

Scientific Programming

Lecture A04 – Functions

Andrea Passerini

Università degli Studi di Trento

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Table of contents

- 1 Defining functions
- 2 Functions for problem decomposition
- 3 Namespaces
- 4 Passing arguments

How to define a function

Functions

Functions are **named blocks of code**. They take inputs and produce outputs.

Abstract syntax

```
def f(arg1, arg2, ...):  
    # the code  
    return <result-exp>
```

- The **arguments** (arg1, arg2, etc.) are variables that specify how many inputs the function takes.

Calling a function

```
the_result = f(value1, value2, ...)
```

Example

```
def plus(a, b):  
    r = a + b  
    return r
```

```
x = 5  
y = 10
```

```
z = plus(x, y)  
print(z)
```

Why functions?

Motivations

- Creating a new function gives you an opportunity to name a group of statements, which **makes your program easier to read and debug**.
- Functions can make a program smaller by **eliminating repetitive code**. Later, if you make a change, you only have to make it in one place.
- **Dividing a long program into functions allows you to debug the parts one** at a time and then assemble them into a working whole.
- **Well-designed functions are often useful for many programs**. Once you write and debug one, you can reuse it.

Fruitful vs void functions

```
from math import sqrt

def hypotenuse(side1,side2):
    return sqrt(side1**2 + side2**2)

def printWarnings():
    print("I never said most of the things I said.")
    print("Yogi Berra")

x = hypotenuse(3,4)
y = printWarnings()
print(x,y)
```

Fruitful vs void functions

```
from math import sqrt

def hypotenuse(side1,side2):
    return sqrt(side1**2 + side2**2)

def printWarnings():
    print("I never said most of the things I said.")
    print("Yogi Berra")

x = hypotenuse(3,4)
y = printWarnings()
print(x,y)
```

```
I never said most of the things I said.
Yogi Berra
5.0 None
```

A first explanation about naming

The name of the variables passed to the function has nothing to do with the name of the arguments

- In the example, the values of the variables `x`, `y` are visible inside the function as `a`, `b`:

```
def plus(a, b):  
    r = a + b  
    return r
```

- When called,
 - `a` takes the value of `x`
 - `b` takes the value of `y`

```
x = 5  
y = 10
```

```
z = plus(x, y)  
print(z)
```

A first explanation about naming

The name of the variables used to store the result inside and outside the call has nothing to do with each other

- In the example, the result is stored
 - in variable `r` inside the function
 - in variable `z` by the caller.
- When the call is concluded,
 - `z` takes the value of `r`

```
def plus(a, b):  
    r = a + b  
    return r
```

```
x = 5  
y = 10
```

```
z = plus(x, y)  
print(z)
```

A first explanation about naming

Python 3.6

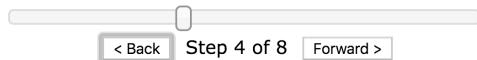
```

1 def plus(a, b):
2     r=a+b
3     return r
4
5 x = 5
➡ 6 y = 10
7
➡ 8 z = plus(x, y)

```

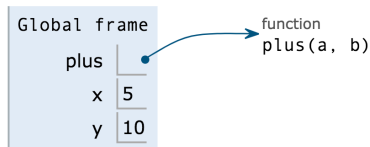
➡ line that has just executed

➡ next line to execute



Frames

Objects



A first explanation about naming

Python 3.6

```

→ 1 def plus(a, b):
    2     r=a+b
    3     return r
    4
    5 x = 5
    6 y = 10
    7
→ 8 z = plus(x, y)

```

→ line that has just executed

→ next line to execute



Frames

Objects

Global frame

plus	
x	5
y	10

function
plus(a, b)

plus

a	5
b	10

A first explanation about naming

Python 3.6

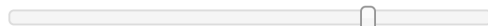
```

1 def plus(a, b):
2     r=a+b
3     return r
4
5 x = 5
6 y = 10
7
8 z = plus(x, y)

```

→ line that has just executed

→ next line to execute



< Back

Step 7 of 8

Forward >

Frames

Objects

Global frame

plus	
x	5
y	10

function
plus(a, b)

plus	
a	5
b	10
r	15

A first explanation about naming

Python 3.6

```

1 def plus(a, b):
2     r=a+b
3     return r
4
5 x = 5
6 y = 10
7
8 z = plus(x, y)

```

→ line that has just executed

→ next line to execute



< Back

Step 8 of 8

Forward >

Frames

Objects

Global frame

plus	
x	5
y	10

function
plus(a, b)

plus

a	5
b	10
r	15

Return
value

15

A first explanation about naming

Python 3.6

```

1  def plus(a, b):
2      r=a+b
3      return r
4
5  x = 5
6  y = 10
7
➡ 8  z = plus(x, y)

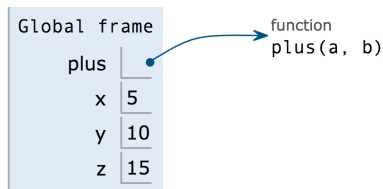
```

➡ line that has just executed

➡ next line to execute

Frames

Objects



< Back

Program terminated

Forward >

Function definition

A function does nothing until it is called

```
print("beginning")
```

```
def f():  
    print("I do stuff")
```

```
print("end")
```

Function definition

A function does nothing until it is called

```
print("beginning")
```

```
def f():  
    print("I do stuff")
```

```
print("end")
```

```
beginning  
end
```

Function definition

If called after its definition, the function is executed without problems

```
print("beginning")
```

```
def f():  
    print("I do stuff")
```

```
f()  
print("end")
```

Function definition

If called after its definition, the function is executed without problems

```
print("beginning")
```

```
def f():  
    print("I do stuff")
```

```
f()  
print("end")
```

```
beginning  
I do stuff  
end
```

Function definition

Functions must be defined before they are called

```
print("beginning")  
f()
```

```
def f():  
    print("I do stuff")
```

```
print("end")
```

Function definition

Functions must be defined before they are called

```
print("beginning")  
f()
```

```
def f():  
    print("I do stuff")
```

```
print("end")
```

```
beginning
```

```
Traceback (most recent call last):
```

```
  File "lecture.py", line 3, in <module>  
    f()
```

```
NameError: name 'f' is not defined
```

Function definition: some explanations

Unlike many languages, `def` is a **statement** that:

- creates a new object of type **function** by reading the code indented after `def`
- assign it to a variable called as the name of the function

The name of the function is like any other variable; can be copied in other variables, used as a function parameters, etc.

```
print("beginning")
def f():
    print("I do stuff")
print(type(f))
fun = f
fun()
print("end")
```

```
beginning
<class 'function'>
I do stuff
end
```

Exercise

Problem

Write a function that given in input a positive integer n , returns the factorial of n .

Exercise

Problem

Write a function that given in input a positive integer n , returns the factorial of n .

```
def fact(n):  
    res = 1  
    for k in range(1, n + 1):  
        res = res * k  
    return res
```

```
factorials = [fact(n) for n in range(1,11)]  
print(factorials)
```

```
[1, 2, 6, 24, 120, 720, 5040, 40320, 362880, 3628800]
```

Multiple results

A function may return multiple results

```
def multiresult():  
    result_1 = "AA"  
    result_2 = 0.12  
    result_3 = "*"   
    return result_1, result_2, result_3
```

Internally, Python interprets the return statement as **returning a tuple**. In practice, the above code is equivalent to:

```
def multiresult():  
    return ("first result", 0.12, "something else")
```

Multiple results

When a “multi-result” function is called, the resulting tuple can be assigned to a variable; elements have to be extracted individually

```
def multiresult():  
    return ("first result", 0.12, "something else")  
  
result = multiresult()  
res0 = result[0]  
res1 = result[1]  
res2 = result[2]  
print(res0+res2, res1)
```

Multiple results

When a “multi-result” function is called, the resulting tuple can be assigned to a variable; elements have to be extracted individually

```
def multiresult():  
    return ("first result", 0.12, "something else")
```

```
result = multiresult()  
res0 = result[0]  
res1 = result[1]  
res2 = result[2]  
print(res0+res2, res1)
```

```
first resultsomething else 0.12
```

Multiple results

Otherwise, the “automatic unpacking” feature of Python can be used

```
def multiresult():  
    return ("first result", 0.12, "something else")
```

```
res0, res1, res2 = multiresult()  
print(res0+res2, res1)
```

```
first resultsomething else 0.12
```

Multiple results

Automatic unpacking only works with the same number of elements

```
def multiresult():  
    return ("first result", 0.12, "something else")
```

```
res0, res1 = multiresult()
```

```
Traceback (most recent call last):
```

```
File "prova.py", line 4, in <module>
```

```
    x,y = fun()
```

```
ValueError: too many values to unpack (expected 2)
```

Exercise

Problem

Write a function that takes two lists as input and returns their intersection, i.e. the objects that appear in both of them.

```
def intersect(seq1, seq2):
```

Exercise

Problem

Write a function that takes two lists as input and returns their intersection, i.e. the objects that appear in both of them.

```
def intersect(seq1, seq2):  
    res = []  
    for x in seq1:  
        if x in seq2:  
            res.append(x)  
    return res
```

Polymorphism

Like all good functions in Python, `intersect()` is **polymorphic**. That is, it works on arbitrary types, as long as they support the expected interface - being iterable.

```
print(intersect([1,2,3], [2,3,4]))  
print(intersect("ABC", "CB0"))  
print(intersect((1,2,4), [3,4,1]))
```

Polymorphism

Like all good functions in Python, `intersect()` is **polymorphic**. That is, it works on arbitrary types, as long as they support the expected interface - being iterable.

```
print(intersect([1,2,3], [2,3,4]))  
print(intersect("ABC", "CB0"))  
print(intersect((1,2,4), [3,4,1]))
```

```
[2, 3]
```

```
['B', 'C']
```

```
[1, 4]
```

Table of contents

- 1 Defining functions
- 2 Functions for problem decomposition**
- 3 Namespaces
- 4 Passing arguments

Problem decomposition

Problem

We want to write a program that:

- reads several sensor datasets from disk;
- reads which pairs of sensors are physically related (e.g., installed close to each other);
- computes correlation statistics for each related pair;
- reports the average statistics over all pairs.

Rather than writing one big block of code, let's break the problem down into small, well-named functions. For now, we only sketch their **skeleton**: signature and docstring, no real implementation yet.

Problem decomposition

```
def read_dataset(path):  
    """Takes a path to a CSV file, returns a  
    header-values pair."""  
    return #"sensor_12", [23.1, 24.0, 22.9, ...]  
  
def read_datasets(paths):  
    """Reads a bunch of CSV files, returns a  
    dict of header-values pairs."""  
    header_to_values = {}  
    for path in paths:  
        header, values = read_dataset(path)  
        header_to_values[header] = values  
    return header_to_values
```

Problem decomposition

```
def read_relationships(path):  
    """Reads physical sensor relationships from a  
    file. Returns a list of pairs of strings."""  
    return #[("sensor_12", "sensor_45"), ("sensor_45", "sensor_45"), ...]  
  
def compute_correlation_stats(values1, values2):  
    """Compute correlation statistics, e.g.  
    co-occurrence or mutual information."""  
    return #correlation, #mutual_information
```

Problem decomposition

```
def compute_avg_stats(datasets, relationships):  
    """Takes a list of statistics (in some format) and  
    computes the average statistics."""  
    stats = []  
    for sensor1, sensor2 in relationships:  
        if sensor1 in datasets and sensor2 in datasets:  
            values1 = datasets[sensor1]  
            values2 = datasets[sensor2]  
            stats.append(compute_correlation_stats(values1,  
                                                    values2))  
    return stats
```

Problem decomposition

```
def main():
    """The whole (fake) program."""

    # Read the sensor datasets
    paths = []
    ans = input("path to CSV file: ")
    while len(ans) > 0:
        paths.append(ans)
        ans = input("path to CSV file: ")
    datasets = read_datasets(paths)

    # Read the relationship file
    ans = input("path to relationship data: ")
    relationships = read_relationships(ans)

    # Print the average stats
    print("average stats =", compute_avg_stats(datasets, relationships))

main()
```

Table of contents

- 1 Defining functions
- 2 Functions for problem decomposition
- 3 Namespaces**
- 4 Passing arguments

Namespaces and scopes

Namespace

A **namespace** (sometimes also called a **context**) is a naming system for making names unique to avoid ambiguity.

- Naming people: `firstname surname [birthday][birthplace]`
- Naming websites: `subdomain.domain.top-level-domain`

Scope

The **scope** of a name is the area of a program where this name can be unambiguously used, for example inside of a function.

Namespaces and scopes

To associate a name, with a particular namespace, Python uses **the location of the assignment of such name**

In other words, the place where you assign a name in your source determines the **namespace** it will live in, and hence its **scope** of visibility.

Local variables

By default, all names assigned inside a function are associated with that function's namespace (**local namespace**)

```
def func():  
    x = 88  
    print("Inside", x)
```

```
func()  
print("Outside", x)
```

Local variables

By default, all names assigned inside a function are associated with that function's namespace (**local namespace**)

```
def func():  
    x = 88  
    print("Inside", x)
```

```
func()  
print("Outside", x)
```

- Names assigned inside a **def** can only be seen by the code within that **def**.
- **x** is called a **local** variable

Inside 88

Traceback (most recent call last):

```
File "lecture.py", line 6, in <module>  
    print("Outside", x)
```

NameError: name 'x' is not defined

Global variables

Names defined outside functions are associated with the **global namespace**.

```
# Var defined before the  
# function and the call  
x = 88  
def func():  
    print("Inside", x)  
  
func()  
print("Outside", x)
```

Global variables

Names defined outside functions are associated with the **global namespace**.

```
# Var defined before the  
# function and the call
```

```
x = 88
```

```
def func():  
    print("Inside", x)
```

```
func()  
print("Outside", x)
```

```
Inside 88
```

```
Outside 88
```

- Names assigned outside a **def** can be seen by functions, *provided that they are defined before the function is called.*
- **x** is called a **global** variable

Global variables

Names defined outside functions are associated with the **global namespace**.

```
def func():  
    print("Inside", x)  
  
# Var defined before the call  
x = 88  
func()  
print("Outside", x)
```

Global variables

Names defined outside functions are associated with the **global namespace**.

```
def func():  
    print("Inside", x)  
  
# Var defined before the call  
x = 88  
func()  
print("Outside", x)
```

```
Inside 88  
Outside 88
```

- Names assigned outside a **def** can be seen by functions, *provided that they are defined before the function is called.*
- **x** is called a **global** variable

Global variables

```
def func():  
    print("Inside", x)  
  
func()  
# Var defined after the call  
x = 88  
print("Outside", x)
```

Global variables

```
def func():  
    print("Inside", x)
```

```
func()  
# Var defined after the call  
x = 88  
print("Outside", x)
```

Inside 88

Traceback (most recent call last):

```
File "lecture.py", line 2, in func  
    print("Inside", x)
```

NameError: name 'x' is not defined

- Names assigned outside a `def` can be seen by functions, *provided that they are defined before the function is called.*
- `x` was not defined before the call

Local and global variables

If a variable exists in both the local and global namespace, the copies are distinct.

```
x = 99
```

```
def func():  
    x = 88  
    print("Inside", x)
```

```
func()  
print("Outside", x)
```

Local and global variables

If a variable exists in both the local and global namespace, the copies are distinct.

```
x = 99
```

```
def func():  
    x = 88  
    print("Inside", x)
```

```
func()  
print("Outside", x)
```

```
Inside 88  
Outside 99
```

- Inside the function, the local namespace for `x` is used.
- Outside the function, the global namespace for `x` is used.

Table of contents

- 1 Defining functions
- 2 Functions for problem decomposition
- 3 Namespaces
- 4 Passing arguments

Argument-passing basic

Basic rules

- Arguments are passed by automatically assigning objects to local variable names
- Assigning to argument names inside a function does not affect the caller.
- Changing a mutable object argument in a function may impact the caller.

Argument-passing basic

- Immutable arguments are effectively passed “by value.”

Objects such as integers and strings are passed by object reference instead of by copying, but because you can't change immutable objects in place anyhow, the effect is much like making a copy.

- Mutable arguments are effectively passed “by pointer”.

Objects such as lists and dictionaries are also passed by object reference, and the object can be effectively modified.

Passing immutable arguments

```
def func(a):  
    a = 99
```

```
b = 88  
func(b)  
print(b)
```

Passing immutable arguments

```
def func(a):  
    a = 99
```

```
b = 88  
func(b)  
print(b)
```

88

Passing mutable arguments

```
def func(a, b):  
    a = 2  
    b[0] = 99
```

```
X = 1  
L = [1,2]  
func(X,L)  
print(X,L)
```

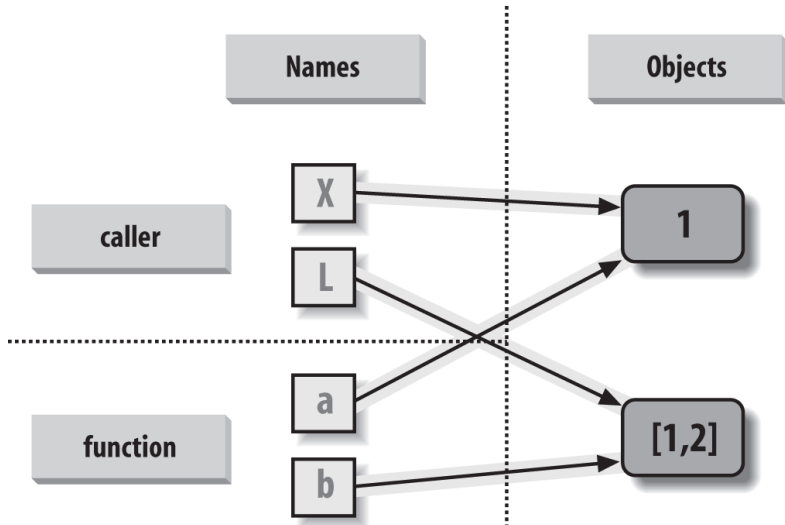
Passing mutable arguments

```
def func(a, b):  
    a = 2  
    b[0] = 99
```

```
X = 1  
L = [1,2]  
func(X,L)  
print(X,L)
```

```
1 [99,2]
```

Passing mutable arguments



Avoid changes - use copies

Sometimes, the caller knows that the function is going to modify mutable objects, but she wants to avoid modifications. The mutable object must be copied before the call.

```
def func(a, b):  
    a = 2  
    b[0] = 99  
  
X = 1  
L = [1,2]  
func(X,L[:])  
print(X,L)
```

Avoid changes - use copies

Sometimes, the caller knows that the function is going to modify mutable objects, but she wants to avoid modifications. The mutable object must be copied before the call.

```
def func(a, b):
```

```
    a = 2
```

```
    b[0] = 99
```

```
X = 1
```

```
L = [1,2]
```

```
func(X,L[:])
```

```
print(X,L)
```

```
1 [1,2]
```

Avoid changes - use copies

Sometimes, the functions needs to modify a mutable object (for example, to sort it), but this change should not be reported back to the caller. The mutable object must be copied in the function.

```
def func(a, b):
```

```
    a = 2
```

```
    b = b[:]
```

```
    b[0] = 99
```

```
X = 1
```

```
L = [1,2]
```

```
func(X,L)
```

```
print(X,L)
```

Avoid changes - use copies

Sometimes, the functions needs to modify a mutable object (for example, to sort it), but this change should not be reported back to the caller. The mutable object must be copied in the function.

```
def func(a, b):
```

```
    a = 2
```

```
    b = b[:]
```

```
    b[0] = 99
```

```
X = 1
```

```
L = [1,2]
```

```
func(X,L)
```

```
print(X,L)
```

```
1 [1,2]
```

Passing parameters by name

Knowing the name of the parameters, is it possible to pass the values by specifying **name=value**. This is useful in combination with defining defaults (see next slide).

```
def f(a, b, c):  
    print(a, b, c)
```

```
f(1, 2, 3)  
f(c=1, b=2, a=3)  
f(1, c=3, b=2)
```

Passing parameters by name

Knowing the name of the parameters, is it possible to pass the values by specifying **name=value**. This is useful in combination with defining defaults (see next slide).

```
def f(a, b, c):  
    print(a, b, c)
```

```
f(1, 2, 3)           1 2 3  
f(c=1, b=2, a=3)  
f(1, c=3, b=2)
```

Passing parameters by name

Knowing the name of the parameters, is it possible to pass the values by specifying **name=value**. This is useful in combination with defining defaults (see next slide).

```
def f(a, b, c):  
    print(a, b, c)
```

f(1, 2, 3)	1 2 3
f(c=1, b=2, a=3)	3 2 1
f(1, c=3, b=2)	

Passing parameters by name

Knowing the name of the parameters, is it possible to pass the values by specifying **name=value**. This is useful in combination with defining defaults (see next slide).

```
def f(a, b, c):  
    print(a, b, c)
```

f(1, 2, 3)	1 2 3
f(c=1, b=2, a=3)	3 2 1
f(1, c=3, b=2)	1 2 3

Defining defaults

```
def f(a, b=2, c=3):  
    print(a, b, c)
```

f(1)

f(4,5)

f(2,3,4)

f(1, c=5)

Defining defaults

```
def f(a, b=2, c=3):  
    print(a, b, c)
```

f(1)

1 2 3

f(4,5)

f(2,3,4)

f(1, c=5)

Defining defaults

```
def f(a, b=2, c=3):  
    print(a, b, c)
```

f(1)	1 2 3
f(4,5)	4 5 3
f(2,3,4)	
f(1, c=5)	

Defining defaults

```
def f(a, b=2, c=3):  
    print(a, b, c)
```

f(1)	1 2 3
f(4,5)	4 5 3
f(2,3,4)	2 3 4
f(1, c=5)	

Defining defaults

```
def f(a, b=2, c=3):  
    print(a, b, c)
```

f(1)	1 2 3
f(4,5)	4 5 3
f(2,3,4)	2 3 4
f(1, c=5)	1 2 5

Exercise

Problem

Create a function `check_alphanumeric()` that takes a string and returns `True` if and only if the string is alphanumeric (contains only alphabetic or numeric characters).

Exercise

Problem

Create a function `check_alphanumeric()` that takes a string and returns `True` if and only if the string is alphanumeric (contains only alphabetic or numeric characters).

```
def check_alphanumeric(s):  
    for c in s.upper():  
        if c not in "ABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789":  
            return False  
    return True
```

Exercise

Problem

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```
def palindromic(s):  
    L = list(s)  
    L.reverse()  
    return s == "".join(L)
```