

Project Assignments

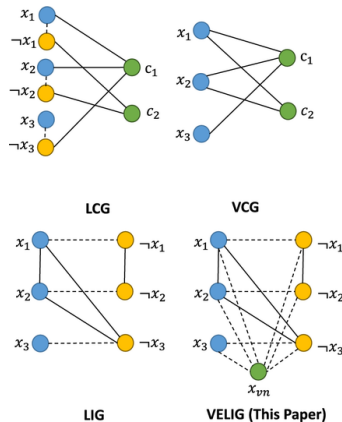
SML Lab, University of Trento

Advanced Topics in Machine Learning and Optimization — 2024-25

Predicting SAT hardness via GNNs

Assignment

- **SAT**isfiability is the problem of checking whether a logic formula is satisfiable by a truth assignment. Graph Neural Networks (GNNs) have been applied to many SAT-related task, from end-to-end SAT solving to feature extraction.
- **Goal:** use **GNNs** for predicting the runtime of SAT instances.
- **Applications:** solver selection in portfolio approaches, theoretical understanding of SAT hardness
- The student is asked to:
 - Create a dataset of formulas/runtime; see ([Liu et al., 2024](#)).
 - Train (and evaluate) the GNNs for predicting the runtime.
 - (option) Analyzing "similar" formulas exhibiting significantly different runtimes.
 - (option) Train on multiple SAT solvers.



Multiple graph representation of a formula.

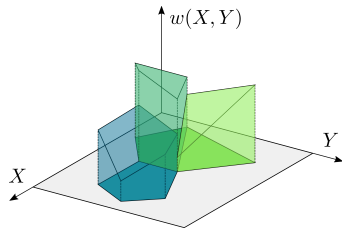
Notes

- **Contact:** [Antonio Longa](#), [Stefano Teso](#), [Paolo Morettin](#)
- Extensible to thesis!

Approximating volume computations via GNNs

Assignment

- Beyond SAT, Graph Neural Networks (GNNs) have been used for approximating other computationally hard problems. We turn to the problem of computing the volume of a **convex polytopes** $\Delta = \bigwedge_i \mathbf{A}_i \mathbf{x} \leq b$
- **Goal:** find a suitable graphical representation of Δ , then train a GNN for approximating $\text{vol}(\Delta)$.
- **Applications:** constrained probabilistic inference
- The student is asked to:
 - Create a dataset of $\langle \Delta_k, \text{vol}(\Delta_k) \rangle$ pairs
 - Implement a procedure for encoding polytopes as graphs. Train (and evaluate) the GNNs.
 - (option) Experiment with different encodings.
 - (option) Compare with sequence-based models (provided).



Polytopes encoding a complex probability distribution.

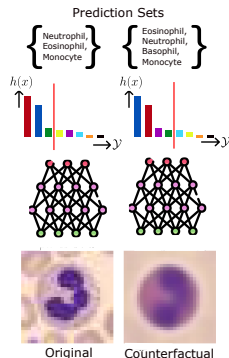
Notes

- **Contact:** [Veronica Lachi Paolo Morettin](#)
- Extensible to thesis!

Counterfactuals with Conformal Predictors

Assignment

- *Conformal prediction* is a framework for uncertainty quantification which can be used to build decision support systems that improve experts' accuracy in classification tasks with theoretical guarantees via *prediction sets* (Straitouri et al., 2023). However, the connection between conformal prediction and explanations is still unexplored.
- The student is asked to:
 - Generate a synthetic dataset for multi-label classification and train a classifier.
 - Implement a *conformal predictor* to extract *prediction sets*.
 - Implement a *counterfactual generating* technique optimizing *sparsity* or *proximity*.
 - Analyze the relationship between *sparsity* and *proximity* and the variations in the *prediction sets*.



Notes

- **Contact:** Cesare Barbera, Giovanni De Toni
- Extensible to thesis!

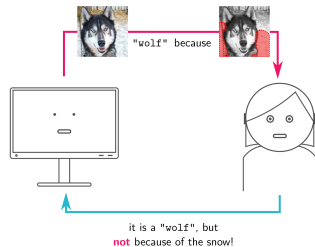
Explanatory Interaction: Ask Smarter Questions!

Assignment

- Explanatory Interactive Learning ([Schramowski et al., 2020](#)) is great for *deconfounding* models, however it builds on very simple active learning strategies for selecting items to be labelled.

Can we do better?

- The student is asked to:
 - Take existing explanatory debugging code and integrate a [state-of-the-art algorithm for confounding-aware query selection](#).
 - Evaluate on confounded data whether this strategy brings the intended benefits.



Explanatory interactive learning (XIL)

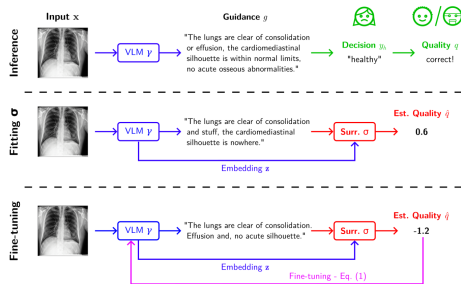
Notes

- **Contact:** [Stefano Teso](#)
- Extensible to thesis!

Learning to Guide Users with CBMs, RLHF-style

Assignment

- In **Learning to Guide** (LTG), a model is learned to produce *textual guidance* useful for guiding human decision makers. This requires fine-tuning an LLM, and in turn a lot of expensive supervision. **Can we do better with CBMs?**
- The student is asked to:
 - Read up on learning to guide ([Banerjee et al., 2024](#)).
 - Design a (simple) classification task
 - Design and train surrogate model that scores the CBM's explanations based on how much they are helpful for a down-stream decision maker.
 - Teach the CBM to output more useful explanations, **RLHF style!**



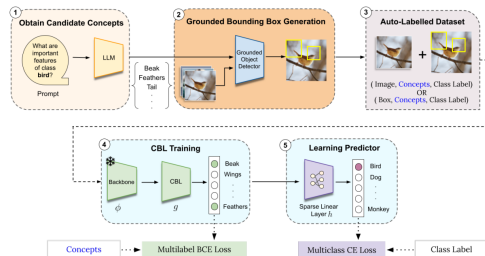
Notes

- **Contact:** [Debodeep Banerjee](#), [Burcu Sayin](#), [Stefano Teso](#)
- Extensible to thesis!

Improving Concepts with Vision-Language Models

Assignment

- **Concept-based Models (CBMs)** learn to map input images to high-level concepts, such as “fluffy dog” and “red car”. These concepts may however not be high quality.
- Can we exploit **Vision-Language Models (VLMs)** to obtain feedback about properties that learned concepts ought to satisfy? ([Srivastava et al., 2024](#))
- The student is asked to:
 - Design a (simple) classification task in which concepts learned by a stock CBM is not great.
 - Query a VLM about properties of learned concepts (“should the ball be red?”) and align the CBM accordingly.



Notes

- **Contact:** [Emanuele Marconato](#), [Stefano Teso](#)
- Extensible to thesis!

Assignment

- Unchecked use of LLMs in law is risky; involving humans in the loop of decision-making in legal tasks is more ethical and practical.
- The student is asked to:
 - Develop an LLM-powered Intelligent Assistant (IA) to augment human decision-makers in the legal field. The IA will not make a final decision but rather help the legal expert make a final decision through an argumentative interaction.

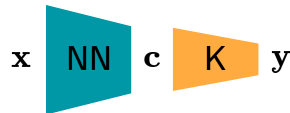
Notes

- **Contact:** [Burcu Sayin](#), [Andrea Passerini](#)
- Extensible to thesis!

Shortcuts in NeSy Models with Structured Knowledge

Assignment

- Inductive Logic Programming ([Evans and Grefenstette, 2018](#)) (ILP) allows to learn logical rules from examples and background knowledge.
- NeSy models (that learns both concepts and knowledge) are prone to reasoning shortcuts and algorithmic shortcuts. What happens when knowledge is more complex?
- The student is asked to:
 - Design an end-to-end NeSy architecture that uses differentiable ILP;
 - Create a logical task that admits reasoning and algorithmic shortcuts;
 - Compare this model with existing ones. Is it more robust to shortcuts?



x : **0 1** c : [A, B] K :

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	0

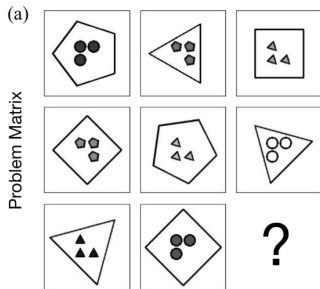
Notes

- **Contact:** [Samuele Bortolotti](#), [Emanuele Marconato](#)
- Extensible to thesis!

Can Neuro-Symbolic models cheat at IQ tests?

Assignment

- NeSy architectures combine learning and perception with reasoning. Sometimes, they solve the task by learning concepts with unexpected or unclear semantics. These are **reasoning shortcuts**.
- Can NeSy models do so in IQ tests like **Raven matrices**?
- The student is asked to:
 - Read up on reasoning shortcuts ([Bortolotti et al., 2024](#)) and Raven matrices ([Zhang et al., 2019](#)).
 - Design a (simplified) Raven data set for one of the NeSy models available in ([Bortolotti et al., 2024](#)).
 - Learn a model on your data and evaluate whether it learns any reasoning shortcuts.



A Raven matrix. What should the missing square be?

Notes

- **Contact:** [Samuele Bortolotti](#), [Emanuele Marconato](#), [Stefano Teso](#)
- Extensible to thesis!

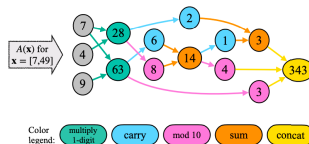
Algorithmic Reasoning in Large Language Models

Assignment

- Surprisingly, Large Language Models perform really well on various tasks they are not trained for.
- Arithmetic Reasoning (e.g., sum, product, ...) is known to be a serious limitation for these models (Dziri et al., 2023).
- We want to test the hypothesis that LLMs do not learn **the intended reasoning algorithm**: the cheapest variant is discovered, which does not generalize.
- The student is asked to:
 - Design tasks of arithmetic reasoning.
 - Use chain-of-thought (COT) techniques to obtain the “reasoning” algorithm of LLMs (Dziri et al., 2023)
 - Validate through **Mechanistic Interpretability** whether the COT is faithful (Wu et al., 2023).

```
function multiply (x[1..p], y[1..q]):  
  // multiply x for each y[i]  
  for i = q to 1  
    carry = 0  
    for j = p to 1  
      t = x[j] * y[i]  
      t += carry  
      carry = t // 10  
      digits[j] = t mod 10  
    summands[i] = digits  
  
  // add partial results (computation not shown)  
  product =  $\sum_{i=1}^q \text{summands}[q+1-i] \cdot 10^{i-1}$   
  return product
```

$A(\mathbf{x})$



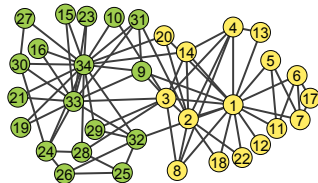
Notes

- Contact:** Emanuele Marconato, Samuele Bortolotti
- Extensible to thesis!

GNN node classification for homophilic and heterophilic labels

Assignment

- The scientific literature contains somewhat inconclusive and potentially conflicting statements regarding the role of *Label Homophily* (the property that two connected nodes are likely to have the same label) for the success of GNN node classifiers.
- The student is asked to:
 - Review recent research literature and critically evaluate existing experimental evaluations of classification performance under different levels of homophily
 - Design new and improved experimental evaluations, e.g. by creating customized synthetic data
 - Explore possible combinations of GNN classifiers with other techniques to optimize performance both under Homo- and Heterophily



Notes

- **Contact:** [Andrea Passerini](#) [Manfred Jaeger](#),
- Extensible to thesis!

Graph Neural Networks for Relational Databases

Assignment

- Databases are ubiquitous, yet deep learning often underperforms compared to tree-based models (e.g., boosting and random forests) in database-related tasks. A recent trend involves converting relational databases into graphs and applying Graph Neural Network models to them. However, these graphs exhibit distinctive features, such as being multipartite, high-diameter, and highly heterogeneous.
- The student is asked to:
 - Test standard GNN models on relational databases benchmark. (RelBench^a)
 - Investigate potential limitations of GNN models when applied to multipartite graphs.
 - The project can be tailored based on the student's preferences, allowing for either (a) a more theoretical focus, for those interested in conceptual exploration. (b) An empirical focus, for students who prefer practical experimentation and analysis.
- Further details can be discussed in a brainstorming session, either in person or online, with Francesco, Antonio, and Veronica.



^a<https://relbench.stanford.edu/>

Notes

- **Contact:** [Francesco Ferrini](#), [Antonio Longa](#), [Veronica Lachi](#)
- Extensible to thesis!

Assignment

- Although Message Passing is the most common framework for learning relational data, it has notable limitations, including Oversmoothing ([Chen et al., 2020](#)), Oversquashing ([Di Giovanni et al., 2023](#)), Under-reaching ([Errica et al., 2023](#)), and challenges with Robustness ([Günemann, 2022](#)).
- It remains unclear which of these issues most significantly impacts the training dynamics and generalization performance of GNNs.
- The student is tasked with:
 - Investigating how (some of) these phenomena evolve during training and whether they correlate with generalization error.
 - Examining how (some of) these phenomena evolve during training and whether they impact the quality of the explanations ([Yuan et al., 2022](#); [De Luca et al., 2024](#)).

Notes

- **Contact:** [Vincenzo Marco De Luca](#)
- Extensible to thesis!

Graph Neural Networks: Can they Generalize with limited data?

Assignment

- Numerous regularization techniques have been proposed for Graph Neural Networks, with most focusing on topological-level adjustments (e.g., rewiring, dropping ([Fang et al., 2023](#))).
- While these strategies have shown positive effects on reducing generalization error, the GNN literature still lacks a thorough comparison with prominent Few-Shot Learning ([Satorras and Estrach, 2018](#)) strategies.
- The student is tasked with:
 - Benchmark various topological regularizers and Few-Shot Learning strategies on the most famous graph datasets to evaluate their potential.

Notes

- **Contact:** [Vincenzo Marco De Luca](#)
- Extensible to thesis!

Project work

- Select one of the projects from the previous slides (or discuss with the teacher for custom projects)
- Complete it and prepare a report summarizing the methodology used and the results obtained
- After completing the assignment send it via email to the (first) contact person for the project
- Subject: ADVML2024
- Attachment: name_surname.zip containing:
 - the report (named report.pdf)
 - the code you wrote
 - the requirements needed to run the code

NOTE

- No group work
- Preliminary versions of the report can be sent for feedback
- The project is discussed asynchronously as soon as it is completed

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