

# Logics for Data and Knowledge Representation: 12th September 2014

NAME ..... SURNAME ..... STUDENT ID.....

1. [6 PT] Say (mark with an X) whether the following statements are true (T) or false (F).

a) Venn diagrams cannot be used to prove the satisfiability of a DL ALC formula w.r.t. a TBox.	<input type="checkbox"/> T <input type="checkbox"/> F
b) In syntactic matching a similarity measure between the nodes of the two graphs is computed by comparing their labels	<input type="checkbox"/> T <input type="checkbox"/> F
c) In a lightweight ontology there are is-a and part-of relations	<input type="checkbox"/> T <input type="checkbox"/> F
d) In RDFS, properties are defined with respect to the classes of the resources they can be attached to	<input type="checkbox"/> T <input type="checkbox"/> F
e) SPARQL forbids RDF Literals as the subject of RDF triples	<input type="checkbox"/> T <input type="checkbox"/> F
f) OWL DL is more expressive than OWL Lite while guarantees conclusions and decidability	<input type="checkbox"/> T <input type="checkbox"/> F

2. [3 PT] Provide the formal semantics of propositional DL in terms of a class valuation and formally explain what it means for a propositional DL formula to be satisfiable.

$$\sigma(\perp) = \emptyset$$

$$\sigma(\top) = U \text{ (Universal Class, or Universe)}$$

$$\sigma(P) \subseteq U, \text{ as defined by } \sigma$$

$$\sigma(\neg P) = \{a \in U \mid a \notin \sigma(P)\} = \text{comp}(\sigma(P)) \text{ (Complement)}$$

$$\sigma(P \sqcap Q) = \sigma(P) \cap \sigma(Q) \text{ (Intersection)}$$

$$\sigma(P \sqcup Q) = \sigma(P) \cup \sigma(Q) \text{ (Union)}$$

### Satisfiability:

Let  $\sigma$  be a class-valuation on language L, we define the truth-relation (or class-satisfaction relation)  $\models$  and write  $\sigma \models P$  (read:  $\sigma$  satisfies P) iff  $\sigma(P) \neq \emptyset$

3. [5 PT] Translate the following natural language sentences in DL language with lowest expressiveness possible (e.g. AL, ALC, FL0...) and say which of the languages you used:
- A parent is a person having at least one natural child or an adopted child
  - Monkeys are animals which are disjoint from Lions
  - The friend of a policeman cannot be a criminal
  - Facebook users can only post photos about their friends
  - Germans do not have Italian friends and friends having Italian friends

PARENT  $\sqsubseteq$  PERSON  $\sqcap$  ( $\exists$ hasNaturalChild. $\top$   $\sqcup$   $\exists$ hasAdoptedChild. $\top$ ) (ALU)

MONKEY  $\sqsubseteq$  ANIMAL  $\sqcap$   $\neg$  LION (AL)

POLICEMAN  $\sqsubseteq$   $\neg$   $\exists$ friendOf.Criminal (ALE)

FACEBOOK-USER  $\sqsubseteq$  USER  $\sqcap$   $\forall$ POST.FRIEND-PHOTO (FL0)

GERMAN  $\sqsubseteq$   $\forall$ friendOf. ( $\neg$  ITALIAN  $\sqcup$   $\neg$   $\exists$  friendOf.ITALIAN) (ALCE)

4. [2 PT] Formally explain the “separation of duties” ReBAC rule with an example in DL

See slides

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5. [3 PT] Formalize the following problem in DL and provide a TBox and ABox as appropriate: “Unicorns are mythical horses having a horn. Pegasus is a unicorn while George is not. Nevertheless, George is a horse”. Provide also a formal proof to demonstrate whether the ABox is consistent with the TBox obtained.

### **TBOX T**

**Unicorn  $\sqsubseteq$  mythical  $\sqcap$  horse  $\sqcap$  hasHorn**

### **ABOX A**

**Unicorn(Pegasus),  $\neg$ Unicorn(George), horse(George)**

**We can check that it is consistent given that the expansion of A w.r.t. T does not contain contradictions. In fact, we have 3 possible expansions of  $\neg$ Unicorn(George):**

**$\neg$ Unicorn(George)  $\Leftrightarrow$   $\neg$  mythical (George) or  $\neg$  horse (George) or  $\neg$  hasHorn(George)**

**Where only the second would generate and contradiction.**

6. [3 PT] Suppose we describe people in an academic environment using DL as follows:

Undergraduate  $\sqsubseteq \neg \text{Teach}$

Bachelor  $\equiv \text{Student} \sqcap \text{Undergraduate}$

Master  $\equiv \text{Student} \sqcap \neg \text{Undergraduate}$

PhD  $\equiv \text{Master} \sqcap \text{Research}$

Assistant  $\equiv \text{PhD} \sqcap \text{Teach}$

Are assistants undergraduates? Provide a proof to answer.

**We need to check whether:**

**$\text{T} \models \text{Assistant} \sqsubseteq \text{Undergraduate}$**

**$\text{Assistant} \equiv \text{PhD} \sqcap \text{Teach} \equiv \text{Master} \sqcap \text{Research} \sqcap \text{Teach} \equiv$**

**$\text{Student} \sqcap \neg \text{Undergraduate} \sqcap \text{Research} \sqcap \text{Teach}$**

**Assistants are actually students who are not undergraduates.**

7. [2 PT] List and provide a brief description of the four basic ABox reasoning services

**See slides**

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8. [3 PT] Given that an RDF model represents information about books and the model is created using standard vocabularies.
- Write a SPARQL query that can return the publishers of the books. Note that books can be represented as URIs.
  - Write a SPARQL query that can return the title and date of publication of the books.

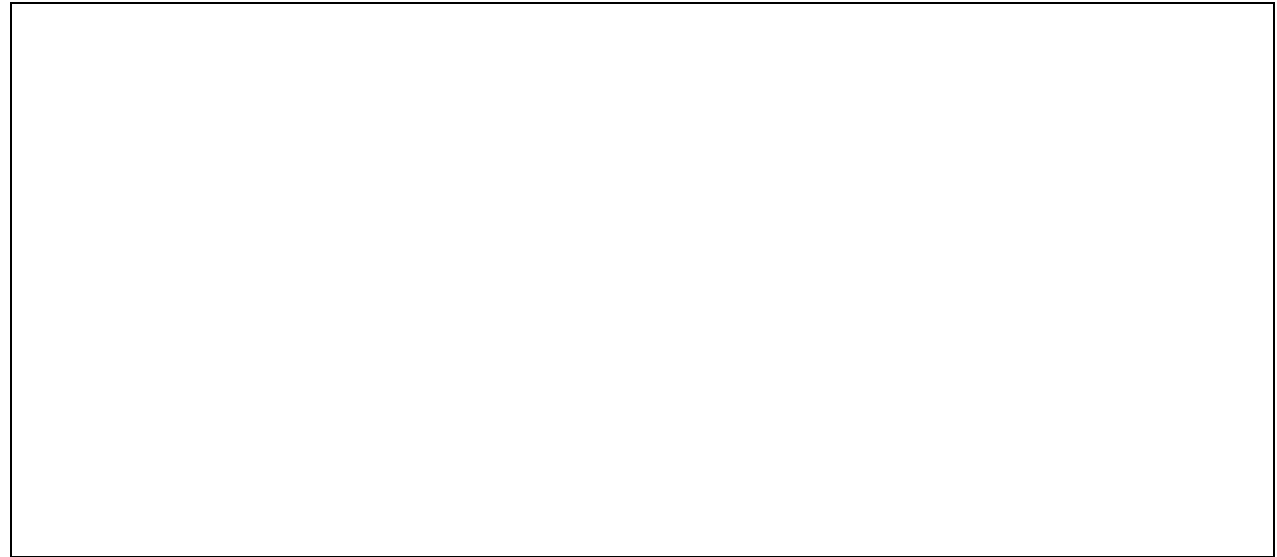
```
i) PREFIX dc: <http://purl.org/dc/elements/1.1/>
   SELECT ?book ?publisher
   WHERE
   { ?book dc:publisher ?publisher }
```

```
ii) PREFIX dc: <http://purl.org/dc/elements/1.1/>
   SELECT ?bookTitle ?dateOfPublication
   WHERE
   { ?book dc:date ?dateOfPublication.
     ?book dc:title ?bookTitle
   }
```

9. [3 PT] What inferences can be drawn from each of the following sets of axioms?

i)	:researcherAt :Benedikt_Elser	rdfs:range :researcherAt	:Italian_University :UniTn
ii)	:Researcher :publishedIn :Fausto_Giunchiglia	rdfs:subClassOf rdfs:domain :publishedIn	:Scientist :Researcher :ISWC_2007_Conference
iii)	:Italian_University :professorshipAt :Fausto_Giunchiglia	rdfs:subClassOf rdfs:range :professorshipAt	:European_University :Italian_University :UniTn

i)	:UniTn	rdf:type	:Italian_University
ii)	:Fausto_Giunchiglia :Fausto_Giunchiglia	rdf:type rdf:type	:Researcher :Scientist
iii)	:UniTn :UniTn	rdf:type rdf:type	:Italian_University :European_University



**10. [3 PT] Provide a comparison among OWL 2 profiles EL, QL and RL, which were specified for different kinds of representation and application needs.**

**See slides**

