Stuff**

- There are countable objects
  - e,g, apples, holes, theorems, ...
- ... and mass objects, aka stuff or substances
  - e.g. butter, water, energy, ...
- ⇒ Intuitive meaning "an amount/quantity of..."
  - ex: b ∈ butter: "b is an amount/quantity of butter"
  - Any part of stuff is still stuff:
    - ex:  $\forall b, p.((b \in Butter \land PartOf(p, b)) \rightarrow p \in Butter)$
  - Can define sub-categories, which are stuff
    - ex: UnsaltedButter ⊂ Butter
  - Stuff has a number of intrinsic properties, shared by its subparts
    - e.g., color, fat content, density ...
    - ex:  $\forall b.(b \in Butter \rightarrow MeltingPoint(b, Centigrade(30)))$
  - Stuff has no extrinsic properties
    - e.g., weight, length, shape, ...

## Outline

Ontologies and Ontological Engineering

#### Categories and Objects



#### Reasoning about Knowledge

- Reasoning about Categories
   Semantic Networks (hints)
   Reasticities Leavies
  - Description Logics

- Intelligence is intrinsically social: agents need to negotiate and coordinate with other agents
- In multi-agents scenarios, to predict what other agents will do, we need methods to model mental states of other agents
  - representations of other agents' knowledge (and beliefs, goals)
- Agent's Propositional attitudes: Knows, Believes, Wants,...
  - ex "Lois Knows that Superman can fly"

#### Problem

Propositional attitudes do not behave as regular predicates

issue: Referential opacity vs. referential transparency

# Referential opacity vs. Referential transparency

- Consider the assertion "Lois knows that Superman can fly"
- Consider the FOL formalization: Knows(Lois, CanFly(Superman))
- Minor Problem: CanFly(Superman) is a formula
  - $\implies$  cannot occur as argument of a predicate
  - $\implies$  must apply reification  $\implies$  make it a term
- Major Problem (Referential Transparency of FOL):
  - since Superman is Clark Kent (but Lois doesn't know it!), FOL allows to conclude "Lois knows that Clark Kent can fly":

Superman = Clark  $\land$  Knows(Lois, CanFly(Superman))

 $\models_{FOL} Knows(Lois, CanFly(Clark))$ 

- → Wrong inference! (Lois doesn't know Clark Kent can fly!)
- Hint: FOL predicates transparent to equality reasoning:

 $t = s \land P(s, ...) \models_{FOL} P(t, ...)$ 

 Need a logic which is opaque to equality reasoning (aka Referential Opacity): Modal Logics

# **Modal Logics**

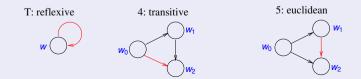
- Modal logics include special modal operators that take formulas (not terms!) as arguments
  - "A knows P" is represented with KAP (P formula, not term!)
  - ex: "Lois knows that Superman can fly": *K*<sub>Lois</sub>CanFly(Superman)
  - ex: "Lois knows Clark Kent knows if he is Superman or not":  $K_{Lois}(K_{Clark} | dentity(Superman, Clark) \lor K_{Clark} \neg Identity(Superman, Clark))$
- Properties in all modal logics:
  - $K_A(P \land Q) \iff K_AP \land K_AQ$
  - $K_A P \lor K_A Q \models K_A (P \lor Q)$ , but  $K_A (P \lor Q) \not\models K_A P \lor K_A Q$  (e.g.  $K_A (P \lor \neg P) \not\models K_A P \lor K_A \neg P$ )
- The following axiom holds in all (normal) modal logics:  $K : (K_A \phi \land K_A (\phi \rightarrow \psi) \rightarrow K_A \psi$  (distribution axiom): "A is able to perform propositional inference"
- The following axioms hold in some (normal) modal logics:
  - $T: K_A \varphi \rightarrow \varphi$  (knowledge axiom): "A knows only true facts"
  - 4 :  $K_A \varphi \rightarrow K_A K_A \varphi$  (positive-introspection axiom): "If A knows fact  $\varphi$ , then [s]he knows [s]he knows it"
  - 5 :  $\neg K_A \varphi \rightarrow K_A \neg K_A \varphi$  (negative-introspection axiom):

"If A doesn't know  $\varphi$ , then [s]he knows [s]he doesn't know it"

- Referential Opacity: Superman = Clark  $\land$  K<sub>Lois</sub>CanFly(Superman)  $\nvDash$  K<sub>Lois</sub>CanFly(Clark)
- Reasoning in (propositional) Modal logics is NP-hard (most often even PSPACE-hard)

# Semantics of Modal Logics

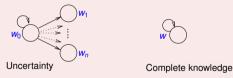
- A model (Kripke model) is a collection of possible world states w<sub>i</sub> (aka worlds, states)
  - possible states are connected in a graph by accessibility relations
  - one relation for each distinct modal operator KA
- $w_1$  is accessible from  $w_0$  wrt.  $K_A$  if everything which holds in  $w_1$  is consistent with what A knows in  $w_0$  (written " $Acc(K_A, w_0, w_1)$ " or " $w_0 \stackrel{K_A}{\longmapsto} w_1$ ")
  - $\implies$   $\mathcal{K}_{A}\varphi$  holds in  $w_o$  iff  $\varphi$  holds in every state  $w_i$  accessible from  $w_0$ 
    - the more is known in  $w_0$ , the less states are accessible from  $w_0$
    - remark: two possible states may differ also for what an agent knows there
- Different modal logics differ by different properties of Acc(K<sub>A</sub>,...)
  - $T: K_A \varphi \to \varphi$  holds iff  $Acc(K_A, ...)$  reflexive:  $w \stackrel{K_A}{\longmapsto} w$
  - 4 :  $K_A \varphi \to K_A K_A \varphi$  holds iff  $Acc(K_A, ...)$  transitive:  $w_0 \stackrel{K_A}{\longmapsto} w_1$  and  $w_1 \stackrel{K_A}{\longmapsto} w_2 \Longrightarrow w_0 \stackrel{K_A}{\longmapsto} w_2$
  - 5:  $\neg K_A \varphi \rightarrow K_A \neg K_A \varphi$  holds iff  $Acc(K_A, ...)$  euclidean:  $w_0 \stackrel{K_A}{\longmapsto} w_1$  and  $w_0 \stackrel{K_A}{\longmapsto} w_2 \Longrightarrow w_1 \stackrel{K_A}{\longmapsto} w_2$



# Semantics of Modal Logics: Some Remarks

Assume the knowledge of A is correct:  $T : K_A \varphi \rightarrow \varphi$  ("Everything which A knows holds")

- $\not\models \varphi \to K_A \varphi$ : *A* does not know everything which holds!
- The less states are accessible, the more precise is the knowledge of A
  - uncertainty on some information makes accessible states different
    - $\implies$  A does not know the state [s]he is
  - complete knowledge: current state is the only successor of itself
    - $\implies$  A knows exactly the state [s]he is



Notice the difference:

- $K_A \neg P$ : agent A knows that P does not hold (in all accessible states P is false)
- $\neg K_A P$ : agent A does not know if P holds (in some accessible states P is false)

$$\implies K_A \neg P \models \neg K_A P, \text{ but } \neg K_A P \not\models K_A \neg P$$

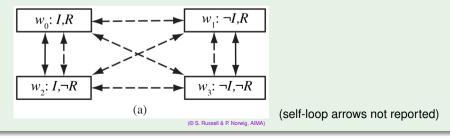
Accessibility relations:  $K_{Superman}$  (solid arrows) and  $K_{Lois}$  (dotted arrows).

Legenda:

- R: "the weather report says tomorrow will rain"
- I: "Superman's secret identity is Clark Kent."
- Ex: K<sub>Lois</sub>(K<sub>Clark</sub> I ∨ K<sub>Clark</sub> ¬ I): "Lois Knows that Clark Knows if he is Superman or not."

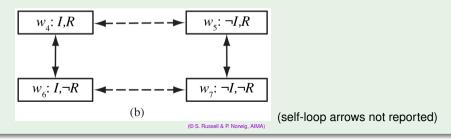
Superman knows his own identity: K<sub>Superman</sub>I ∨ K<sub>Superman</sub>¬I, and

 (a) neither Superman nor Lois has seen the weather report, she knows Superman knows if he is Clark (¬K<sub>Lois</sub>R ∧ ¬K<sub>Lois</sub>¬R) ∧ (¬K<sub>Superman</sub>R ∧ ¬K<sub>Superman</sub>¬R) ∧ K<sub>Lois</sub>(K<sub>Superman</sub>¬I)



Accessibility relations:  $K_{Superman}$  (solid arrows) and  $K_{Lois}$  (dotted arrows).

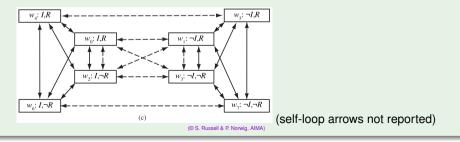
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  - Ex: K<sub>Lois</sub>(K<sub>Clark</sub> I ∨ K<sub>Clark</sub>¬I): "Lois Knows that Clark Knows if he is Superman or not."
- Superman knows his own identity:  $K_{Superman}I \lor K_{Superman}\neg I$ , and (b) Lois has seen the weather report, Superman has not, but he knows that Lois has seen it  $(K_{Lois}R \lor K_{Lois}\neg R) \land (\neg K_{Superman}R \land \neg K_{Superman}\neg R)$  $K_{Lois}(K_{Superman}I \lor K_{Superman}\neg I) \land K_{Superman}(K_{Lois}R \lor K_{Lois}\neg R)$



Accessibility relations:  $K_{Superman}$  (solid arrows) and  $K_{Lois}$  (dotted arrows).

- Legenda:
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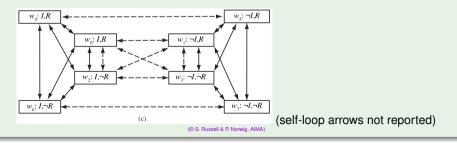
Superman knows his own identity: K<sub>Superman</sub>I ∨ K<sub>Superman</sub>¬I, and
 (c) Lois may or may not have seen the weather report, Superman has not:
 ((¬K<sub>Lois</sub>R ∧ ¬K<sub>Lois</sub>¬R) ∨ (K<sub>Lois</sub>R ∨ K<sub>Lois</sub>¬R)) ∧ (¬K<sub>Sup</sub>. R ∧ ¬K<sub>Sup</sub>. ¬R)
 K<sub>Lois</sub>(K<sub>Superman</sub>I ∨ K<sub>Superman</sub>¬I)



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Superman knows his own identity: K<sub>Superman</sub>I ∨ K<sub>Superman</sub>¬I, and
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 K<sub>Lois</sub>(K<sub>Superman</sub>I ∨ K<sub>Superman</sub>¬I)



Consider the previous example.

• For each scenario (a), (b) and (c) define doubly-nested knowledge in terms of

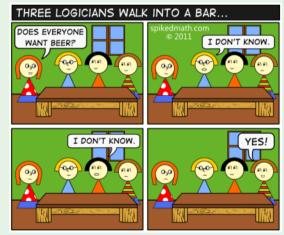
```
 \begin{array}{l} [\neg] K_{Lois} [\neg] K_{Lois} [\neg] I, \\ [\neg] K_{Lois} [\neg] K_{Lois} [\neg] R, \\ [\neg] K_{Sup.} [\neg] K_{Sup.} [\neg] I, \\ [\neg] K_{Sup.} [\neg] K_{Sup.} [\neg] R \end{array}
```

Consider (normal) modal logics (i.e., axioms K, T, 4 and 5 hold). Let IsRed(Pen), IsOnTable(Pen) be possible facts, let *Mary*, *John* be agents and let  $K_{Mary}$ ,  $K_{John}$  denote the modal operators "Mary knows that..." and "John knows that..." respectively. For each of the following facts, say if it is true or false.

- If  $K_{Mary} \neg IsRed(Pen)$  holds, then  $\neg K_{Mary}IsRed(Pen)$  holds
- If  $\neg K_{Mary}$  IsRed(Pen) holds, then  $K_{Mary} \neg$  IsRed(Pen) holds
- If  $K_{John}$  IsRed(Pen) and IsRed(Pen)  $\leftrightarrow$  IsOnTable(Pen) hold, then  $K_{John}$  IsOnTable(Pen) holds
- If  $K_{Mary}$ IsRed(Pen) and  $K_{Mary}$ (IsRed(Pen)  $\rightarrow K_{John}$ IsRed(Pen)) hold, then  $K_{Mary}K_{John}$ IsRed(Pen)) holds

### Exercise

- Why does the third logician answers "Yes"?
- Formalize and solve the problem by means of modal logic (K+T+4+5)



(Courtesy of Maria Simi, UniPI)

## Outline

Ontologies and Ontological Engineering

- Categories and Objects
- B Reasoning about Knowledge



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- Beasoning about Knowledge



# Reasoning Systems for Categories

### Q. How to organize and reason with categories?

- Semantic Networks
  - allow to visualize knowledge bases
  - efficient algorithms for category membership inference
  - limited expressivity
  - many variants

### Description Logics (DLs)

- formal language for constructing and combining category definitions
- (relatively) efficient algorithms to decide subset and superset relationships between categories
- many DLs
  - up to very high expressivity
  - up to very high complexity (e.g., DOUBLY-EXPTIME)

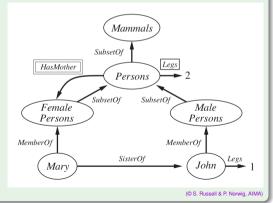
# Semantic Networks

- Allow for representing individual objects, categories of objects, and relations among objects
- A Semantic Network is a graph where:
  - nodes, with a label, correspond to concepts
  - arcs, labelled and directed, correspond to binary relations between concepts (aka roles)
- Two kinds of nodes:
  - Generic concepts, corresponding to categories/classes
  - Individual concepts, corresponding to individuals
- Two special relations are always present, with different names
  - IS-A, aka SubsetOf/SubclassOf (subclass)
  - InstanceOf aka MemberOf (membership)
- Inheritance detection straightforward
- Ability to represent default values for categories
- Limited expressive power: cannot represent negation, disjunction, nested function symbols, existential quantification

# Semantic Networks: Example

- Notice
  - "HasMother" is a relation between persons (individuals) (categories do not have mothers)
  - "HasMother" (double-boxed notation) means  $\forall x.(x \in Persons \rightarrow [\forall y.(HasMother(x, y) \rightarrow y \in FemalePersons)])$
  - "Legs" is a property of single persons (individuals)
  - "Legs" (single-boxed notation) means:

 $\forall x.(x \in Persons \rightarrow Legs(x, 2))$ 



# Inheritance in Semantic Networks

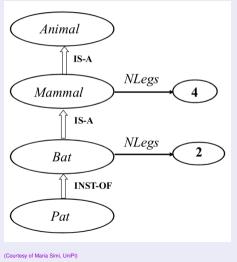
- Inheritance conveniently implemented as link traversal
- Q. How many legs has Clyde?
- ⇒ follow the INST-OF/IS-A chain until find the property NLegs

Animal	
IS-A Mammal NLegs 4	
Elephant Color grey	
INST-OF Clyde	
(Courtesy of Maria Simi, UniPI)	

## Inheritance with Exceptions

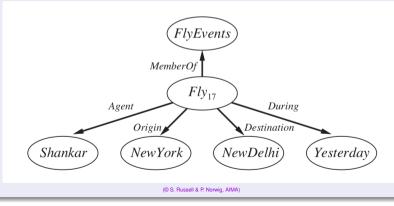
The presence of exceptions does not create any problem with S.N.

- How many legs has Pat?
- Just take the most specific information: the first that is found going up the hierarchy
- ⇒ ability to represent default values for categories



# **Encoding N-Ary Relations**

- Semantic networks allow only binary relations
- Q. How to represent n-ary relations?
- $\implies$  Reify the proposition as an event belonging to an appropriate event category
  - ex "Fly<sub>17</sub>" for Fly(Shankar, NewYork, NewDelhi, Yesterday)



# Outline

Ontologies and Ontological Engineering

- Categories and Objects
- B Reasoning about Knowledge



Description Logics

- Designed to describe definitions and properties about categories
- Principal inference tasks:
  - Subsumption: check if one category is a subset (sub-category) of another
  - Classification: check whether an object belongs to a category
  - Consistency: check if category membership criteria are satisfiable
- Defaults and exceptions are lost

# Concepts, Roles, Individuals

- Concepts, corresponding to unary relations
  - $\top, \bot$ : universal and empty concepts
  - atomic concepts: ex: Female, Male, Article, Journalist,...
  - operators for the construction of complex concepts: and (□), or (□), not (¬), all (∀), some (∃), atleast (≥ n), atmost (≤ n), ...
  - ex: mothers (i.e., women who have children) of at least three female children: Woman □ ∃hasChildren.Person □ ≥ 3 hasChild.Female
  - ex: articles that have authors and whose authors are all journalists: *Article* □ ∃*hasAuthor*. ⊤ □ ∀*hasAuthor*. *Journalist*
- Roles corresponding to binary relations
  - ex: hasAuthor, hasChild
  - can be combined with operators for constructing complex roles
  - $hasChildren \equiv hasSon \sqcup hasDaughter$
- Individuals (used in assertions only)
  - ex: Mary, John

### **T-Boxes and A-Boxes**

- Terminologies (T-Boxes): sets of
  - concepts definitions (C<sub>1</sub> ≡ C<sub>2</sub>)
     ex: Father ≡ Man ⊓ ∃hasChild.Person
  - or concept generalizations ( $C_1 \sqsubseteq C_2$ ) ex: Woman  $\sqsubseteq$  Person
- Assertions (A-Boxes): assert
  - individuals as concept members *i* : *C*, where i is an individual and C is a concept ex: *mary* : *Person*, *john* : *Father*
  - individual pairs as relation members (*i*, *j*) : *R*, where i,j are individuals and R is a relation ex: (*john, mary*) : *hasChild*

# T-Box: Example (Logic $\mathcal{ALCN}$ )

Woman ≡ Person □ Fema	e
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- $\mathsf{Man} \equiv \mathsf{Person} \sqcap \neg \mathsf{Woman}$
- Mother  $\equiv$  Woman  $\sqcap \exists hasChild.Person$ 
  - Father  $\equiv$  Man  $\sqcap \exists$ hasChild.Person
  - Parent  $\equiv$  Father  $\sqcup$  Mother
- Grandmother  $\equiv$  Mother  $\sqcap \exists hasChild.$  Parent
- MotherWithManyChildren
  - MotherWithoutDaughter
- $\equiv$  Mother  $\square \ge 3$  hasChild .Person
- Mother □ ∀hasChild.¬ Woman

(Courtesy of Maria Simi, UniPI)

Wife

# **Reasoning Services for DLs**

- Design and management of ontologies
  - consistency checking of concepts, creation of hierarchies
- Ontology integration
  - Relations between concepts of different ontologies
  - Consistency of integrated hierarchies
- Queries
  - Determine whether facts are consistent wrt ontologies
  - Determine if individuals are instances of concepts
  - Retrieve individuals satisfying a query (concept)
  - Verify if a concept is more general than another (subsumption)

All the children of John are females. Mary is a child of John. Tim is a friend of professor Blake. Prove that Mary is a female.

- *A* <sup>def</sup> { john : ∀hasChild.female, (john, mary) : hasChild, (blake, tim) : hasFriend, blake : professor
- Query: mary : female (or: is  $A \sqcap mary : \neg$  female unsatisfiable?)
- Yes

#### Given:

- a set of basic concepts: {Person, Male, Doctor, Engineer}
- a set of relations: {hasChild}

with their obvious meaning. Write a  $\mathcal{T}\text{-box}$  in  $\mathcal{ALCN}$  defining the following concepts

- (a) Female, Man, Woman (with their standard meaning)
- (b) femaleDoctorWithoutChildren: female doctor with no children
- (c) fatherOfFemaleDoctor: father of at least two female doctors
- (d) motherOfDoctorsOrEngineers: woman whose children are all engineers or <sup>a</sup> doctors

<sup>a</sup>non-exclusive or.