Computational Linguistics: Syntax II

RAFFAELLA BERNARDI

KRDB, FREE UNIVERSITY OF BOZEN-BOLZANO P.ZZA DOMENICANI, ROOM: 2.28, E-MAIL: BERNARDI@INF.UNIBZ.IT

Contents

1	Summ	ary	5
2	Today	's topics	6
3		nent	7
	3.1	First try	8
	3.2	Loss of efficiency	9
	3.3	Second Try	10
	3.4	Second try (cont'd)	11
	3.5	Loss of generalization	12
	3.6	Feature Pergolation	13
	3.7	Set of properties	14
4	Constr	aint Based Grammars	15
5	Featur	e Structures	16
6	Agreer	nent Feature	18
7		e Path	19
	7.1	Directed Graphs	20
	7.2	Reentrancy	21
	7.3	Reentrancy as Coindexing	22

	7.4	FS: Sub	sumption	23
	7.5	Examples		
	7.6	Exercis	e	25
	7.7	Exercis	e: (Cont'd)	26
8	Opera	tions on	FS	27
	8.1	Unificat	tion of FS	28
		8.1.1	Partial Operation	29
		8.1.2	Unification: Formal Definition	30
		8.1.3	Similarity with set operations	31
		8.1.4	Exercises	32
		8.1.5	Exercises: Reentrancy	33
		8.1.6	Exercise: Empty feature structure	34
	8.2	Genera	lization	35
	8.3	Genera	lization: Formal Definition	37
	8.4	Unificat	tion vs. Generalization	38
9	Augm	enting C	FG with FS	39
10	Augm	enting C	FG wiht FS (cont'd)	40
	10.1	Exercis	e	41
	10.2	Head F	eatures and Subcategorization	42

	10.3	Schema	44
	10.4	Example	44
11	Concl	usion	45
12	Pract	ical Info	46

1. Summary

The main issues of this morning lecture are:

- ▶ Syntax: Constituents; Head; Dependencies.
- ▶ NL Syntax cannot be formalized by RL.
- ▶ CFG can be used to recognize NL syntax, but
- overgeneration (agreement) and undergeneration (long-distance dependencies) problems.

2. Today's topics

Today, we will see how to

- ▶ use features to account for agreement,
- ▶ represent complex feature structures, and
- ▶ augment CFG with these feature structures.

3. Agreement

When working with agreement a first important fact to be taken into account is that we use

- ▶ a plural VP if and only if we have a plural NP, and
- ▶ a singular VP if and only if we have a singular NP.

For instance,

- 1. "the gangster dies"
- 2. *"the gangster die"

That is, we have to distinguish between singular and plural VPs and NPs.

3.1. First try

One way of doing this would be to **invent new non-terminal symbols** for plural and singular NPs and VPs. Our grammar would then look as follows.

We would have two rules for building sentences: one for building a sentence out of a singular NP (NPsg) and a singular VP (VPsg), and the other one for using a plural NP (NPpl) with a plural VP (VPpl).

Singular NPs are built out of a determiner and a singular noun (Nsg) and plural NPs are built out of a determiner and a plural noun (Npl). Note that we don't have to distinguish between singular and plural determiners as we are only using "the" at the moment, which works for both.

Similarly, singular VPs are built out of singular intransitive verbs (IVsg) and plural VPs out of plural intransitive verbs (IVpl).

Finally, we have singular and plural nouns and verbs in our lexicon.

3.2. Loss of efficiency

Now, the grammar does what it should:

- 1. "the gangster dies" 2. "the gangsters die"
- 3. *"the gangster die" 4. *"the gangsters dies".

However, compared to the grammar we started with, it has become **huge** – we have twice as many phrase structure rules, now. And we only added the information whether a noun phrase or a verb phrase is plural or singular.

Imagine we next wanted to add transitive verbs and pronouns. To be able to correctly accept "he shot him" and reject "him shot he", we would need case information in our grammar. And if we also wanted to add the pronouns "I" and "you", we would further have to distinguish between first, second and third person.

If we wanted to code all this information in the non-terminal symbols of the grammar, we would need non-terminal symbols for all combinations of these features. Hence, the **size of the grammar would explode** and the rules would probably become very difficult to read.

3.3. Second Try

We use features to represent case (subject, object), gender (female, masculine), number (singular, plural).

```
s --> np(subj), vp.
vp --> vt, np(obj).
vp --> vi.
np(CASE) --> pro(CASE).
np(_) --> det, n.
np(_) --> pn.
Lexicon
det --> the
n --> whiskey
pn --> bill
pro(subj) --> he
pro(obj) --> him
vi --> fights
vt --> kills
```

Try the second exercise.

3.4. Second try (cont'd)

While doing the exercise, you might have noticed that the extra argument — the feature — is simply **passed up the tree** by ordinary **unification**. And, depending on whether it can correctly unify or not, this feature controls the facts of English case avoiding duplications of categories.

Summing up,

- ▶ features let us get rid of lots of unnecessary rules in a natural way.
- ▶ In the lab we will see that PROLOG enables us to implement rules with feature information in a natural way.

This way of handling features however has some limits, in particular it does not provide an adequate syntax descriptions of the agreement phenomena in general terms.

3.5. Loss of generalization

Both strategies misses some important generalizations.

In the extended grammar above, for example, the non-terminals NPsg and NPpl are not more similar to each other than to say VPsg. The generalization that they are both NPs is lost. Similarly, the information that sentence are always built out of a noun phrase and a verb phrase (although their number can vary) is lost in the first try.

So, what we would like to say is something like this:

"Sentences consist of an NP and a VP. They must both be of the same number; either plural or singular."

Moreover, the properties we might need to speak about are many.

3.6. Feature Pergolation

Last time we have spoken of the **head** of the phrase as the word characterizing the phrase itself. E.g. the head of a noun phrase is the noun, the head of a verb phrase is the verb, the head of a prepositional phrase is the preposition, etc.

Notice that its the head of a phrase that **provides the features of the phrase**. E.g. in the noun phrase "this cat", it's the noun ("cat") that characterizes the np as singular.

Note, this also means that the noun requires the article to match its features.

3.7. Set of properties

This can be captured in an elegant way, if we say that our **non-terminals are** no longer atomic category symbols, but a **set of properties**, such as type of category, number, person, case

Certain rules can then impose **constraints** on the individual properties that a category involved in that rule may have.

These constraints can force a certain property to have **some specific value**, but can also just say that two properties must have the **same value**, no matter what that value is. Using this idea, we could specify our grammar like this:

```
s ---> np vp : number of np= number of vp
np ---> Det n : number of np= number of n
vp ---> iv
Det ---> the
n ---> gangster : number of n= singular
n ---> gangsters : number of n= plural
iv ---> dies: number of iv = singular
iv ---> die : number of iv = plural
```

4. Constraint Based Grammars

In computational linguistics such sets of properties are commonly represented as feature structures.

The grammars that use them are known as **constraint-based** grammars, i.e. grammars that can express **constrains on the properties** of the categories to be combined by means of its rules. Roughly, a rule would have to say

$s \to np \ vp$

only if the number of the np is equal to the number of the vp.

The most well known Constraint Based Grammars are Lexical Functional Grammar (LFG, Bresnan '82), Generalized Phrase Structure Grammar (GPSG, Gazdar et al. '85), Head-driven Phrase Structure Grammar (HPSG, Pollard and Sag, '87), Tree Adjoining Grammar (TAG, Joshi et al. '91).

5. Feature Structures

Constraints-Based Grammars usually encode properties by means of **Feature Structures** (FS). They are simply sets of feature-value pairs, where features are unalayzable atomic symbols drown from some finite set, and values are either atomic symbols or feature structures.

They are traditionally illustrated with the following kind of matrix-like diagram, called **attribute-value matrix (AVM)**:

${f Feature}_1 \ {f Feature}_2$	$Value_1$ $Value_2$
\dots Feature $_n$	\dots Value _n

For instance, the number features ${\tt sg}$ (singular) and ${\tt pl}$ plural, are represented as below.

 $\left[\begin{array}{ccc} \texttt{NUM} & sg\end{array}\right] \quad \left[\begin{array}{ccc} \texttt{NUM} & pl\end{array}\right]$

Contents First Last Prev Next \triangleleft

Similarly, the slightly more complex feature 3rd singular person is represented as

$$\begin{bmatrix} \text{NUM} & sg \\ \text{PERS} & 3 \end{bmatrix}$$

Next, if we include also the category we obtain, e.g.

$$\begin{bmatrix} CAT & np \\ NUM & sg \\ PERS & 3 \end{bmatrix}$$

which would be the proper representation for "Raffaella" and would differ from the FS assigned to "they" only with respect to (w.r.t.) the number.

Therefore, FS give a way to encode the information we need to take into consideration in order to deal with **agreement**. In particular, we obtain a way to encode the constraints we have seen before.

6. Agreement Feature

In the above example all feature values are atomic, but they can also be feature structures again. This makes it possible to group features of a common type together.

For instance, the two important values to be considered for agreement are NUM and PERS, hence we can group them together in one AGR feature obtaining a more compact and efficient representation of the same information we expressed above.

$$\left[\begin{array}{ccc} \operatorname{CAT} & np \\ & \operatorname{AGR} & \left[\begin{array}{cc} \operatorname{NUM} & sg \\ & \operatorname{PERS} & 3 \end{array}\right] \end{array}\right]$$

Given this kind of arrangement, we can test for the equality of the values for both NUM and PERS features of two constituents by testing for the equality of their AGR features.

7. Feature Path

A $Feature \ Path$ is a list of features through a FS leading to a particular value. For instance, in the FS below

$$\begin{bmatrix} \text{CAT} & np \\ & \text{AGR} & \begin{bmatrix} \text{NUM} & sg \\ & \text{PERS} & 3 \end{bmatrix} \end{bmatrix}$$

the $\langle \texttt{AGR NUM} \rangle$ path leads to the value sg, while the $\langle \texttt{AGR PERS} \rangle$ path leads to the value 3.

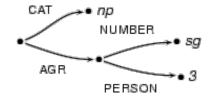
This notion of paths brings us to an alternative graphical way of illustrating FS, namely directed graphs.

7.1. Directed Graphs

Another common way of representing feature structures is to use directed graphs. In this case, values (no matter whether atomic or not) are represented as nodes in the graph, and features as edge labels. Here is an example. The attribute value matrix

$$\left[\begin{array}{cc} \texttt{CAT} & np \\ \texttt{AGR} & \left[\begin{array}{c} \texttt{NUM} & sg \\ \texttt{PERS} & 3 \end{array}\right] \end{array}\right]$$

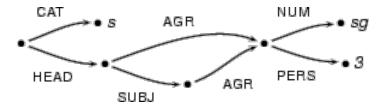
can also be represented by the following directed graph.



Paths in this graph correspond to sequences of features that lead through the feature structure to some value. The path carrying the labels AGR and NUM corresponds to the sequence of features $\langle AGR, NUM \rangle$ and leads to the value sg.

7.2. Reentrancy

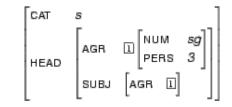
The graph that we have just looked at had a tree structure, i.e., there was no node that had more than one incoming edge. This need not always be the case. Look at the following example:



Here, the paths $\langle \text{Head}, \text{AGR} \rangle$ and $\langle \text{Head}, \text{SUBJ}, \text{AGR} \rangle$ both lead to the same node, i.e., they lead to the same value and share that value. This property of feature structures that several features can share one value is called **reentrancy**. It is one of the reasons why feature structures are so useful for computational linguistics.

7.3. Reentrancy as Coindexing

In attribute value matrices, reentrancy is is commonly expressed by coindexing the values which are shared. Written in the matrix notation the graph from above looks as follows. The **boxed 1** indicates that the two features sequences leading to it **share the value**.



7.4. **FS**: Subsumption

We have said that feature structures are essentially sets of properties. Given two different sets of properties an obvious thing to do is to **compare the information they contain**.

A particularly important concept for comparing two feature structures is **subsump-tion**.

A feature structure F1 subsumes (\sqsubseteq) another feature structure F2 iff all the information that is contained in F1 is also contained in F2.

7.5. Examples

The following two feature structures for instance subsume each other.

[NUM	sg	[PERS	3]
PERS	3	NUM	sg

They both contain exactly the same information, since the order in which the features are listed in the matrix is not important.

7.6. Exercise

And how about the following two feature structures?

$$\left[\begin{array}{cc} \texttt{NUM} & sg \end{array}\right] \quad \left[\begin{array}{cc} \texttt{PERS} & 3\\ \texttt{NUM} & sg \end{array}\right]$$

Well, the first one subsumes the second, but not vice versa. Every piece of information that is contained in the first feature structure is also contained in the second, but the second feature structure contains additional information.

7.7. Exercise: (Cont'd)

Do the following feature structures subsume each other?

Γ	NUM	sg	PERS	3]
	GENDER	masc	L NUM	sg

The first one doesn't subsume the second, because it contains information that the second doesn't contain, namely GENDER masc.

But, the second one doesn't subsume the first one either, as it contains PERS 3 which is not part of the first feature structure.

8. Operations on **FS**

The two principal operations we need to perform of FS are **merging** the information content of two structures and **rejecting** the merger of structures that are incompatible.

A single computational technique, namely **unification**, suffices for both of the purposes.

Unification is implemented as a binary operator that accepts two FS as arguments and returs a FS when it succeeds.

8.1. Unification of **FS**

Unification is a (partial) operation on feature structures. Intuitively, it is the operation of combining two feature structures such that the new feature structure contains **all the information of the original two, and nothing more**. For example, let F1 be the feature structure

$$\left[\begin{array}{ccc} \texttt{CAT} & np \\ \texttt{AGR} & \left[\begin{array}{c} \texttt{NUM} & sg \end{array}\right] \end{array}\right]$$

and let F2 be the feature structure

CAT	np	·
AGR	PERS	3]

Then, what is $F1 \sqcup F2$, the unification of these two feature structures?

$$\begin{bmatrix} \text{CAT} & np \\ & \text{AGR} & \begin{bmatrix} \text{NUM} & sg \\ & \text{PERS} & 3 \end{bmatrix} \end{bmatrix}$$

8.1.1. Partial Operation Why did we call unification a **partial operation**? Why didn't we just say that it was an operation on feature structures?

The point is that unification is not guaranteed to return a result. For example, let F3 be the feature structure

$$\begin{bmatrix} CAT & np \end{bmatrix}$$

and let F4 be the feature structure

$\begin{bmatrix} \text{CAT} & vp \end{bmatrix}$

Then $F3 \sqcup F4$ does not exist. There is no feature structure that contains all the information in F3 and F4, because the information in these two feature structures is contradictory. So, the value of this unification is undefined.

8.1.2. Unification: Formal Definition Those are the basic intuitions about unification, so let's now give a precise definition. This is easy to do if we make use of the idea of subsumption, which we discussed above.

The unification of two feature structures F and G (if it exists) is the smallest feature structure that is subsumed by both F and G. That is, (if it exists) $F \sqcup G$ is the feature structure with the following three properties:

- 1. $F\sqsubseteq F\sqcup G$ ($F\sqcup G$ is subsumed by F)
- 2. $G \sqsubseteq F \sqcup G$ ($F \sqcup G$ is subsumed by G)
- 3. If H is a feature structure such that $F \sqsubseteq H$ and $G \sqsubseteq H$, then $F \sqcup G \sqsubseteq H$ ($F \sqcup G$ is the smallest feature structure fulfilling the first two properties. That is, there is no other feature structure that also has properties 1 and 2 and subsumes $F \sqcup G$.)

If there is no smallest feature structure that is subsumed by both F and G, then we say that the unification of F and G is **undefined**.

8.1.3. Similarity with set operations The subsumption relation on feature structures can be thought of as analogous to the subset relation on sets.

Similarly, **unification** is rather like an analog of **set-theoretic union** (recall that the union of two sets is the smallest set that contains all the elements in both sets).

But there is a difference: union of sets is an operation (that is, the union of two sets is always defined) whereas (as we have discussed) unification is only a **partial operation** on feature structures.

8.1.4. Exercises Now that the formal definition is in place, let's look at a few more examples of feature structure unification. First, let F5 be

$$\left[\begin{array}{ccc} \operatorname{AGR} & \left[\begin{array}{c} \operatorname{NUM} & sg \end{array}\right] \\ \operatorname{SUBJ} & \left[\begin{array}{c} \operatorname{AGR} & \left[\begin{array}{c} \operatorname{NUM} & sg \end{array}\right] \end{array}\right] \end{array}\right]$$

and let F6 be the feature structure

```
\left[\begin{array}{cc} \text{SUBJ} & \left[\begin{array}{cc} \text{AGR} & \left[\begin{array}{cc} \text{PERS} & 3 \end{array}\right] \end{array}\right]
```

What is the result of $F5 \sqcup F6$?

$$\begin{bmatrix} \text{AGR} & \begin{bmatrix} \text{NUM} & sg \end{bmatrix} \\ \text{SUBJ} & \begin{bmatrix} \text{AGR} & \begin{bmatrix} \text{NUM} & sg \\ \text{PERS} & 3 \end{bmatrix} \end{bmatrix}$$

8.1.5. Exercises: Reentrancy Next, an example involving reentrancies. Let F7 be

What is then $F7 \sqcup F6$?



8.1.6. Exercise: Empty feature structure What happens if one of the feature structures we are trying to unify is the empty feature structure [] — that is, the feature structure containing no information at all?

Pretty clearly, for any feature structure F, we have that:

 $F \sqcup [] = [] \sqcup F = F$

That is, the empty feature structure is the identity element for the (partial) operation on feature structure unification. That is, the empty feature structure behaves like the empty set in set theory (recall that the union of the empty set with any set Sis just S).

8.2. Generalization

Generalization can be thought of as an analog of the **set-theoretic operation of intersection**. Recall that the intersection of two sets is the set that contains only the elements common to both sets. Similarly, the generalization of two feature structures contains only the information that is common to both feature structures.

For example, let F9 be

AGR	NUM PERS	$\begin{bmatrix} pl \\ 3 \end{bmatrix}$
ARITY	3	

and let $F10~{\rm be}$

AGR	NUM	pl
	PERS	1]
L ARITY	1	J

What is then $F9 \sqcap F10$, the generalization of F and G?

$\left[\begin{array}{cc} \texttt{AGR} & \left[\begin{array}{cc} \texttt{NUM} & pl \end{array} \right] \end{array} \right]$

Clearly $F9 \sqcap F10$ contains only information which can be found in both F and G.

8.3. Generalization: Formal Definition

Here's a precise definition of generalization: The generalization of two feature structures F and G is the largest feature structure that subsumes both F and G. That is, $F \sqcap G$ is the feature structure with the following three properties:

- 1. F \sqcap G \sqsubseteq F
- 2. F \sqcap G \sqsubseteq G
- 3. If H is a feature structure such that $H \sqsubseteq F$ and $H \sqsubseteq G$, then $H \sqsubseteq F \sqcup G$.

8.4. Unification vs. Generalization

There is an important difference between unification and **generalization**: unlike unification, generalization is **an operation** on feature structures, not just a partial operation. That is, **the generalization of two features is always defined**.

Think about it. Consider the worst case — two feature structures F and G that contain no common information at all. Is there a largest feature structure that subsumes both? Of course there is — the empty feature structure []!

Thus, from a mathematical perspective, generalization is somewhat easier to work with than unification. Nonetheless, it is not used nearly so often in computational linguistics as unification is, so we won't discuss how to implement it.

9. Augmenting CFG with FS

We have seen that agreement is necessary, for instance, between the np and vp: they have to agree in number in order to form a sentence.

The basic idea is that non-terminal symbols no longer are atomic, but are feature structures, which specify what properties the constituent in question has to have. So, instead of writing the (atomic) non-terminal symbols s, vp, np, we use feature structures CAT where the value of the attribute is s, vp, np. The rule becomes

 $[\texttt{CAT} \ s] \to [\texttt{CAT} \ np] \ [\texttt{CAT} \ vp]$

That doesn't look so exciting, yet.

10. Augmenting CFG wiht FS (cont'd)

But what we can do now is to add further information to the feature structures representing the non-terminal symbols. We can, e.g., add the information that the **np** must have nominative case:

$$\begin{bmatrix} \mathsf{CAT} & s \end{bmatrix} \to \begin{bmatrix} \mathsf{CAT} & np \\ \mathsf{CASE} & nom \end{bmatrix} \begin{bmatrix} \mathsf{CAT} & vp \end{bmatrix}$$

Further, we can add an attribute called NUM to the np and the vp and require that the values be shared. Note how we express this requirement by co-indexing the values.

$$\begin{bmatrix} \mathsf{CAT} & s \end{bmatrix} \to \begin{bmatrix} \mathsf{CAT} & np \\ \mathsf{CASE} & nom \\ \mathsf{NUM} & \blacksquare \end{bmatrix} \begin{bmatrix} \mathsf{CAT} & vp \\ \mathsf{NUM} & \blacksquare \end{bmatrix}$$

10.1. Exercise

Try to build a feature based grammar for the (tiny) fragment of English below. Lexicon

```
det --> a
det --> the
n --> bride
n --> whiskey
pn --> bill
pn --> gogo
pro(subj) --> he
pro(subj) --> she
pro(obj) --> him
pro(obj) --> her
vi --> whistles
vi --> fights
vt --> drinks
vt --> kills
```

10.2. Head Features and Subcategorization

We have seen that to "put together" words to form constituents two important notions are the "head" of the constituent and its dependents (also called the arguments the head subcategorize for).

In some constraints based grammars, e.g. HPSG, besides indicating the category of a phrase, FS are used also to sign the head of a phrase and its arguments.

In these grammars, the CAT (category) value is an object of sort category (cat) and it contains the two attributes HEAD (head) and SUBCAT (subcategory).

Head Recall, the features are percolated from one of the children to the parent. The child that provides the features is called the **head** of the phrase, and the features copied are referred to as head features. Therefore, the HEAD value of any sign is always unified with that of its phrasal projections.

Subcategorization The notion of subcategorization, or valence, was originally designed for verbs but many other kinds of words exhibit form of valence-like behavior. This notion expresses the fact that such words determine which patterns of argument they must/can occur with. They are used to express **dependencies**. For instance,

- 1. an intransitive verb subcategorizes (requires) a subject.
- 2. a transitive verb requires two arguments, an object and a subject.

3. . . .

Other verbs

- ▶ want [to see a girl called Evelyn]_{Sto}
- ▶ asked $[him]_{NP}$ [whether he could make it]_{sif}

10.3. Schema

Schematically the subcategorization is represented as below.

 $\left[\begin{array}{cc} {\rm ORTH} & word \\ {\rm CAT} & category \\ {\rm HEAD} & \left[\begin{array}{c} {\rm SUBCAT} & \left< 1st \ required \ argument, 2nd \ required \ argument, \ldots \right> \end{array} \right] \end{array}\right]$

10.4. Example

For instance, the verb "want" would be represented as following

 $\left[\begin{array}{ccc} \text{ORTH} & want \\ \text{CAT} & verb \\ \text{HEAD} & \left[\begin{array}{ccc} \text{SUBCAT} & \langle [\text{CAT} & np], \left[\begin{array}{ccc} \text{CAT} & vp \\ \text{HEAD} & [\text{VFORM} INFINITIVE] \end{array} \right] \rangle \end{array} \right] \end{array} \right]$

11. Conclusion

The model of subcategorization we have described so far helps us solving the overgeneration problem described this morning. However, we still have to see how to deal with long-distance dependencies.

We will return to this in November.

Not done on FS:

- 1. Implementing Unification
- 2. Parsing with Unification Constraints
- 3. Types and Inheritance

Projects 1, and 2 are possible topics for projects. Another possible project on today topic is to build a Constraint Based for a fragment of a language of your choice. Wednesday, we will look at parsing techniques. Then we move to semantics and discourse.

12. Practical Info

Topics for projects

- ▶ Morphology analyzer (FST).
- ▶ PoS Tagging.
- ▶ Formal Grammars: build a CFG for a fragment of a language of your choice.
- ► Formal Grammars: CFG+FS implementation: (programming languages?).
- ► Semantics: extending CFG with lambda calculus (Prolog).
- ▶ Semantics: underspecification.

Make up your mind by the 21st of October –when we have covered all these topics already.