

Algorithmic Recourse

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Advanced Topics in Machine Learning and Optimization
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Why do we need explanations?

- ▶ **Recidivism risk** (Dressel & Farid [8])
- ▶ **University admissions** (Waters & Miikkulainen [30])
- ▶ **Rejecting/Accepting a job applicant** (Liem et al. [15])
- ▶ **Prescribing medications and treatments** (Yoo et al. [31])
- ▶ Many others...

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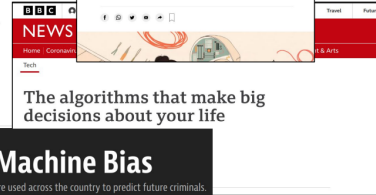
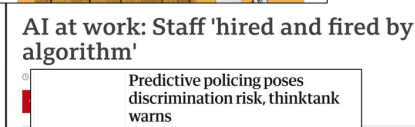
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Are neural networks safer to use?

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Why do we need explanations?

- ▶ **Example-based explanations**
 - ▶ Prototype and criticism (Kim et al. [14])
- ▶ **(Local/Global) Model-agnostic explanations**
 - ▶ SHAP (Lundberg & Lee [16])
 - ▶ LIME (Ribeiro et al. [21])
- ▶ **Counterfactual explanations** (Wachter et al. [29])
- ▶ **Interpretable Models** (e.g., decision trees, linear models)
- ▶ See surveys on the topic (Adabi & Berrada [1])

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These methods mostly target machine learning practitioners and researchers!

Explainability as "right to an explanation"

In reality, a user wants to know how to act to appeal to or change a potentially negative decision.

We need to consider *"explanations as a means to help a data-subject act rather than merely understand"* [29]

It is also defined as a requirement by the GDPR [27]

Definition 1 (Algorithmic Recourse, adapted from [25])

Algorithmic recourse is the systematic process of reversing unfavourable decisions by algorithms and bureaucracies across a range of counterfactual scenarios.

Counterfactual Explanations

Definition 2

A **counterfactual explanation** (CFE) is a statement about “how the world would have (had) to be different for a desirable outcome to happen”.

We are usually interested in **nearest counterfactual explanations**, the most similar instances of the feature vector that change the prediction of the classifier.

Counterfactual Explanations

$$\mathbf{x} := \{x_0, \dots, x_n\} \quad x \in \mathcal{X}$$

$$h : \mathcal{X} \rightarrow \{0, 1\}$$

$$d : \mathcal{X} \times \mathcal{X} \rightarrow \mathbb{R}$$

Counterfactual Explanations

$$\begin{aligned}\mathbf{x} &:= \{x_0, \dots, x_n\} \quad x \in \mathcal{X} \\ h &: \mathcal{X} \rightarrow \{0, 1\} \\ d &: \mathcal{X} \times \mathcal{X} \rightarrow \mathbb{R}\end{aligned}$$

$$\begin{aligned}\mathbf{x}^* &= \arg \min_{\mathbf{x}'} d(\mathbf{x}, \mathbf{x}') \\ \text{s.t. } & h(\mathbf{x}) \neq h(\mathbf{x}^*)\end{aligned} \tag{1}$$

Counterfactual Explanations

- ▶ CFEs are **model-agnostic**
- ▶ CFEs do not need to be instances from the training data
- ▶ CFEs are **human-friendly** explanations
 - ▶ Both **contrastive** and **selective**
- ▶ CFEs are relatively easy to find (e.g., minimizing a loss function)

Counterfactual Explanations

Wachter et al. [29] provides a loss function to learn CFEs.

$$\mathcal{L}(\mathbf{x}, \mathbf{x}', y', \lambda) = \lambda(h(\mathbf{x}') - y')^2 + d(\mathbf{x}, \mathbf{x}')$$

$$d(\mathbf{x}, \mathbf{x}') = \sum_{i=0}^n \frac{|x'_i - x_i|}{MAD_i} \quad (2)$$

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$$\mathbf{x}^* = \arg \min_{\mathbf{x}' \in \mathcal{X}} \max_{\lambda \in \mathbb{R}} \lambda(h(\mathbf{x}') - y')^2 + d(\mathbf{x}, \mathbf{x}') \quad (3)$$

Counterfactual Explanations

There are already many research works on how to build CFEs:

- ▶ **Multi-objective Counterfactual Explanations** [5]
- ▶ **Counterfactual Explanations under uncertainty** [24]
- ▶ **MACE** (Karimi et al. [13])
- ▶ **LORE** (Guidotti, Monreale, Ruggieri, Pedreschi, et al. [9])
- ▶ **DICE** (Mothilal et al. [17])
- ▶ **FACE** (Poyiadzi et al. [19])
- ▶ Many surveys on the topic. See Guidotti, Monreale, Ruggieri, Turini, et al. [10]

Counterfactual Explanations

- ▶ Given $\mathbf{x} \in \mathcal{X}$, there exists multiple \mathbf{x}^* (Rashomon Effect)
- ▶ CFEs are not **actionable**
- ▶ CFE optimization does not consider the **feasibility**
- ▶ Prior works ignore the **causal relationship** between features.

Counterfactual Interventions

- ▶ Actionable **sequence of actions** instead of a CFE
- ▶ It defines a **cost** to mimic the **user's effort** for each action
- ▶ It considers **causal relationships** between features
- ▶ **Minimize** the cost of the sequence, such that $h(\mathbf{x}) \neq h(\mathbf{x}')$
- ▶ **Same properties** of counterfactual explanations (CFEs).

Counterfactual Interventions II

$$\mathbf{x} := \{x_0, \dots, x_n\} \quad x \in \mathcal{X}$$

$$h : \mathcal{X} \rightarrow \{0, 1\}$$

$$a \in \mathcal{A} \quad C : \mathcal{A} \times \mathcal{X} \rightarrow \mathbb{R}$$

Counterfactual Interventions II

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$$I^* = \arg \min_{I \in \mathcal{I}} \sum_{t=1}^T C(a_t, \mathbf{x}_t)$$

$$\begin{aligned} \text{s.t.} \quad & I^* = \{a_t\}_{t=1}^T \\ & \mathbf{x}_t = I(\mathbf{x}_{t-1}) \\ & h(I(\mathbf{x}_0)) \neq h(\mathbf{x}_0) \end{aligned} \tag{4}$$

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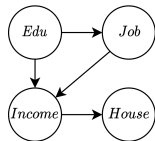
$$h(I(\mathbf{x}_0)) \neq h(\mathbf{x}_0)$$

(4)

Algorithmic Recourse is an **NP-Hard problem**.

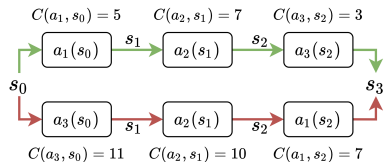
Causality

(A)



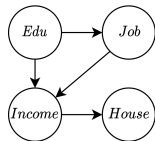
a_1 : get_degree(bachelor)
 a_2 : change_job(developer)
 a_3 : change_house(buy)

(B)



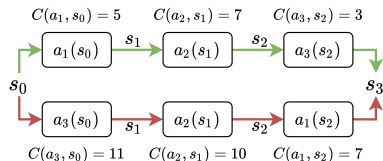
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Theorem 3 (Adapted from 3.2 in [22])

Unless we are intervening on variables without descendants, algorithmic recourse can be guaranteed only if the structural equations are known, no matter the amount or the type of available data.

Counterfactual Interventions

- ▶ **Recourse in linear classification** (Spangher et al. [23])
- ▶ **SYNTH** (Ramakrishnan et al. [20])
- ▶ **CSCF** (Naumann & Ntoutsi [18])
- ▶ **FastAR** (Verma et al. [26])
- ▶ **FARE** (De Toni, Lepri, & Passerini [6])
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$$\begin{aligned}
 & \min_{\mathcal{S}} \left(\underbrace{o_1}_{\text{Sequence cost}}, \underbrace{o_2}_{\text{Gower's distance}}, \underbrace{o_{2+1}, \dots, o_{2+h}, \dots, o_{2+d}}_{\text{Feature tweaking frequencies}} \right) \\
 & \text{s.t. } f(\mathbf{x}_T) = \text{accept} \text{ and } \bigwedge_{(a_i, v_i) \in \mathcal{S}} \mathbb{C}_i
 \end{aligned}$$

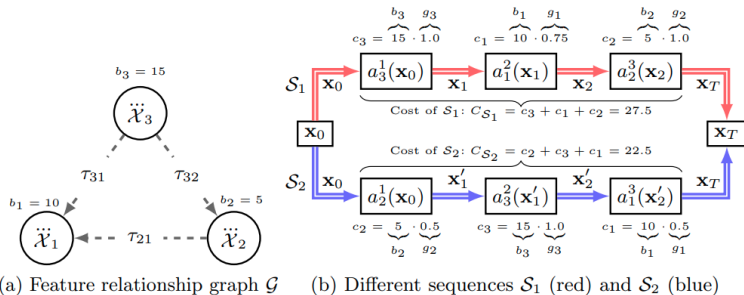


Fig. 2. For simplicity, the $\tau(\cdot)$ functions in (a) are based on binary conditions: $\tau_{32} = 1.0$ if $\mathcal{X}_3 := \text{US}$, else 0.5. $\tau_{31} = 0.5$ if $\mathcal{X}_3 := \text{US}$, else 1.0. $\tau_{21} = 0.5$ if $\mathcal{X}_2 \geq \text{BSc}$, else 1.0. As a reference, the action efforts b_i are provided above each feature in (a).

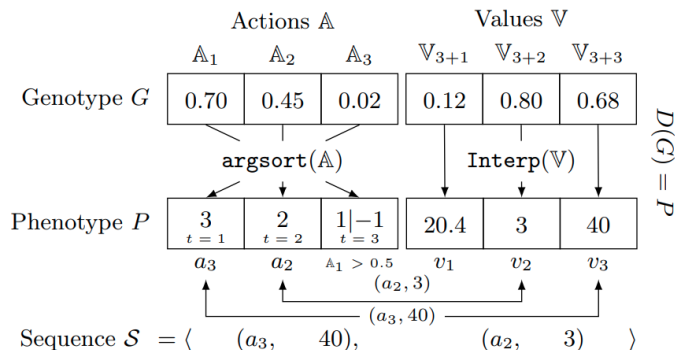


Fig. 3. Anatomy and representation of the solution decoding.

CSCF (Naumann & Ntoutsi [18])

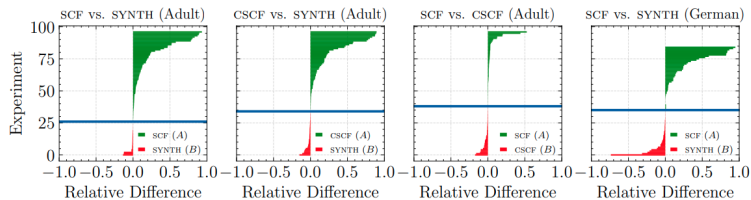


Fig. 4. Relative minimal sequence cost (σ_1) differences between the three methods for both datasets and solutions with $T \leq 2$. It is computed as: $(B - A) / \max\{A, B\}$.

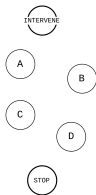
Counterfactual Interventions

- ▶ Current methods rely on **optimization techniques**
- ▶ **Run them ex-novo** for each user (might be a costly process)
- ▶ Fail to explain **why** we are suggesting each intervention (Barocas et al. [2])
- ▶ **Limitations of CFE-based recourse** (Karimi et al. [12])

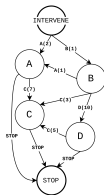
FARE (De Toni, Lepri, & Passerini [6])

Explainable Program Training Phase

1. Add nodes



2. Add transitions

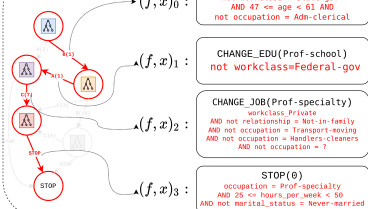


3. Train decision trees



Inference Phase

4. Predict



- ▶ **Jointly train end-to-end models providing both predictions and interventions.** See VCNet (Guyomard et al. [11])

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- ▶ **Human-in-the-Loop Counterfactual Intervention Generation.** Eliciting user preferences over the actions (De Toni, Viappiani, et al. [7])

Future Directions

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- ▶ **Validation with real-users of counterfactual interventions** See "One counterfactual does not make an explanation" (Butz et al. [3])

Future Directions

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- ▶ **Validation with real-users of counterfactual interventions** See "One counterfactual does not make an explanation" (Butz et al. [3])
- ▶ **Fairness of Algorithmic Recourse.** See "On the fairness of causal algorithmic recourse" (von Kügelgen et al. [28]).

Questions?

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