Fundamentals of Artificial Intelligence Chapter 04: Beyond Classical Search

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M.S. Course "Artificial Intelligence Systems", academic year 2020-2021

Last update: Tuesday 8th December, 2020, 13:06

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Outline

- Local Search and Optimization
 - Hill-Climbing
 - Simulated Annealing
- Local Beam Search & Genetic Algorithms
- Local Search in Continuous Spaces [hints]
- Search with Nondeterministic Actions
- Search with Partial Observations
 - Search with No Observations
 - Search with (Partial) Observations
- Online Search



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- Search techniques: systematic exploration of search space
 - solution to problem: the path to the goal state
 - ex: 8-puzzle
- With many problems, the path to goal is irrelevant
 - solution to problem: only the goal state itself
 - ex: N-queens
 - many important applications: integrated-circuit design, factory-floor layout, job-shop scheduling, automatic programming, telecommunications network optimization, vehicle routing, portfolio management...
 - goals expressed as conditions, not as explicit list of goal states
- The state space is a set of "complete" configurations
 - find goal configuration satisfying constraints/rules (ex: N-queens)
 - find optimal configurations
 (ex: Travelling Salesperson Problem, TSP)
- If so, we can use iterative-improvement algorithms (in particular local search algorithms):
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- Idea: use single current state and move to "neighbouring" states
 - operate using a single current node
 - the paths followed by the search are not retained
- Two key advantages:
 - use very little memory (usually constant)
 - can often find reasonable solutions in large or infinite (continuous state spaces, for which systematic algorithms are unsuitable
- Also useful for pure optimization problems
 - find the best state according to an objective function
 - often do not fit the "standard" search model of previous chapter
 - ex: Darwinian survival of the fittest: metaphor for optimization, but no "goal test" and no "path cost"
- A complete local search algorithm: guaranteed to always find a solution (if exists)
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 - maximization and minimization dual (switch sign)

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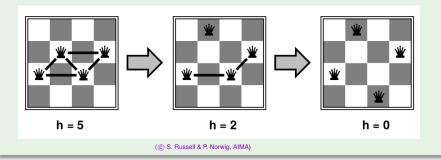
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Local Search Example: N-Queens

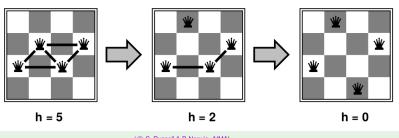
- One queen per column (incremental representation)
- Cost (h): # of queen pairs on the same row, column, or diagonal
- Goal: h=0
- Step: move a queen vertically to reduce number of conflicts



Almost always solves N-queens problems almost instantaneously for very large N (e.g., N=1million)

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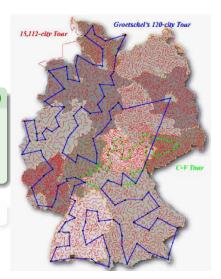
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Travelling Salesperson Problem (TSP)

Given an undirected graph, with n nodes and each arc associated with a positive value, find the Hamiltonian tour with the minimum total cost.

Very hard for classic search!

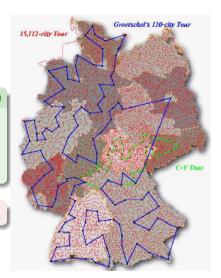


(Courtesy of Michela Milano, UniBO)

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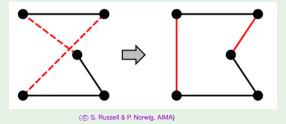
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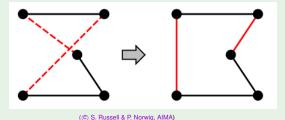
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- State represented as a permutation of numbers (1, 2, ..., n)
- Cost (h): total cycle length
- Start with any complete tour
- Step: (2-swap) perform pairwise exchange



Variants of this approach get within 1% of optimal very quickly with thousands of cities

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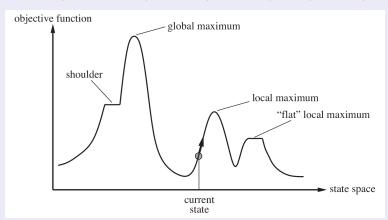


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Local Search: State-Space Landscape

State-space landscape (Maximization)

- Local search algorithms explore state-space landscape
 - state space n-dimensional (and typically discrete)
 - move to "nearby" states (neighbours)
- NP-Hard problems may have exponentially-many local optima



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Hill-Climbing

- Very-basic local search algorithm
- Idea: a move is only performed if the solution it produces is better than the current solution
 - (steepest-ascent version): selects the neighbour with best scores improvement (select randomly among best neighbours if ≥ 1)
 does not look ahead of immediate neighbors of the current state
 stops as soon as it finds a (possibly local) minimum
- Several variants (Stochastic H.-C., Random-Restart H.-C., ...
- Often used as part of more complex local-search algorithms

 $\textbf{function} \ \textbf{Hill-Climbing} (\textit{problem}) \ \textbf{returns} \ \textbf{a} \ \textbf{state} \ \textbf{that} \ \textbf{is} \ \textbf{a} \ \textbf{local} \ \textbf{maximum}$

```
current \leftarrow \texttt{MAKE-NODE}(problem.\texttt{INITIAL-STATE})
```

loop do

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function HILL-CLIMBING(problem) **returns** a state that is a local maximum

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current \leftarrow Make-Node(problem.Initial-State)
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```
neighbor \leftarrow a highest-valued successor of current if neighbor. Value \leq current. Value then return current. State current \leftarrow neighbor
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8-queen puzzle (minimization)

- Neighbour states: generated by moving one queen vertically
 - Cost (h): # of queen pairs on the same row, column, or diagonal
 - Goal: h=0
- Two scenarios $((a) \Longrightarrow (b)$ in 5 steps):

18	12	14	13	13	12	14	14
14	16	13	15	12	14	12	16
14	12	18	13	15	12	14	14
15	14	14	♛	13	16	13	16
₩	14	17	15	壍	14	16	16
17	₩	16	18	15	₩	15	₩
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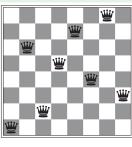


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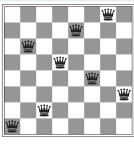


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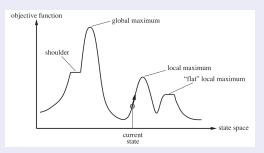




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Hill-Climbing Search: Drawbacks

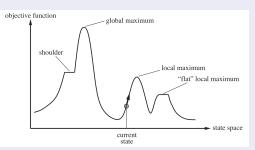
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 - Ex: with 8-queens, gets stuck 86% of the time, fast when succeed note: converges very fast till (local) minima or plateaux
- Possible idea: allow 0-progress moves (aka sideways moves)





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 - pros: may allow getting out of shoulders
 - cons: may cause infinite loops with flat local optima
 - ⇒ set a limit to consecutive sideways moves (e.g. 100)
 - Ex: with 8-queens, pass from 14% to 94% success, slower

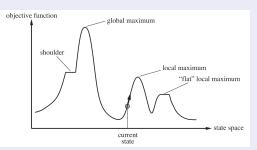




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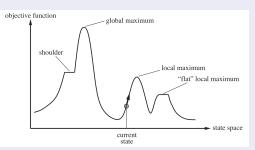




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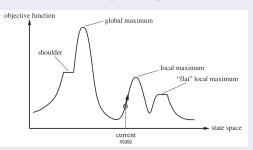




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Hill-climbing: Variations

Stochastic hill-climbing

- random selection among the uphill moves
- selection probability can vary with the steepness of uphill move
- sometimes slower, but often finds better solutions

First-choice hill-climbing

- cfr. stochastic h.c., generates successors randomly until a better one is found
- good when there are large amounts of successors

Random-restart hill-climbing

- conducts a series of hill-climbing searches from randomly generated initial states
- Tries to avoid getting stuck in local maxima

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Simulated Annealing

- Inspired to statistical-mechanics analysis of metallurgical annealing (Boltzmann's state distributions)
- Idea: Escape local maxima by allowing "bad" moves...
 - "bad move": move toward states with worse value
 - typically pick a move taken at random ("random walk")
- ... but gradually decrease their size and frequency.
 - sideways moves progressively less likely
- Analogy: get a ball into the deepest crevice in a bumpy surface
 - initially shaking hard ("high temperature")
 - progressively shaking less hard ("decrease the temperature")

Widely used in VSLI layout problems, factory scheduling, and other large-scale optimization tasks

Simulated Annealing [cont.]

Simulated Annealing (maximization)

- "temperature" T slowly decreases with steps ("schedule")
- The probability of picking a "bad move":
 - ullet decreases exponentially with the "badness" of the move $|\Delta E|$
 - decreases as the "temperature" T goes down
- If schedule lowers T slowly enough, the algorithm will find a global optimum with probability approaching 1

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Local Beam Search

- Idea: keep track of k states instead of one
- Initially: k random states
- Step:
 - determine all successors of k states
 - \bigcirc if any of successors is goal \Longrightarrow finished
 - else select k best from successors
- Different from k searches run in parallel:
 - searches that find good states recruit other searches to join them
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- Variant of local beam search: successor states generated by combining two parent states (rather than one single state)
- States represented as strings over a finite alphabet (e.g. {0,1})
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 - k parent pairs are selected at random for reproduction, with probability increasing with their fitness
 - for each parent pair

- Ends when some state is fit enough (or timeout)
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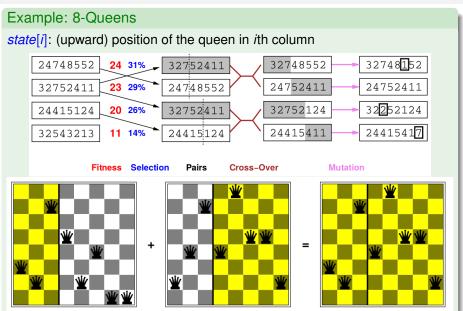
Resembles natural selection, with sexual reproduction

```
inputs: population, a set of individuals
        FITNESS-FN, a function that measures the fitness of an individual
repeat
    new\_population \leftarrow empty set
   for i = 1 to Size(population) do
       x \leftarrow \text{RANDOM-SELECTION}(population, \text{FITNESS-FN})
        y \leftarrow \text{RANDOM-SELECTION}(population, \text{FITNESS-FN})
        child \leftarrow REPRODUCE(x, y)
       if (small random probability) then child \leftarrow MUTATE(child)
       add child to new_population
    population \leftarrow new\_population
until some individual is fit enough, or enough time has elapsed
return the best individual in population, according to FITNESS-FN
```

function GENETIC-ALGORITHM(population, FITNESS-FN) returns an individual

```
function REPRODUCE(x,y) returns an individual inputs: x,y, parent individuals n \leftarrow \text{LENGTH}(x); \ c \leftarrow \text{random number from 1 to } n return APPEND(SUBSTRING(x,1,c), SUBSTRING(y,c+1,n))
```

Genetic Algorithms: Example



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Intuitions

- Selection drives the population toward high fitness
- Crossover combines good parts from good solutions (but it might achieve the opposite effect)
- Mutation introduces diversity

Pros & Cons

- Pros:
 - extremely simple
 - general purpose
 - tractable theoretical models
 - Cons:
 - not completely understood
 - good coding is crucial (e.g., Gray codes for numbers)
 - too simple genetic operators

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Outline

- Local Search and Optimization
 - Hill-Climbing
 - Simulated Annealing
 - Local Beam Search & Genetic Algorithms
- Local Search in Continuous Spaces [hints]
- Search with Nondeterministic Actions
- Search with Partial Observations
 - Search with No Observations
 - Search with (Partial) Observations
- Online Search



Local Search in Continuous Spaces [Hints]

Continuous environments

- Successor function produces infinitely many states
 - → previous techniques do not apply
- Discretize the neighborhood of each state
 - turn continuous space into discrete space
 - ullet e.g., empirical gradient considers $\pm \delta$ change in each coordinate
- Gradient methods compute gradients

$$\nabla f \stackrel{\text{def}}{=} \left[\frac{\partial f}{\partial x_1}, ..., \frac{\partial f}{\partial x_k} \right]$$

to increase/reduce f, e.g. by $x := x + \nabla f(x)$

- The Newton/Raphson Method iterates $x := x H_f^{-1}(X)\nabla f(x)$ where $H_f[i,j] \stackrel{\text{def}}{=} \frac{\partial^2 f}{\partial x_i \partial x_i}$ (Hessian matrix)
- all techniques from optimization theory

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- Assumptions so far (see ch. 2 and 3):
 - the environment is deterministic
 - the environment is fully observable
 - the agent knows the effects of each action
- The agent does not need perception:
 - can calculate which state results from any sequence of actions
 - always knows which state it is in
- If one of the above does not hold, then percepts are useful
 - the future percepts cannot be determined in advance
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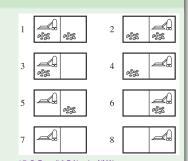
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Example: The Erratic Vacuum Cleaner

Erratic Vacuum-Cleaner Example

- actions: Left, Right, Suck
- goal: A and B cleaned (states 7, 8)
- if environment is observable, deterministic, and completely known ⇒ solvable by search algos
- ex: if initially in 1, then [suck,right,suck] leads to 8: [1,5,6,8]



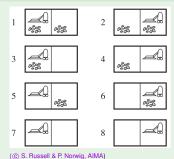
(© S. Russell & P. Norwig, AIMA)

- Nondeterministic version (erratic vacuum cleaner):
 - if dirty square: cleans the square, sometimes cleans also the other square. Ex: $1 \stackrel{suck}{\Longrightarrow} \{5,7\}$
 - if clean square: sometimes deposits dirt on the carpet Ex: $5 \stackrel{\text{suck}}{\Longrightarrow} \{1, 5\}$

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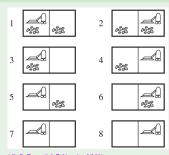
(C) S. Hussell & F. Norwig, Alivia

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- RESULTS(S,A) returns a set of possible outcomes states
 - Ex: RESULTS(1,SUCK)={5,7}, RESULTS(5,SUCK)={1,5}, ...
- A solution is a contingency plan (aka conditional plan, strategy)
 - contains nested conditions on future percepts (if-then-else, case-switch, ...)
 - Ex: from state 1 we can act the following contingency plan: [SUCK, IF STATE = 5 THEN [RIGHT, SUCK] ELSE []]
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And-Or Search Trees

- In a deterministic environment, branching on agent's choices
 - → OR nodes, hence OR search trees
 - OR nodes correspond to states
- In a nondeterministic environment, branching also on environment's choice of outcome for each action
 - the agent has to handle all such outcomes
 - ⇒ AND nodes, hence AND-OR search trees
 - AND nodes correspond to actions
 - leaf nodes are goal, dead-end or loop OR nodes
- A solution for an AND-OR search problem is a subtree s.t.:
 - has a goal node at every leaf
 - specifies one action at each of its OR nodes
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 - AND nodes correspond to actions
 - leaf nodes are goal, dead-end or loop OR nodes
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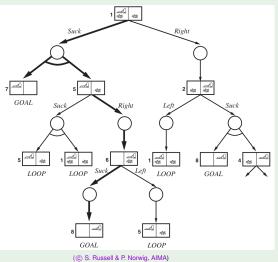
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And-Or Search Trees: Example

(Part of) And-Or Search Tree for Erratic Vacuum Cleaner Example. Solution for [SUCK, IF STATE = 5 THEN [RIGHT, SUCK] ELSE []]



AND-OR Search

Recursive Depth-First (Tree-based) AND-OR Search

```
\begin{tabular}{ll} \textbf{function} & \texttt{AND-OR-GRAPH-SEARCH}(problem) & \textbf{returns} & a & conditional & plan, & or & failure \\ & \texttt{OR-SEARCH}(problem.\texttt{INITIAL-STATE}, problem, [\ ]) \\ \end{tabular}
```

```
function OR-SEARCH(state, problem, path) returns a conditional plan, or failure if problem.GOAL-TEST(state) then return the empty plan if state is on path then return failure for each action in problem.ACTIONS(state) do plan \leftarrow \text{AND-SEARCH}(\text{RESULTS}(state, action), problem, [state \mid path]) if plan \neq failure then return [action \mid plan] return failure
```

```
function AND-SEARCH(states, problem, path) returns a conditional plan, or failure for each s_i in states do plan_i \leftarrow \text{OR-SEARCH}(s_i, problem, path) if plan_i = failure then return failure return [\text{if } s_1 \text{ then } plan_1 \text{ else if } s_2 \text{ then } plan_2 \text{ else } \dots \text{if } s_{n-1} \text{ then } plan_{n-1} \text{ else } plan_n]
```

(© S. Russell & P. Norwig, AIMA)

Note: nested if-then-else can be rewritten as case-switch

AND-OR Search [cont.]

Recursive Depth-First (Tree-based) AND-OR Search

- ullet Cycles: if the current state already occurs in the path \Longrightarrow failure
 - cycle detection like with ordinary DFS
 - does not mean "no solution"
 - means "if there is a non-cyclic solution, it must be reachable from the earlier incarnation of the current state"
- Complete (if state space finite): every path must reach a goal, a dead-end or loop state
- Can be augmented with "explored" data structure for avoiding redundant branches (graph-based search)
- Can also be explored by breadth-first or best-first method
 - e.g. A* variant for AND-OR search available (see AIMA book)

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Some problems have no acyclic solutions

- A cyclic plan may be considered a cyclic solution provided that:
 - every leaf is a goal state(loop states not considered leaves), and
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- Can be expressed by means of introducing
 - labels, and backward goto's to labels
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- Executing a cyclic solution eventually reaches a goal, provided that each outcome of a nondeterministic action eventually occurs
- Is this assumption reasonble?
- Yes, provided we distinguish: ⟨nondeterministic, observable⟩
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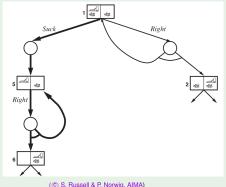
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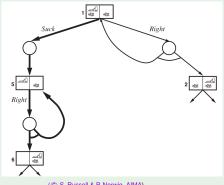
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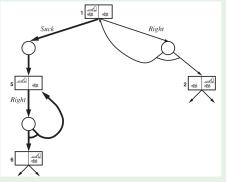
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- A cyclic solution
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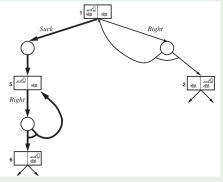
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 - Hill-Climbing
 - Simulated Annealing
 - Local Beam Search & Genetic Algorithms
- 2 Local Search in Continuous Spaces [hints]
- Search with Nondeterministic Actions
- Search with Partial Observations
 - Search with No Observations
 - Search with (Partial) Observations
- Online Search



- Partial observability: percepts do not capture the whole state
 partial state corresponds to a set of possible physical states
- If the agent is in one of several possible physical states, then an action may lead to one of several possible outcomes, even if the environment is deterministic
- Belief state: the agent's current belief about the possible physical states it might be in, given the previous sequence of actions and percepts
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- Idea: To solve sensorless problems, the agent searches in the space of belief states rather than in that of physical states
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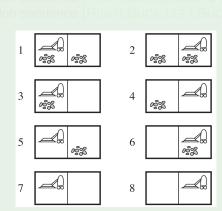
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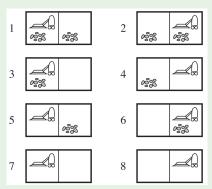
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Example: Sensorless Vacuum Cleaner

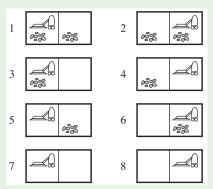
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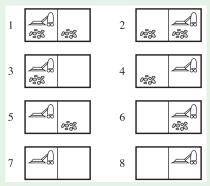
- the vacuum cleaner knows the geography of its world, but it doesn't know its location or the distribution of dirt
 - initial state: {1,2,3,4,5,6,7,8}
 - after action RIGHT, state is {2, 4, 6, 8}
 - after action sequence [RIGHT, SUCK], state is {4,8}
 - after action sequence [RIGHT, SUCK, LEFT, SUCK], state is {7}



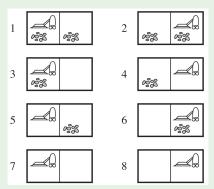
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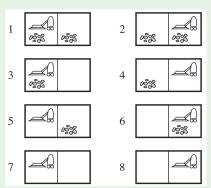
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- Belief states: subsets of physical states
 - If P has N states, then the sensorless problem has up to 2^N states
- Initial state: typically the set of all physical states in P
- Actions: (assumption: illegal actions have no effects)
 - $Actions(b) \stackrel{\text{def}}{=} \bigcup_{s \in b} Actions_P(s)$
- Transition model:
 - for deterministic actions:

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b' = Result(b, a) \stackrel{\text{def}}{=} \{s' \mid s' = Result_P(s, a) \text{ and } s \in b\}
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- for nondeterministic actions: $b' = Result(b, a) \stackrel{\text{def}}{=} \{s' \mid s' \in Result_P(s, a) \text{ and } s \in b\} = \bigcup_{s \in b} Result_P(s, a)$
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Belief-State Problem Formulation

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 - If P has N states, then the sensorless problem has up to 2^N states
- Initial state: typically the set of all physical states in P
- Actions: (assumption: illegal actions have no effects)
 - $Actions(b) \stackrel{\text{def}}{=} \bigcup_{s \in b} Actions_P(s)$
- Transition model:
 - for deterministic actions:

```
b' = Result(b, a) \stackrel{\text{def}}{=} \{s' \mid s' = Result_P(s, a) \text{ and } s \in b\}
```

- for nondeterministic actions: $b' = Result(b, a) \stackrel{\text{def}}{=} \{s' \mid s' \in Result_P(s, a) \text{ and } s \in b\} = \bigcup_{s \in b} Result_P(s, a)$
- This step is called Prediction: $b' \stackrel{\text{def}}{=} Predict(b, a)$
- Goal test: GoalTest(b) holds iff $GoalTest_P(s)$ holds, $\forall s \in b$
- Path cost: (assumption: cost of an action the same in all states)
 - $StepCost(a, b) \stackrel{\text{def}}{=} StepCost_P(a, s), \forall s \in b$

 $Actions_P()$, $Result_P()$, $GoalTest_P()$, $StepCost_P()$ refer to physical System P

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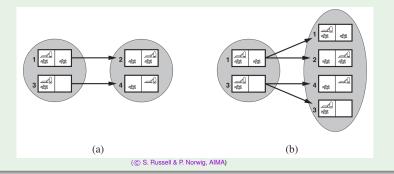
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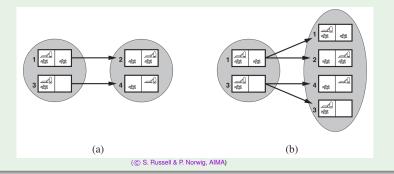
Example: Sensorless Vacuum Cleaner, plain and slippery versions

Prediction: Result({1,3}, Right), deterministic (a) and nondeterministic action (b)



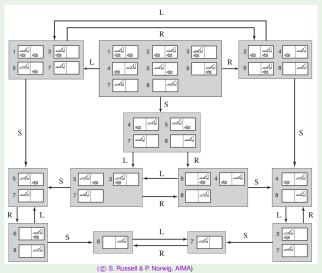
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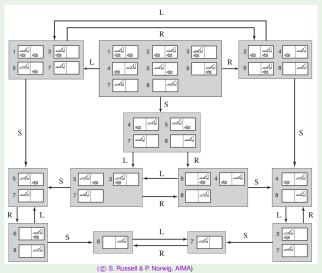
Example: Sensorless Vacuum Cleaner: Belief State Space

(note: self-loops are omitted)



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Remarks

- if $b \subseteq b'$, then $Result(b, a) \subseteq Result(b', a)$
- If a is deterministic, then $|Result(b, a)| \le |b|$
- The agent might achieve the goal earlier than *GoalTest(b)* holds, but it does not know it

Properties

- An action sequence is a solution for b iff it leads b to to a goal
- If an action sequence is a solution for a belief state b, then it is also a solution for any belief state b' s.t. $b' \subseteq b$
 - \bullet if $b \stackrel{a_1}{\mapsto} \stackrel{a_k}{\mapsto} g$, then $b' \stackrel{a_1}{\mapsto} \stackrel{a_k}{\mapsto} g$

- we can discard a path reaching a belief state b if $b' \subseteq b$ has already been generated and discarded
- if a solution for b has been found, then any $b' \subseteq b$ is solvable
- \implies Dramatically improves efficiency

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Outline

- Local Search and Optimization
 - Hill-Climbing
 - Simulated Annealing
 - Local Beam Search & Genetic Algorithms
- 2 Local Search in Continuous Spaces [hints]
- Search with Nondeterministic Actions
- Search with Partial Observations
 - Search with No Observations
 - Search with (Partial) Observations
- Online Search

- Percept(s) returns the percept received in state s
 - if sensing is nondeterministic, it returns a set of possible percepts
 - ex: (local-sensing vacuum cleaner, can perceive dirty/clean only on the current position): Percept(1) = [A. Dirty]
 - with fully observable problems: $Percept(s) = s, \forall s$
 - with sensorless problems: Percept(s) = null, ∀s
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 - ex: Percept(1) = Percept(3) = [A, Dirty]
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- Three steps (aka prediction-observation-update process):
 - Prediction: (same as for sensorless): $\hat{b} = Predict(b, a) \stackrel{\text{def}}{=} Result_{constant}(b, a) = \{s' \mid s' = Result_{constant}(b, a) \text{ and } s \in b\}$
 - Observation prediction: determines the set of percepts that could
 - be observed in the predicted belief state

 PossiblePercepts(\hat{b}) $\stackrel{\text{def}}{=} \{o \mid o = Percept(s) \text{ and } s \in \hat{b}\}$
 - Update: for each percept o, determine the belief state b_o , i.e., the set of states in \hat{b} that could have produced the percept o
 - $b_o = \textit{Update}(\hat{b}, o) \stackrel{\mathsf{def}}{=} \{ s \mid s \in \hat{b} \; \textit{and} \; o = \textit{Percept}(s) \}$
- \Rightarrow Result(b, a) = $\left\{b_o \middle| \begin{array}{ccc} b_o = & Update(Predict(b, a), o) & and \\ o \in & PossiblePercepts(Predict(b, a)) \end{array}\right\}$
 - $b_o \subseteq \hat{b}, \forall o \Longrightarrow$ sensing reduces uncertainty!
 - (if sensing is deterministic) the b_0 's are all disjoint $\implies \hat{b}$ partitioned into smaller belief states, one for each possible
- Non-deterministic belief-state problem
 - due to the inability to predict exactly the next percept

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- \Rightarrow Result $(b,a)=\left\{b_o \mid b_o=Update(Predict(b,a),o) \ and \ o\in PossiblePercepts(Predict(b,a)) \
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Transition Model with Perceptions

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 - Observation prediction: determines the set of percepts that could be observed in the predicted belief state
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 - **3** Update: for each percept o, determine the belief state b_o , i.e., the set of states in \hat{b} that could have produced the percept o
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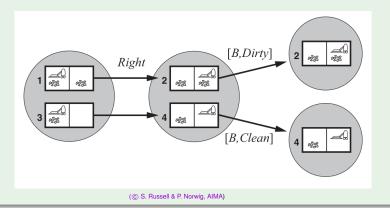
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Transition Model with Perceptions: Example

Deterministic: Local-sensing vacuum cleaner

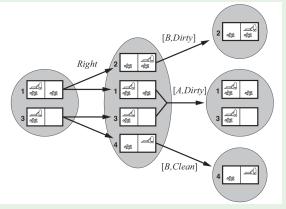
- $\hat{b} = Predict(\{1,3\}, Right) = \{2,4\}$
- $PossiblePercepts(\hat{b}) = \{[B, Dirty], [B, Clean]\}$
- Result({1,3}, Right) = {{2}, {4}}



Transition Model with Perceptions: Example

Nondeterministic: Slippery local-sensing vacuum cleaner

- $\hat{b} = Predict(\{1,3\}, Right) = \{1,2,3,4\}$
- PossiblePercepts(\hat{b}) = {[B, Dirty], [A, Dirty], [B, Clean]}
- Result({1,3}, Right) = {{2}, {1,3}, {4}}



- Formulation as a nondeterministic belief-state search problem
- \implies The AND-OR search algorithms can be applied
- \implies The solution is a conditional plan

Solution for [A, Dirty]: [Suck, Right, if Bstate = 6 then Suck else []

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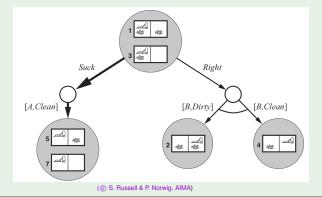
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- Agent quite similar to the simple problem-solving agent [Ch.3]
 - formulates a problem as a belief-state search
 - calls an AND-OR-GRAPH search algorithm
 - executes the solution
- Two main differences:
 - the solution is a conditional plan, not an action sequence
 - the agent needs to maintain its belief state as it performs actions and receives percepts (aka monitoring, filtering, state estimation)
- Similar to the prediction-observation-update process:
 - simpler, because the percept o is given by the environment
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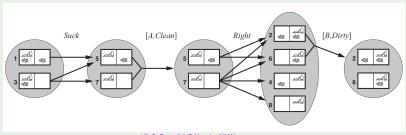
Example: Belief-State Maintenance

Example: Kindergarden Vacuum-Cleaner

- local sensing ⇒ partially observable
- any square may become dirty at any time unless the agent is actively cleaning
 it at that moment

 nondeterministic

Ex: Update(Predict({5,7}, Right), [B, Dirty]) = {2,6}



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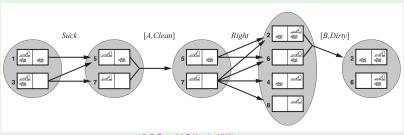
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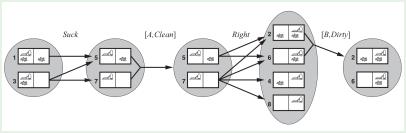
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- Knows the map, senses walls in the four directions (NESW)
 - localization broken: does not know where it is
 - navigation broken: does not know the direction is moving to
 - goal: localization (know where it is)
- $b = \{all\ locations\}, o = NSW$

 - \bigcirc $b_o = Update(Predict(Update(b, NSW), Move), NS) = (b)$

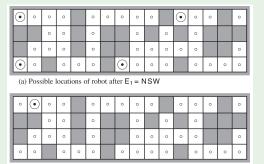


(a) Possible locations of robot after E₁ = NSW

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	0	0		0	0	0		0	٥	0	0		٥	0	0	٥

(b) Possible locations of robot After E₁ = NSW, E₂ = NS

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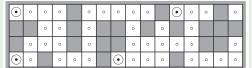
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Outline

- Local Search and Optimization
 - Hill-Climbing
 - Simulated Annealing
 - Local Beam Search & Genetic Algorithms
- 2 Local Search in Continuous Spaces [hints]
- Search with Nondeterministic Actions
- Search with Partial Observations
 - Search with No Observations
 - Search with (Partial) Observations
- Online Search



- So far: Offline search
 - it computes a complete solutions before executing it
- Online search: agent interleaves computation and action
 - it takes an action,
 - then it observes the environment and computes the next action
 - (repeat)
- Useful in nondeterministic domains
 - prevents search blowup
- Necessary in dynamic domains or unknown domains
 - cannot know the states and consequences of actions
 - faces an exploration problem: must use actions as experiments in order to learn enough
 - ex: a robot placed in a new building
 - ⇒ must explore it to build a map to use for getting from A to B
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Online vs. offline search

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 - GoalTest(s)
- Remark: The agent cannot determine Result(s, a)
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- The agent knows an admissible heuristic function h(s), that estimates the distance from the current state to a goal state
- Objective: reach goal with minimal cost
 - Cost: total cost of traveled path
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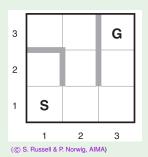
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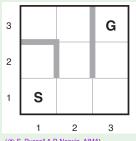
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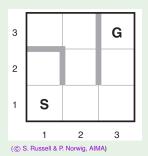
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- the agent might know the location of the goal
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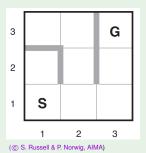
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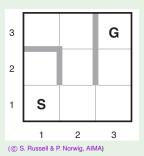
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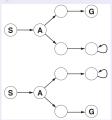


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- No algorithm can avoid dead ends in all state spaces
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 - If states S and A visit. What next?
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- Assumption the state space is safely explorable: some goal state is reachable from every reachable state (ex: reversible actions)

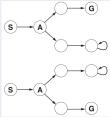
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 - map is updated based on percept input after every action
 - map is used to decide next action
- Difference wrt. offline algorithms (ex A*, BFS)
 - Can only expand the node it is physically in
 - Needs to backtrack physically

- Works only if actions are always reversible
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Online Search Agents: Basic Ideas

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 - DFS: go back to the state from which the agent most recently entered the current state
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Online Search Agents [cont.]

function ONLINE-DFS-AGENT(s') **returns** an action

```
inputs: s', a percept that identifies the current state
persistent: result, a table indexed by state and action, initially empty
             untried, a table that lists, for each state, the actions not yet tried
             unbacktracked, a table that lists, for each state, the backtracks not yet tried
             s, a, the previous state and action, initially null
if GOAL-TEST(s') then return stop
if s' is a new state (not in untried) then untried[s'] \leftarrow ACTIONS(s')
if s is not null then
    result[s, a] \leftarrow s'
    add s to the front of unbacktracked[s']
if untried[s'] is empty then
    if unbacktracked[s'] is empty then return stop
    else a \leftarrow an action b such that result[s', b] = POP(unbacktracked[s'])
else a \leftarrow Pop(untried[s'])
s \leftarrow s'
return a
```

(© S. Russell & P. Norwig, AIMA)

- Hill Climbing natural candidate for online search
 - locality of search
 - only one state is stored
 - unfortunately, stuck in local minima
 - random restarts not possible
- Possible solution: Random Walk
 - selects randomly one available actions from the current state
 - preference can be given to actions that have not yet been tried
 - eventually finds a goal or complete its exploration if space is finite
 - unfortunately, very slow

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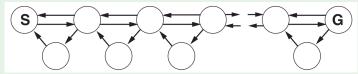
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LRTA*: General ideas

- Better possible solution: add memory to hill climbing
- Idea: store a "current best estimate" H(s) of the cost to reach the goal from each state that has been visited
 - initially h(s)
 - updated as the agent gains experience in the state space

(recall that h(s) is in general "too optimistic")

⇒ Learning Real-Time A* (LRTA*)

- builds a map of the environment in the result[s,a] table
- chooses the "apparently best" move a according to current H(
- updates the cost estimate H(s) for the state s it has just left,
 using the cost estimate of the target state s'
 - \bullet H(s) := c(s, a, s') + H(s')
- "optimism under uncertainty": untried actions in s are assumed to lead immediately to the goal with the least possible cost h(s)
- \Longrightarrow encourages the agent to explore new, possibly promising paths

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if s' is undefined then return h(s) else return c(s, a, s') + H[s']

```
function LRTA*-AGENT(s') returns an action
  inputs: s', a percept that identifies the current state
  persistent: result, a table, indexed by state and action, initially empty
               H, a table of cost estimates indexed by state, initially empty
               s, a, the previous state and action, initially null
  if GOAL-TEST(s') then return stop
  if s' is a new state (not in H) then H[s'] \leftarrow h(s')
  if s is not null
       result[s, a] \leftarrow s'
      H[s] \leftarrow \min_{b \in ACTIONS(s)} LRTA*-COST(s, b, result[s, b], H)
   a \leftarrow an action b in ACTIONS(s') that minimizes LRTA*-COST(s', b, result[s', b], H)
  s \leftarrow s'
  return a
function LRTA*-COST(s, a, s', H) returns a cost estimate
```

Example: LRTA*

Five iterations of *LRTA** on a one-dimensional state space

- states labeled with current H(s), arcs labeled with step cost
- shaded state marks the location of the agent,
- updated cost estimates a each iteration are circled

