Fundamentals of Artificial Intelligence Chapter 10: Classical Planning

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Basics on Planning

- The Problem
- The PDDL Language
- Search Strategies and Heuristics
 - Forward and Backward Search
 - Heuristics



- Planning Graphs, Heuristics and Graphplan
- Planning Graphs
- Heuristics Driven by Planning Graphs
- The Graphplan Algorithm
- Other Approaches (hints)
 - Planning as SAT Solving
 - Planning as FOL Inference



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Automated Planning

Synthesize a sequence of actions (plan) to be performed by an agent leading from an initial state of the world to a set of target states (goal)

- Planning is both:
 - an application per se
 - a common activity in many applications (e.g. design & manufacturing, scheduling, robotics,...
- Similar to problem-solving agents (Ch.03), with factored/structured representation of states
- "Classical" Planning (this chapter): fully observable, deterministic, static environments with single agents

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Automated Planning [cont.]

Automated Planning

• Given:

- an initial state
- a set of actions you can perform
- a (set of) state(s) to achieve (goal)

• Find:

• a plan: a partially- or totally-ordered set of actions needed to achieve the goal from the initial state

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Decidability and Complexity

• PlanSAT: the question of whether there exists any plan that solves a planning problem

- decidable for classical planning
- with function symbols, the number of states becomes infinite
 - \implies undecidable
- in PSPACE
 - harder than NP, no polynomial-size witness (e.g., Tower of Hanoi)

• Bounded PlanSAT: the question of whether there exists any plan of a given length k or less

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Planning Domain Definition Language (PDDL)

- A state is a conjunction of fluents: ground, function-less atoms
 - ex: Poor \land Unknown, At(Truck₁, Melbourne) \land At(Truck₂, Sydney)
 - ex of non-fluents: At(x, y) (non ground), ¬Poor (negated), At(Father(Fred), Sydney) (not function-less)
 - closed-world assumption: all non-mentioned fluents are false
 - unique names assumption: distinct names refer to distinct objects
- Actions are described by a set of action schemata
 - concise description: describe which fluent change
 - $\Rightarrow~$ the other fluents implicitly maintain their values

• Action Schema: consists in action name, a list of variables in the schema, the precondition, the effect (aka postcondition)

- precondition and effect are conjunctions of literals (positive or negated atomic sentences)
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• Action schema:

 $\begin{array}{l} \textit{Action}(\textit{Fly}(p,\textit{from},\textit{to}), \\ \textit{PRECOND}:\textit{Plane}(p) \land \textit{Airport}(\textit{from}) \land \textit{Airport}(\textit{to}) \land \textit{At}(p,\textit{from}) \\ \textit{EFFECT} : \neg \textit{At}(p,\textit{from}) \land \textit{At}(p,\textit{to})) \end{array}$

 Action instantiation: Action(Fly(P₁, SFO, JFK), PRECOND : At(P₁, SFO) ∧ Plane(P₁) ∧ Airport(SFO) ∧ Airport(JFK EFFECT : ¬At(P₁, SFO) ∧ At(P₁, JFK))
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• Precondition: must hold to ensure the action can be executed

- defines the states in which the action can be executed
- action is applicable in state s if the preconditions are satisfied by s
- Effect: represent the effects of the action on the world
 - defines the result of executing the action
- Add list (ADD(a)): (the fluents in) the positive literals in the action's effects
 - ex: {*At*(*p*, *to*)}
- Delete list (DEL(a)): (the fluents in) the negative literals in the action's effects
 - ex: {*At*(*p*, *from*)}
- Result of action a in state s: RESULT(s,a) $\stackrel{\text{def}}{=}$ (s\DEL(a) \cup ADD(a))
 - start from s
 - remove the fluents that appear as negative literals in effect
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 - ex: $Fly(P_1, SFO, JFK) \Longrightarrow$ remove $At(P_1, SFO)$, add $At(P_1, JFK)$

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- Result of action a in state s: $\text{RESULT}(s,a) \stackrel{\text{def}}{=} (s \setminus \text{DEL}(a) \cup \text{ADD}(a))$
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• $s : At(P_1, SFO) \land Plane(P_1) \land Airport(SFO) \land Airport(JFK) \land ...$

 $\Rightarrow s' : At(P_1, JFK) \land Plane(P_1) \land Airport(SFO) \land Airport(JFK) \land ...$

Sometimes we want to <mark>propositionalize</mark> a PDDL problem: replace each action schema with a set of ground actions.

• Ex: ...At_P₁_SFO \land Plane_P₁ \land Airport_SFO \land Airport_JFK)...

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Time in PDDL

- Fluents do not explicitly refer to time
- Times and states are implicit in the action schemata:
 - the precondition always refers to time t
 - the effect to time t+1.

- A set of action schemata defines a planning domain
- PDDL problem: a planning domain, an initial state and a goal
 - the initial state is a conjunction of ground atoms (positive literals)
 - closed-world assumption: any not-mentioned atoms are false
 - the goal is a conjunction of literals (positive or negative)
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- Ex: goal: At(p, SFO) ∧ Plane(p):
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 - a goal g may represent a set of states (the set of states entailing g)
- Ex: goal: *At*(*p*, *SFO*) ∧ *Plane*(*p*):
 - variable "p" implicitly means "for some plane p"
 - the state $Plane(Plane_1) \land At(Plane_1, SFO) \land ...$ entails g

Time in PDDL

- Fluents do not explicitly refer to time
- Times and states are implicit in the action schemata:
 - the precondition always refers to time t
 - the effect to time t+1.

PDDL Problem

- A set of action schemata defines a planning domain
- PDDL problem: a planning domain, an initial state and a goal
 - the initial state is a conjunction of ground atoms (positive literals)
 - closed-world assumption: any not-mentioned atoms are false
 - the goal is a conjunction of literals (positive or negative)
 - may contain variables, which are implicitly existentially quantified
 - a goal g may represent a set of states (the set of states entailing g)
- Ex: goal: At(p, SFO) \land Plane(p):
 - variable "p" implicitly means "for some plane p"
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Planning as a search problem

All components of a search problem

- an initial state
- an ACTIONS function
- a RESULT function
- and a goal test

Example: Air Cargo Transport

 $Init(At(C_1, SFO) \land At(C_2, JFK) \land At(P_1, SFO) \land At(P_2, JFK))$ $\wedge Cargo(C_1) \wedge Cargo(C_2) \wedge Plane(P_1) \wedge Plane(P_2)$ $\wedge Airport(JFK) \wedge Airport(SFO))$ $Goal(At(C_1, JFK) \land At(C_2, SFO))$ Action(Load(c, p, a)).**PRECOND:** $At(c, a) \land At(p, a) \land Cargo(c) \land Plane(p) \land Airport(a)$ EFFECT: $\neg At(c, a) \land In(c, p)$) Action(Unload(c, p, a)).**PRECOND:** $In(c, p) \land At(p, a) \land Cargo(c) \land Plane(p) \land Airport(a)$ EFFECT: $At(c, a) \land \neg In(c, p)$) Action(Flu(p, from, to)). **PRECOND:** $At(p, from) \land Plane(p) \land Airport(from) \land Airport(to)$ EFFECT: $\neg At(p, from) \land At(p, to))$

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One solution: [*Load*(*C*₁, *P*₁, *SFO*), *Fly*(*P*₁, *SFO*, *JFK*), *Unload*(*C*₁, *P*₁, *JFK*), *Load*(*C*₂, *P*₂, *JFK*), *Fly*(*P*₂, *JFK*, *SFO*), *Unload*(*C*₂, *P*₂, *SFO*)]

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```
One solution: [Load(C<sub>1</sub>, P<sub>1</sub>, SFO), Fly(P<sub>1</sub>, SFO, JFK), Unload(C<sub>1</sub>, P<sub>1</sub>, JFK), Load(C<sub>2</sub>, P<sub>2</sub>, JFK), Fly(P<sub>2</sub>, JFK, SFO), Unload(C<sub>2</sub>, P<sub>2</sub>, SFO)]
```

Example: Spare Tire Problem

```
Init(Tire(Flat) \land Tire(Spare) \land At(Flat, Axle) \land At(Spare, Trunk))
Goal(At(Spare, Axle))
Action(Remove(obj, loc),
  PRECOND: At(obj, loc)
  EFFECT: \neg At(obj, loc) \land At(obj, Ground))
Action(PutOn(t, Axle)),
   PRECOND: Tire(t) \land At(t, Ground) \land \neg At(Flat, Axle)
   EFFECT: \neg At(t, Ground) \land At(t, Axle))
Action(LeaveOvernight,
   PRECOND:
   EFFECT: \neg At(Spare, Ground) \land \neg At(Spare, Axle) \land \neg At(Spare, Trunk)
            \wedge \neg At(Flat, Ground) \land \neg At(Flat, Axle) \land \neg At(Flat, Trunk))
```

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(We assume that the car is parked in a particularly bad neighborhood, so that the effect of leaving it overnight is that the tires disappear.)

One solution: [*Remove*(*Flat*, *Axle*), *Remove*(*Spare*, *Trunk*), *PutOn*(*Spare*, *Axle*)]

Example: Spare Tire Problem

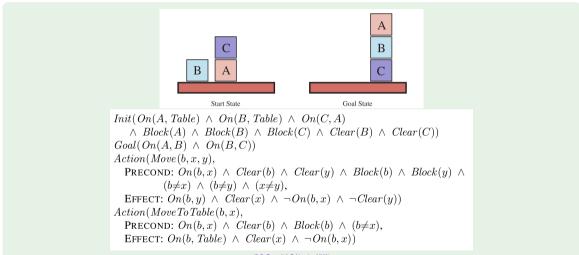
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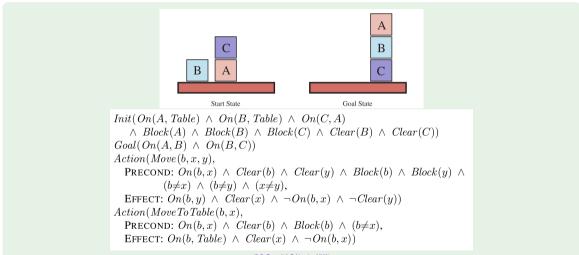
Example: Blocks World



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One solution: [MoveToTable(C, A), Move(B, Table, C), Move(A, Table, B)]

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Outline

Basics on Planning

- The Problem
- The PDDL Language

Search Strategies and Heuristics

- Forward and Backward Search
- Heuristics
- Planning Graphs, Heuristics and Graphplan
 - Planning Graphs
 - Heuristics Driven by Planning Graphs
 - The Graphplan Algorithm
- Other Approaches (hints)
 - Planning as SAT Solving
 - Planning as FOL Inference

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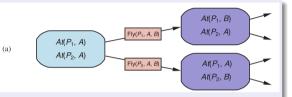
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Two Main Approaches

(a) Forward search (aka progression search)

- start in the initial state
- use actions to search forward for a goal state
- (b) Backward search (aka regression search
 - start from goals
 - use reverse actions to search forward for the initial state

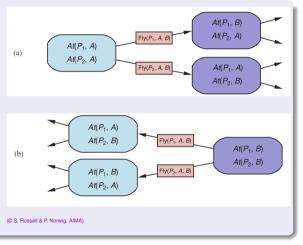


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- Forward search (aka progression search)
 - choose actions whose preconditions are satisfied
 - add positive effects, delete negative
- Goal test: does the state satisfy the goal?
- Step cost: each action costs 1
- \Rightarrow We can use any of the search algorithms from Ch. 03, 04
 - need keeping track of the actions used to reach the goal
- Breadth-first and best-first
 - Sound: if they return a plan, then the plan is a solution
 - Complete: if a problem has a solution, then they will return one
 - Require exponential memory wrt. solution length! \Longrightarrow unpractical
- Depth-first search and greedy search
 - Sound
 - Not complete
 - may enter in infinite loops
 - (classical planning only): made complete by loop-checking
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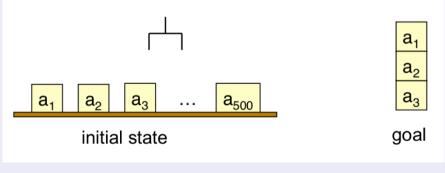
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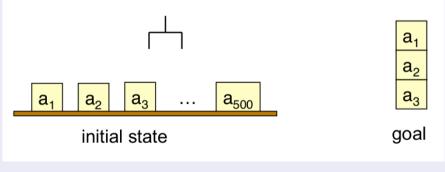
Planning problems can have huge state spaces

- Forward search can have a very large branching factor
 - ex: *pickup*(*a*₁), *pickup*(*a*₂), ..., *pickup*(*a*₅₀₀)
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- \implies Need a good heuristic to guide the search



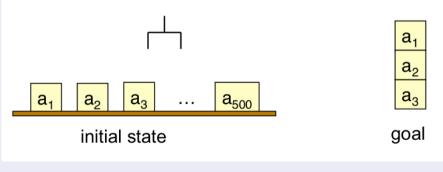
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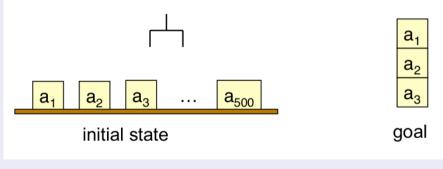


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- Note: Both g and g' represent many states
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- Idea: deal with partially un-instantiated actions and states
 - avoid unnecessary instantiations
 - \implies no need to produce a goal for every possible instantiation
- use the most general unifier \implies compute weakest precondition
- standardize action schemata first (rename vars into fresh ones)
- Consider the goal $At(C_1, SFO) \land At(C_2, JFK)$
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 - avoid unnecessary instantiations
 - \implies no need to produce a goal for every possible instantiation
- use the most general unifier

 compute weakest precondition
- standardize action schemata first (rename vars into fresh ones)
- Consider the goal $At(C_1, SFO) \land At(C_2, JFK)$
- Consider the partially-instantiated action: $Action(Unload(C_1, p', SFO), PRECOND : In(C_1, p') \land At(p', SFO) \land Cargo(C_1) \land Plane(p') \land Airport(SFO)$ $EFFECT : At(C_1, SFO) \land \neg In(C_1, p'))$
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Which action to choose?

- Relevant action: could be the last step in a plan for goal g
 - at least one of the action's effects (positive or negative) must unify with an element of the goal
 - (see AIMA book for formal definition)
- Consistent action: must not undo desired literals of the goal
 - inconsistent actions are also non-relevant
- Ex: consider the goal $At(C_1, SFO) \land At(C_2, JFK)$
 - Action(Unload(C₁, pl., SFO),) is relevant (previous example)
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- Recall: A* is a best-first algorithm which
 - uses an evaluation function f(s) = g(s) + h(s),
 - g(s): (exact) cost to reach s
 - h(s): admissible (optimistic) heuristics (never overestimates the distance to the goal)
- A technique for admissible heuristics: problem relaxation
 - \implies h(s): the exact cost of a solution to the relaxed problem
- Forms of problem relaxation exploiting problem structure
 - Add arcs to the search graph make it easier to search
 - ignore-preconditions heuristics
 - ignore-delete-lists heuristics
 - Clustering nodes (aka state abstraction) \implies reduce search space
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Ignore (some) Preconditions Heuristics

Ignore all preconditions drops all preconditions from actions

- every action is applicable in any state
- any single goal literal can be satisfied in one step (or there is no solution)
- fast, but over-optimistic
- Remove all preconditions & effects, except literals in the goal
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 - NP-complete, but greedy algorithms efficient
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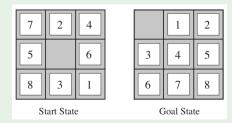
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Ignore-Preconditions Heuristics: Example

Sliding tiles

 $\begin{array}{l} \textit{Action}(\textit{Slide}(t, s_1, s_2), \\ \textit{PRECOND}: \textit{Tile}(t) \land \textit{Blank}(s_2) \land \textit{On}(t, s_1) \land \textit{Adjacent}(s_1, s_2) \\ \textit{EFFECT}: \textit{On}(t, s_2) \land \textit{Blank}(s_1) \land \neg\textit{On}(t, s_1) \land \neg\textit{Blank}(s_2)) \end{array}$

- Remove the preconditions $Blank(s_2) \land Adjacent(s_1, s_2)$
 - \implies we get the number-of-misplaced-tiles heuristics
- Remove the precondition *Blank*(s₂)
 - ⇒ we get the Manhattan-distance heuristics

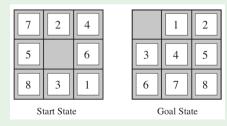


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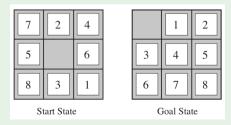


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 reasonable in many domains

Idea: Remove the delete lists from all actions

• No action will ever undo the effect of actions,

 $\Rightarrow~$ there is a monotonic progress towards the goa

• Still NP-hard to find the optimal solution of the relaxed problem

• can be approximated in polynomial time, with hill-climbing

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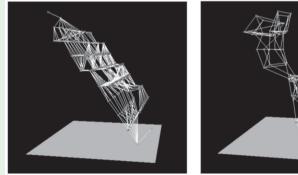
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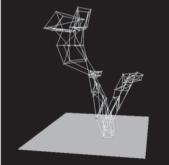
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Ignore Delete-list Heuristics: Example (Hoffmann'05)

- Planning state spaces with ignore-delete-lists heuristic
 - height above the bottom plane is the heuristic score of a state
 - states on the bottom plane are goals

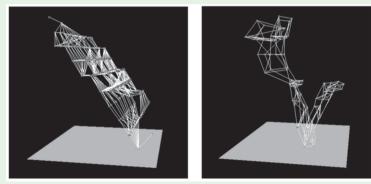




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 - · height above the bottom plane is the heuristic score of a state
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- \implies No local minima, non dead-ends, non backtracking
- \implies Search for the goal is straightforward for hill-climbing



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- Many-to-one mapping from states in the ground/original representation of the problem to a more abstract representation
 - drastically reduces the number of states
- Common strategy: ignore some (less-relevant) fluents
 - drop k fluents \implies reduce search space by 2^k factors
 - relevance based on (heuristic) evaluation or domain knowledge
- Air cargo problem: 10 airports, 50 planes, 200 pieces of cargo $\implies 10^{50} \cdot (50 + 10)^{200} \approx 10^{405}$ states (*)
- Consider particular problem in that domain
 - all packages are at 5 airports
 - all packages at a given airport have the same destination
- Abstraction: drop all "At" fluents except for these involving one plane and one package at each of the the 5 airports
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Other Strategies for Planning

Other strategies to define heuristics

- Problem decomposition
 - "divide & conquer" problem into subproblem
 - solve subproblems independently
- Using a data structure called "planning graphs" (next section)

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 - can drive an algorithm called Graphplan
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 - can be constructed very quickly
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- A directed graph, built forward and organized into levels
 - level S_0 : contain each ground fluent that holds in the initial state
 - level A_0 : contains each ground action applicable in S_0
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 - level A_i: contains all ground actions with preconditions in S_i
 - level S_{i+1} : all the effects of all the actions in A_i
 - each S_i may contain both P_j and $\neg P_j$
 - until $S_N = S_{N-1}$ ("leveled off").
- Contains persistence actions (aka maintenance actions, no-ops)
 - say that a literal / persists if no action negates it
- Mutual exclusion links (mutex) connect
 - incompatible pairs of actions
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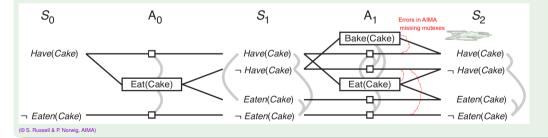
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Planning Graph: Example

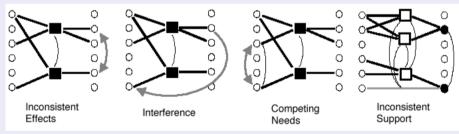
You would like to eat your cake and still have a cake. Fortunately, you can bake a new one.

> Rectangles indicate actions Small squares persistence actions (**no-ops**) Straight lines indicate preconditions and effects Mutex links are shown as curved gray lines



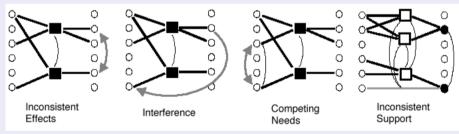
Mutex Computation

- Two actions at the same action-level have a mutex relation if
 - Inconsistent effects: an effect of one negates an effect of the other
 - Interference: one deletes a precondition of the other
 - Inconsistent preconditions (aka competing needs): they have mutually exclusive preconditions
- Otherwise they don't interfere with each other
 - \Rightarrow both may appear in a solution plan
- Two literals at the same state-level have a mutex relation if
 - inconsistent support: one is the negation of the other
 - all ways of achieving them are pairwise mutex



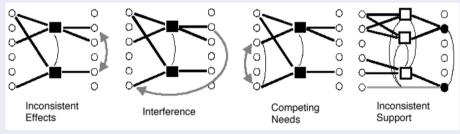
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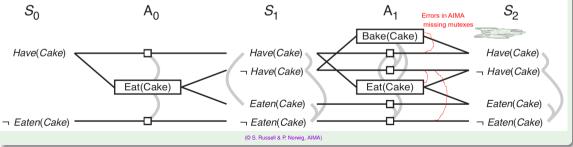


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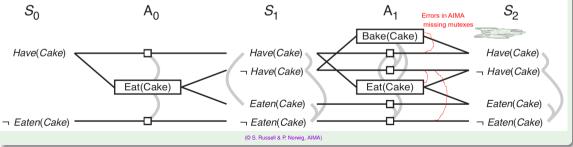
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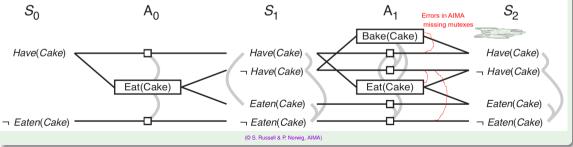
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 - Interference: one deletes a precondition of the other ex: Eat(Cake) interferes with the persistence of Have(Cake)
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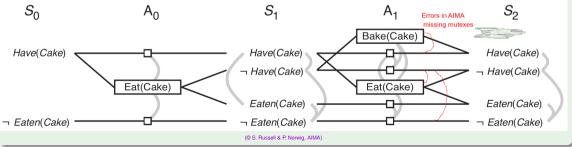
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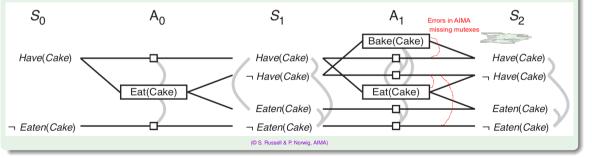


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Mutex Computation: Example [cont.]

- Two literals at the same state-level have a mutex relation if
 - inconsistent support: one is the negation of the other ex.: Have(Cake), ¬Have(Cake)
 - all ways of achieving them are pairwise mutex
 ex.: (S₁): Have(Cake) in mutex with Eaten(Cake)
 because persistence of Have(Cake), Eat(Cake) are mutex



Create initial layer S_0 :

() insert into S_0 all literals in the initial state

Repeat for increasing values of i = 0, 1, 2, ...

Create action layer A_i:

- for each action schema, for each way to unify its preconditions to non-mutually exclusive literals in S_i , enter an action node into A_i
- (a) for every literal in S_i , enter a no-op action node into A_i
- add mutexes between the newly-constructed action nodes

- () for each action node a in A_i ,
 - add to S_{i+1} the fluents in his Add list, linking them to a
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- If for every "no-op" action node a in A_i,
 - add the corresponding literal to S_{i+1}
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- ... until $S_{i+1} = S_i$ (aka "graph leveled off") or bound reached (if any)

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Planning Graphs: Properties

- Literals and actions increase monotonically and are finite
 we eventually reach a level where they stabilize
- Mutexes decrease monotonically (and cannot become less than zero)
 - \implies they too eventually must level off
- ⇒ When we reach this stable state, if one of the goal literals is missing or is mutex with another goal literal, then it will remain so
 ⇒ we can stop

Planning Graphs: Complexity

- A planning graph is polynomial in the size of the problem:
 - a graph with n levels, a actions, I literals, has size $O(n(a+l)^2)$
 - time complexity is also $O(n(a+l)^2)$
- \implies The process of constructing the planning graph is very fast
 - does not require choosing among actions

Outline

Basics on Planning

- The Problem
- The PDDL Language
- 2 Search Strategies and Heuristics
 - Forward and Backward Search
 - Heuristics
 - Planning Graphs, Heuristics and Graphplan
 - Planning Graphs
 - Heuristics Driven by Planning Graphs
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- Other Approaches (hints)
 - Planning as SAT Solving
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- Each level S_i represents a set of possible belief states
 - two literals connected by a mutex belong to different belief state
- A literal not appearing in the final level of the graph cannot be achieved by any plan
 - \Rightarrow if a goal literal is not in the final level, the problem is unsolvable
- The level S_j a literal I appears first is never greater than the level it can be achieved in a plan
 - *j* is called the level cost of literal *l*
- the level cost of a literal g_i in the graph constructed starting from state s, is an estimate of the cost to achieve it from s (i.e. h(g))
 - this estimate is admissible
 - ex: from s_0 Have(cake) has cost 0 and Eaten(cake) has cost 1
- Planning graph admits several actions per level
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 - if that fails, expand another level and try again (and add $\langle goal, level \rangle$ as nogood)
- If graph and nogoods have both leveled off then return failure
- Depends on EXPAND-GRAPH & EXTRACT-SOLUTION

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 \begin{array}{l} \textbf{function } \texttt{GRAPHPLAN}(problem) \ \textbf{returns} \ \texttt{solution or failure} \\ graph \leftarrow \texttt{INITIAL-PLANNING-GRAPH}(problem) \\ goals \leftarrow \texttt{CONJUNCTS}(problem.\texttt{GOAL}) \\ nogoods \leftarrow \texttt{an empty hash table} \\ \textbf{for } t] = 0 \ \textbf{to} \infty \ \textbf{do} \\ \hline \textbf{for } t] = 0 \ \textbf{to} \infty \ \textbf{do} \\ \hline \textbf{for } t] = 0 \ \textbf{to} \infty \ \textbf{do} \\ \hline \textbf{for } t] = 0 \ \textbf{to} \infty \ \textbf{do} \\ \hline \textbf{solution} \leftarrow \texttt{EXTRACT-SOLUTION}(graph, goals, \texttt{NUMLEVELS}(graph), nogoods) \\ \textbf{if } solution \neq failure \ \textbf{then return } solution \\ \hline \textbf{if } graph \ \textbf{and } nogoods \ \textbf{have both leveled off then return } failure \\ graph \leftarrow \texttt{EXPAND}-\texttt{GRAPH}(graph, problem) \\ \end{array}
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function GRAPHPLAN(problem) returns solution or failure

\begin{aligned} graph \leftarrow \text{INITIAL-PLANNING-GRAPH}(problem) \\ goals \leftarrow \text{CONJUNCTS}(problem.GOAL) \\ nogoods \leftarrow \text{an empty hash table} \\ \textbf{for } t] = 0 \textbf{ to } \infty \textbf{ do} \\ \end{aligned}
\begin{aligned} & \text{for } t] = 0 \textbf{ to } \infty \textbf{ do} \\ & \text{if } goals \text{ all non-mutex in } S_t \text{ of } graph \textbf{ then} \\ & \text{ solution } \leftarrow \text{EXTRACT-SOLUTION}(graph, goals, \text{NUMLEVELS}(graph), nogoods) \\ & \text{if } solution \neq failure \textbf{ then return } solution \\ & \text{if } graph \text{ and } nogoods \text{ have both leveled off then return } failure \\ & graph \leftarrow \text{EXPAND-GRAPH}(graph, problem) \end{aligned}
```

- A strategy for extracting a plan from the planning graph
- Repeatedly adds a level to a planning graph (EXPAND-GRAPH)
- If all the goal literals occur in last level and are non-mutex
 - search for a plan that solves the problem (EXTRACT-SOLUTION)
 - if that fails, expand another level and try again (and add $\langle goal, level \rangle$ as nogood)
- If graph and nogoods have both leveled off then return failure
- Depends on EXPAND-GRAPH & EXTRACT-SOLUTION

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function GRAPHPLAN(problem) returns solution or failure

graph \leftarrow INITIAL-PLANNING-GRAPH(problem)

goals \leftarrow CONJUNCTS(problem.GOAL)

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for t_{s} = 0 to \infty do

fi goals all non-mutex in S_t of graph then

solution \leftarrow EXTRACT-SOLUTION(graph, goals, NUMLEVELS(graph), nogoods)

if solution \neq failure then return solution

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graph \leftarrow EXPAND-GRAPH(graph, problem)
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[Recall] Example: Spare Tire Problem

```
Init(Tire(Flat) \land Tire(Spare) \land At(Flat, Axle) \land At(Spare, Trunk))
Goal(At(Spare, Axle))
Action(Remove(obj, loc),
  PRECOND: At(obj, loc)
  EFFECT: \neg At(obj, loc) \land At(obj, Ground))
Action(PutOn(t, Axle)),
   PRECOND: Tire(t) \land At(t, Ground) \land \neg At(Flat, Axle)
   EFFECT: \neg At(t, Ground) \land At(t, Axle))
Action(LeaveOvernight,
   PRECOND:
   EFFECT: \neg At(Spare, Ground) \land \neg At(Spare, Axle) \land \neg At(Spare, Trunk)
            \wedge \neg At(Flat, Ground) \land \neg At(Flat, Axle) \land \neg At(Flat, Trunk))
```

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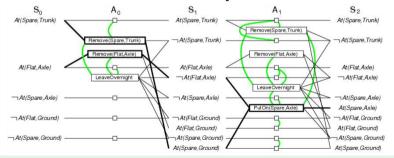
(We assume that the car is parked in a particularly bad neighborhood, so that the effect of leaving it overnight is that the tires disappear.)

One solution: [Remove(Flat, Axle), Remove(Spare, Trunk), PutOn(Spare, Axle)]

Graphplan: Example

Spare Tire problem

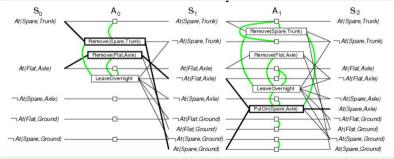
- Initial plan 5 literals from initial state and the Closed-World-Assumption literals (S₀).
 - fixed literals (e.g. Tire(Flat)) ignored here
 - irrelevant literals ignored here
- Goal At(Spare, Axle) not present in S₀
 - \implies no need to call EXTRACT-SOLUTION
- Graph and nogoods not leveled off \implies invoke EXPAND-GRAPH



Graphplan: Example [cont.]

Spare Tire problem

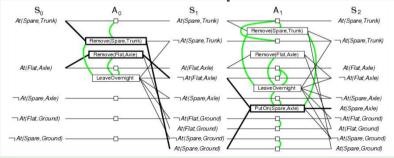
- Invoke EXPAND-GRAPH
 - add actions A₀, persistence actions and mutexes
 - add fluents S₁ and mutexes
- Goal At(Spare, Axle) not present in S₁
 - \implies no need to call EXTRACT-SOLUTION
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Graphplan: Example [cont.]

Spare Tire problem

- Invoke EXPAND-GRAPH
 - add actions A₁, persistence actions and mutexes
 - add fluents S₂ and mutexes
- Goal At(Spare, Axle) present in S₂
 - call EXTRACT-SOLUTION
- Solution found!



(© S. Russell & P. Norwig, AIMA) (inter-fluent mutexes omitted for readability)

- Consider the following variant of the Spare Tire problem: add *At*(*Flat*, *Trunk*) to the goal
- Write the (non-serialized) planning graph
- Extract a plan from the graph
- Do the same with the serialized planning graph

Graphplan "family" of algorithms, depending on approach used in EXTRACT-SOLUTION(...)

- Can be formulated as an (incremental) SAT problem
 - one proposition for each ground action and fluent
 - clauses represent preconditions, effects, no-ops and mutexes
- Can be formulated as a backward search problem
- Planning problem restricted to planning graph
 - mutexes found by EXPAND-GRAPH prune paths in the search tree
 - \Rightarrow much faster than unrestricted planning
- (if P.G. not serialized) may produce partial order plans
 - \Rightarrow may be later serialized into a total-order plan

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Partial-Order vs. Total-Order Plans

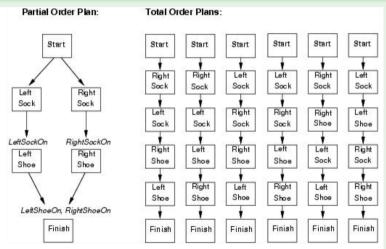
- Total-order plans: strictly linear sequences of actions
 - disregards the fact that some action are mutually independent
- Partial-order plans: set of precedence constraints between action pairs
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 - longest path to goal may be much shorter than total-order plan
 - easily converted into (possibly many) distinct total-order plans (any possible interleaving of independent actions)

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Partial-Order Plans: Example

Socks & Shoes Examples



Termination of Graphplan

- Theorem: If the graph and the no-goods have both leveled off, and no solution is found we can safely terminate with failure
- Intuition (proof sketch):
 - Literals and actions increase monotonically and are finite
 - \implies we eventually reach a level where they stabilize
 - Mutexes and no-goods decrease monotonically (and cannot become less than zero)
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Exercise

• Socks & Shoes example:

- Formalize the Socks & Shoes example in PDDL
- Write the non-serialized planning graph
- Compute the level cost for every fluent
- Choose some states, compute h(s) using the three heuristics
- Extract a plan from the graph in (2)
- Compare h(s) with the level they occur in the plan
- Write the serialized planning graph
- Repeat steps (3)-(6) with the serialized graph
- Do same steps (1)-(8) for the Air Cargo Transport example

Outline

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 - Many variants in the encoding
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Planning as SAT Solving [cont.]

- TRANSLATE-TO-SAT(INIT, TRANSITION, GOAL, T):
 - ground fluents & actions at each step are propositionalized
 - ex: $\langle At(P_1, SFO), 3 \rangle \Longrightarrow At_P_1_SFO_3$
 - ex: $\langle Fly(P_1, SFO, JFK), 3 \rangle \Longrightarrow Fly_P_1_SFO_JFK_3$
 - returns propositional formula: $Init^0 \land (\bigwedge_{i=1}^{t-1} Transition^{i,i+1}) \land Goal^t$
- *Init*⁰ and *Goal*^t: conjunctions of literals at step 0 and t resp.
 - ex: $Init^0$: $At_P_1_SFO_0 \land At_P_2_JFK_0$
 - ex: Goal³: $At_P_1_JFK_3 \wedge At_P_2_SFO_3$
- *Transition*^{i,i+1}: encodes transition from steps i to i + 1
 - Actions: Actionⁱ \rightarrow (Precondⁱ \wedge Effectsⁱ⁺¹) ex: Fly_P₁_SFO_JFK_2 \rightarrow (At_P₁_SFO_2 \wedge At_P₁_JFh
 - No-Ops: for each fluent F and step i:

$$\mathcal{F}^{i+1} \leftrightarrow \bigvee \mathsf{ActionCausingF}^i_k \lor (\mathsf{F}^i \land \bigwedge \neg \mathsf{ActionCausingNotF}^i_j)$$

- Mutex constraints: ¬Action¹/₁ ∨ ¬Action¹/₂
 ex: ¬Fly_P₁_SFO_JFK_2 ∨ ¬Fly_P₁_SFO_Newark_2
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- Trenslate it into SAT for t=0,1,2
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- Planning as FOL Inference

- Idea: formalize planning into FOL
- \Rightarrow use resolution-based inference for planning
 - Admit quantifications => very expressive
 - allows formalizing sentences like "move all the cargos from A to B regardless of how many pieces of cargo there are"
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Basic concepts

- Situation:
 - the initial state is a situation
 - if s is a situation and a is an action, then *Result(s, a)* is a situation

• Result() injective: Result(s, a) = Result(s', a') \leftrightarrow (s = s' \land a = a')

- Solution: a situation that satisfies the goal
- Action preconditions: $\Phi(s) \rightarrow \textit{Possible}(a, s)$
 - Φ(s) describes preconditions
 - ex: (Alive(Agent, s) \land Have(Agent, Arrow, s)) \rightarrow Possible(Shoot, s)
- Successor-state axioms (similar to propositional case):

• ex: $Possible(a, s) \rightarrow \begin{bmatrix} Holding(Agent, g, Result(a, s)) \leftrightarrow \\ a = Grab(g) \lor (Holding(Agent, g, s) \land a \neq Release(g)) \end{bmatrix}$

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- Situation:
 - the initial state is a situation
 - if s is a situation and a is an action, then *Result(s, a)* is a situation

• Result() injective: Result(s, a) = Result(s', a') \leftrightarrow (s = s' \land a = a')

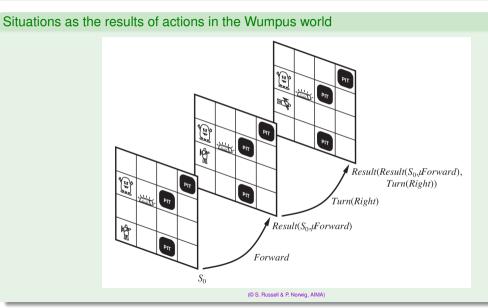
- Solution: a situation that satisfies the goal
- Action preconditions: $\Phi(s) \rightarrow \textit{Possible}(a, s)$
 - Φ(s) describes preconditions
 - ex: $(Alive(Agent, s) \land Have(Agent, Arrow, s)) \rightarrow Possible(Shoot, s)$
- Successor-state axioms (similar to propositional case):

 $[\text{Action is possible}] \rightarrow \left[\begin{array}{c} [\text{Fluent is true in result state}] \leftrightarrow \\ ([\text{Action's effect made it true}] \lor \\ ([\text{It was true before}] \land [\text{action left it alone}])) \end{array} \right]$

• ex: $Possible(a, s) \rightarrow \begin{bmatrix} Holding(Agent, g, Result(a, s)) \leftrightarrow \\ a = Grab(g) \lor (Holding(Agent, g, s) \land a \neq Release(g)) \end{bmatrix}$

• Unique action axioms: $A_i(x,...) \neq A_j(y,...)$ ex $Shoot(x) \neq Grab(y)$

Situation Calculus: Example



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