

# Computational Linguistics: Semantics II

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# Contents

|     |   |    |
|-----|---|----|
| 1   | Recall: Formal Semantics Main questions ..... | 4  |
| 1.1 | Building Meaning Representations .....        | 5  |
| 1.2 | Lambda-calculus: Functional Application ..... | 6  |
| 2   | Extending the lexicon .....                   | 7  |
| 2.1 | Quantified NP .....                           | 8  |
| 2.2 | Generalized Quantifiers .....                 | 9  |
| 2.3 | Generalized Quantifiers .....                 | 10 |
| 2.4 | Determiners .....                             | 11 |
| 2.5 | Determiners (cont'd) .....                    | 12 |
| 2.6 | Determiners (Cont'd) .....                    | 13 |
| 3   | Ambiguities .....                             | 14 |
| 3.1 | Scope Ambiguities .....                       | 15 |
| 4   | Dependencies .....                            | 16 |
| 4.1 | Relative Pronouns .....                       | 17 |
| 4.2 | Relative Pronoun (Cont'd) .....               | 18 |
| 5   | Summing up: Constituents and Assembly .....   | 19 |
| 6   | Historical Remark: Montague .....             | 20 |

|     |  |    |
|-----|--|----|
| 7   | Inference .....                              | 21 |
| 8   | Inference (Cont'd) .....                     | 22 |
| 9   | The need for semantic representation .....   | 23 |
| 9.1 | Syntactic Representation .....               | 24 |
| 9.2 | Meaning Representation .....                 | 25 |
| 9.3 | Meaning Representation (Cont'd) .....        | 26 |
| 9.4 | Remark .....                                 | 27 |
| 10  | Semantics vs. Knowledge Representation ..... | 29 |
| 11  | Conclusions .....                            | 30 |

# 1. Recall: Formal Semantics Main questions

The main questions are:

1. What does a given sentence mean?
2. How is its meaning built?
3. How do we infer some piece of information out of another?

## 1.1. Building Meaning Representations

To build a meaning representation we need to fulfill three tasks:

**Task 1** Specify a reasonable **syntax** for the natural language fragment of interest.

**Task 2** Specify semantic representations for the **lexical items**.

**Task 3** Specify the **translation** of constituents **compositionally**. That is, we need to specify the translation of such expressions in terms of the translation of their parts, parts here referring to the substructure given to us by the syntax.

Moreover, when interested in Computational Semantics, all three tasks need to be carried out in a way that leads to computational implementation naturally.

## 1.2. Lambda-calculus: Functional Application

Summing up:

- ▶ FA has the form:  $\text{Functor}(\text{Argument})$ . E.g.  $(\lambda x.\text{love}(x, \text{mary}))(\text{john})$
- ▶ FA triggers a very simple operation: Replace the  $\lambda$ -bound variable by the argument. E.g.  $(\lambda x.\text{love}(x, \text{mary}))(\text{john}) \Rightarrow \text{love}(\text{john}, \text{mary})$

Correction of Lab exercise .

## 2. Extending the lexicon

Before we have left open the question of what does an expression like “a” contribute to? FOL does not give us the possibility to express it’s meaning representation. We will see now that instead lambda terms provide us with the proper expressivity.

## 2.1. Quantified NP

- a) Every Mexican student of the EM in CL attends the Comp Ling course.
- b) No Mexican student of the EM in CL attend the Logic course.

a) means that if Sergio and Luis constitute the set of the Mexican students of the EM in CL, then it is true for both of them that they attend the Comp. Ling course.

b) means that for none of the individual members of the set of Mexican student of the EM in CL it is true that he attends the Logic course.

What is the interpretation of “every Mexican student” and of “no Mexican student”?

Individual constants used to denote specific individuals cannot be used to denote quantified expressions like “every man”, “no student”, “some friends”.

Quantified-NPs like “every man”, “no student”, “some friends” are called non-referential.

## 2.2. Generalized Quantifiers

A Generalized Quantifier (GQ) is a set of properties, i.e. **a set of sets-of-individuals**.

For instance, “every man” denotes the set of properties that every man has. The property of “walking” is in this set iff every man walks. For instance,

$$\llbracket \text{man} \rrbracket = \{a, b, c\};$$

$$\llbracket \text{fat} \rrbracket = \{a, b, c, d\};$$

$$\llbracket \text{dog} \rrbracket = \{d\};$$

$$\llbracket \text{run} \rrbracket = \{a, b\};$$

$$\llbracket \text{jump} \rrbracket = \{b, c, d\};$$

$$\llbracket \text{laugh} \rrbracket = \{b, d\};$$

Which is the interpretation of “every man”?

$$\llbracket \text{every man} \rrbracket = \{X \mid \llbracket \text{man} \rrbracket \subseteq X\} = \{\{a, b, c\}, \{a, b, c, d\}\}.$$

## 2.3. Generalized Quantifiers

$$\begin{aligned} \llbracket \text{no man} \rrbracket &= \{X \subseteq E \mid \llbracket \text{man} \rrbracket \cap X = \emptyset\}. \\ \llbracket \text{some man} \rrbracket &= \{X \subseteq E \mid \llbracket \text{man} \rrbracket \cap X \neq \emptyset\}. \\ \llbracket \text{every man} \rrbracket &= \{X \subseteq E \mid \llbracket \text{man} \rrbracket \subseteq X\}. \\ \llbracket \text{man which VP} \rrbracket &= \llbracket \text{man} \rrbracket \cap \llbracket \text{VP} \rrbracket. \end{aligned}$$

Therefore, determiners are as below:

$$\begin{aligned} \llbracket \text{no N} \rrbracket &= \{X \subseteq E \mid \llbracket \text{N} \rrbracket \cap X = \emptyset\}. \\ \llbracket \text{some N} \rrbracket &= \{X \subseteq E \mid \llbracket \text{N} \rrbracket \cap X \neq \emptyset\}. \\ \llbracket \text{every N} \rrbracket &= \{X \subseteq E \mid \llbracket \text{N} \rrbracket \subseteq X\}. \\ \llbracket \text{N which VP} \rrbracket &= \llbracket \text{N} \rrbracket \cap \llbracket \text{VP} \rrbracket. \end{aligned}$$

Generalized quantifiers have attracted the attention of many researchers working on the interaction between logic and linguistics.

New exercises Ex. 5

## 2.4. Determiners

Which is the lambda term representing quantifiers like “nobody”, “everybody”, “a man” or “every student” or a determiners like “a”, “every” or “no” ?

We know how to represent in FOL the following sentences

- ▶ “Nobody left”

$$\neg \exists x. \text{left}(x)$$

- ▶ “Everybody left”

$$\forall x. \text{left}(x)$$

- ▶ “Every student left”

$$\forall x. \text{Student}(x) \rightarrow \text{left}(x)$$

- ▶ “A student left”

$$\exists x. \text{Student}(x) \wedge \text{left}(x)$$

- ▶ “No student left”

$$\neg \exists x. \text{Student}(x) \wedge \text{left}(x)$$

But how do we reach these meaning representations starting from the lexicon?

## 2.5. Determiners (cont'd)

Let's start representing "a man" as  $\exists x.man(x)$ . Applying the rules we have seen so far, we obtain that the representation of "A man loves Mary" is:

$$love(\exists x.man(x), mary)$$

which is clearly wrong.

Notice that  $\exists z.man(z)$  just isn't the meaning of "a man". If anything, it translates the complete sentence "There is a man".

## 2.6. Determiners (Cont'd)

Let's start from what we have, namely “man’ and “loves Mary”:

$\lambda y.man(y)$ ,  $\lambda x.love(x, mary)$ .

Hence, the term representing “a” is:

$$\lambda X.\lambda Y.\exists z.X(z) \wedge Y(z)$$

Try to obtain the meaning representation for “a man”, and the “a man loves Mary”.

By  $\beta$ -conversion twice we obtain that “a man” is  $\lambda Y.\exists z.Man(z) \wedge Y(z)$ , and then  $\exists z.Man(z) \wedge love(z, mary)$

New exercises Ex. 6

### 3. Ambiguities

Starting from:

|  |   |
|--|---|
| john: $j$  | book: $\lambda x(\mathbf{book}(x))$     |
| read: $\lambda x.\lambda y.\mathbf{read}(y, x)$      | didn't: $\lambda X.\lambda y.\neg X(y)$ |
| a: $\lambda X.\lambda Y(\exists x.X(x) \wedge Y(x))$ |   |

Built the meaning representation for “John didn’t read a book”.

a.  $\exists x.\mathbf{book}(x) \wedge \neg\mathbf{read}(j, x)$  [A > NOT]

b.  $\neg\exists x.B(x) \wedge \mathbf{read}(j, x)$  [NOT > A]

► **Scope:** In a. the quantifier phrase (QP), “a book”, has scope over “didn’t” [A > NOT], whereas in b. it has narrow scope [NOT > A].

► **Binding:** the variable  $x$  is bound by “a book” in “John didn’t read a book”.

## 3.1. Scope Ambiguities

Can you think of other expressions that may cause scope ambiguity?

John **think** a student left

Does the student exist or not?

a.  $\exists x.think(j, left(x))$

b.  $think(j, \exists x.left(x))$

## 4. Dependencies

While studying the syntax of natural language, we have seen that important concepts to account for are local and long-distance dependencies.

The  $\lambda$ -operator gives us (more or less) a way to represent this link semantically.

For instance, in  $\lambda x.\lambda y.like(y, x)$  we express that the dependency of the subject and object from the verb.

But the calculus gives us also a natural way to handle long-distance dependencies: eg. relative pronouns.

## 4.1. Relative Pronouns

For instance, “which John read [...]”:

We know how to represent the noun phrase “John” and the verb “read”, namely, as `john` and `λx.y.read(y, x)`.

What is the role of “which” in e.g. “the book which John read is read”?

The term representing “which” has to express the fact that it is replacing the role of a noun phrase in subject (or object position) within a subordinate sentence while being the subject (object) of the main sentence:

$$\lambda X.\lambda Y.\lambda z.X(z) \wedge Y(z)$$

The double role of “which” is expressed by the double occurrence of  $z$ .

## 4.2. Relative Pronoun (Cont'd)

Recall,

$$\lambda X.\lambda Y.\lambda z.X(z) \wedge Y(z)$$

- i. read u:  $\lambda y(\text{read}(y, u))$       ii. John read u:  $\text{read}(j, u)$   
iii. John read:  $\lambda u.\text{read}(j, u)$       iv. which John read:  $\lambda Y.\lambda z.\text{read}(j, z) \wedge Y(z)$

- ▶ at the syntactic level we said that the relative pronoun “which” plays the role of the verb’s object and it leaves a **gap** in the object position.
- ▶ Semantically, the gap is represented by the  $u$  on which the relative pronoun forces the abstraction [iii.] before taking its place.

## 5. Summing up: Constituents and Assembly

Let's go back to the points where FOL fails, i.e. constituent representation and assembly. The  $\lambda$ -calculus succeeds in both:

**Constituents:** each constituent is represented by a lambda term.

John:  $j$  knows:  $\lambda xy.(\text{know}(x))(y)$  read john:  $\lambda y.\text{know}(y, j)$

**Assembly:** function application ( $\alpha(\beta)$ ) and abstraction ( $\lambda x.\alpha[x]$ ) capture **composition** and **decomposition** of meaning representations.

## 6. Historical Remark: Montague

Montague ('74) was the first to seriously propose and defend the thesis that the relation between syntax and semantics in a natural language such as English could be viewed as not essentially different from the relation between syntax and semantics in formal language such as the language of FOL. The framework he developed is known as “Montague’s Universal Grammar” and its main components are:

- ▶ Model-Theory
- ▶ The principle of “Compositionality” which is due to Frege (1879).
- ▶ The  $\lambda$ -calculus which was invented by Church in the 1930’s.
- ▶ Categorical Grammar which is due to Ajdukiewicz ('35) and Bar-Hill ('53). It’s a (context free) Grammar based on functional application.

The novelty of Montagues’ work was to apply them to natural language in a uniform framework.

We will study Categorical Grammar next time.

## 7. Inference

We've said that an important ultimate question in Formal Semantics is “How do we infer some piece of information out of other?”

We have seen how to use logic to represent natural language input.

Therefore the question reduces to the question of “Which are the inference tools for the logic we used?”.

For instance, a tool you already know is the “Tableaux Method” (**Logic** Course by Franconi).

In the **Computational Logic** course (by Martinenghi) you are studying the computational properties of this tool

## 8. Inference (Cont'd)

Inference play a crucial role also at the discourse level. For instance,

“Jon has a rabbit. The tail is white and fluffy”.

“The tail” of whom?

I know that most rabbits have a tail, hence Jon’s rabbit has a tail. Therefore, I can interpret “the tail” to be of Jon’s rabbit.

## 9. The need for semantic representation

We shall also assume a framework in which we are attempting to communicate in natural language with some computer system which has its own internal representation of “knowledge” in some symbolic form.

The natural language front end (NLFE) has to formulate queries, commands and statements in a way that allow appropriate responses to be produced by the “back-end” system.

This can be done in two ways, using:

- ▶ Syntactic Representation
- ▶ Meaning Representation

## 9.1. Syntactic Representation

In this framework, it would be possible in principle to have the syntactic form of an input sentence (i.e. the syntax tree) act directly upon the stored information within the back-end knowledge based system, without any intermediate representations being constructed. That is, the response of the system, whether it be the moving of a robot arm, or the printing out of information, would be computed directly from the syntax tree.

This approach is **rarely followed**, as it leads to unnecessary complications. There are certain regularities about how each natural language expresses information, and there may be several different ways of expressing essentially the same request. If the syntactic tree is directly interpreted, then all the (linguistic) knowledge about these **grammatical variations** (which are irrelevant to the work of the back-end) has to be built-in to the interpreter which controls the back-end responses. Minor alterations to the grammatical coverage of the front-end then necessitate changes to this response-generator.

## 9.2. Meaning Representation

It is therefore normal to have the NLFE formulate its query (or command, or whatever) in some specialised notation for semantic representation, and then pass this on to further levels of the system for processing.

The superficial details of how the request was expressed in English can then be handled by separate linguistic rules, without the back-end having to include such information – the semantic representation of the input is a “canonical form”. (This is a very similar methodological argument to that which supports splitting the earlier phase of processing into two stages, syntax and semantic interpretation).

Much of the research that goes on in NL semantics is concerned with the design of suitable formalisms for this intermediate language.

## 9.3. Meaning Representation (Cont'd)

It is important to note that this intermediate semantic language need not be the same as whatever representation the actual back-end uses to store its knowledge. The semantic representation language is suitable for depicting the content of a sentence (or a sequence of sentences), and for extracting a response from the back-end; the back-end's own formalism, used for storing information, might be completely different. This point is sometimes glossed over in systems which use some very general notation (e.g. logic, Prolog) for both purposes.

## 9.4. Remark

Notice that a system of semantic representation is not just some diagrams or symbolic expressions thrown together in a pleasing or intuitively attractive way. Very simple examples such as representing “John loves Mary” by *love(john, mary)* can sometimes tempt beginners into thinking that a semantic expression is just the words rearranged, with a bit of punctuation thrown in. This is not a viable approach. A semantic representation formalism should have at the very least the following properties:

1. It should be **clearly defined**. That is, there should be an explicit statement of what would qualify as a legal (well-formed) expression in this notation.
2. Its operations/behaviour should be clearly defined. That is, there should be proper definitions of what **inference** or other manipulations can be carried out on these expressions.
3. To justify the term “semantic”, it should be reasonable to argue that the behaviour of these expressions in some way captures the meaning of the corresponding linguistic expressions.

Anything that lacks these fundamental properties cannot be a serious semantic representation, although it might be handy as an informal notation for sketching out one's thoughts, or a visual aid in conveying ideas to other workers.

## 10. Semantics vs. Knowledge Representation

To a large extent, the issues involved in semantics are the same as the more general issues of knowledge representation.

But the two endeavours (semantics and knowledge representation) are not wholly identical, since knowledge representation could well be less constrained in what is acceptable as a solution.

- ▶ For natural language **semantics**, the formalisations chosen should make those **distinctions which are reflected in the natural language involved**, whereas general knowledge representation need make only those distinctions relevant to inference and other processes.
- ▶ The representations used in general **knowledge representation need not be expressible in natural language at all**, but those in semantics have expressibility in language as their entire justification.
- ▶ More particularly, NL semantic representations (and their rules) must have a well-defined interface to actual words, phrases and sentences (the concrete syntax), which is not a requirement for more general knowledge representation.

# 11. Conclusions

Possible projects on topic introduced so far:

## 1. PoS tagging:

- ▶ One person: Read the paper by Eric Brill, “Transformation-Based Error-Driven Learning and NLP: A case study in POS Tagging”. 1995, and right a report on it comparing to other existing pos taggers (state of the art review).
- ▶ Two persons: Besides the above point. Try to implement and test the system on some corpora.

## 2. Morphology:

- ▶ One person: Read about KIMMO and report on it.
- ▶ Two persons: Try to test it too.

## 3. Parsing:

- ▶ One person: Read about PATR (or another parser) and report on it.

- ▶ Two persons: Try to test it too.

#### 4. Semantic:

- ▶ One person: Read the paper by Blackburn and Bos “Computational Semantics” and report on it.
- ▶ Two persons: Try to use lambda in prolog

#### 5. Formal Grammars:

- ▶ One person: Read the paper by Joshi ”Tree-Adjoining Grammars”. In The Oxford Handbook of Computational Linguistics” and report on it.
- ▶ One person: Read about Dependency Grammar (I will give some material)

#### 6. Dialogue: TO BE DECIDED.

(i) Always try to search for other relevant literature, (ii) describe the problem addressed (iii) and the solution proposed in the paper, and (iv) try to comment about advantages and disadvantages of it.

Projects could also be combined if you want to work in bigger teams.