

# Real Time Operating Systems and Middleware

## *Sensitivity Analysis*

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# Considerations on WCET

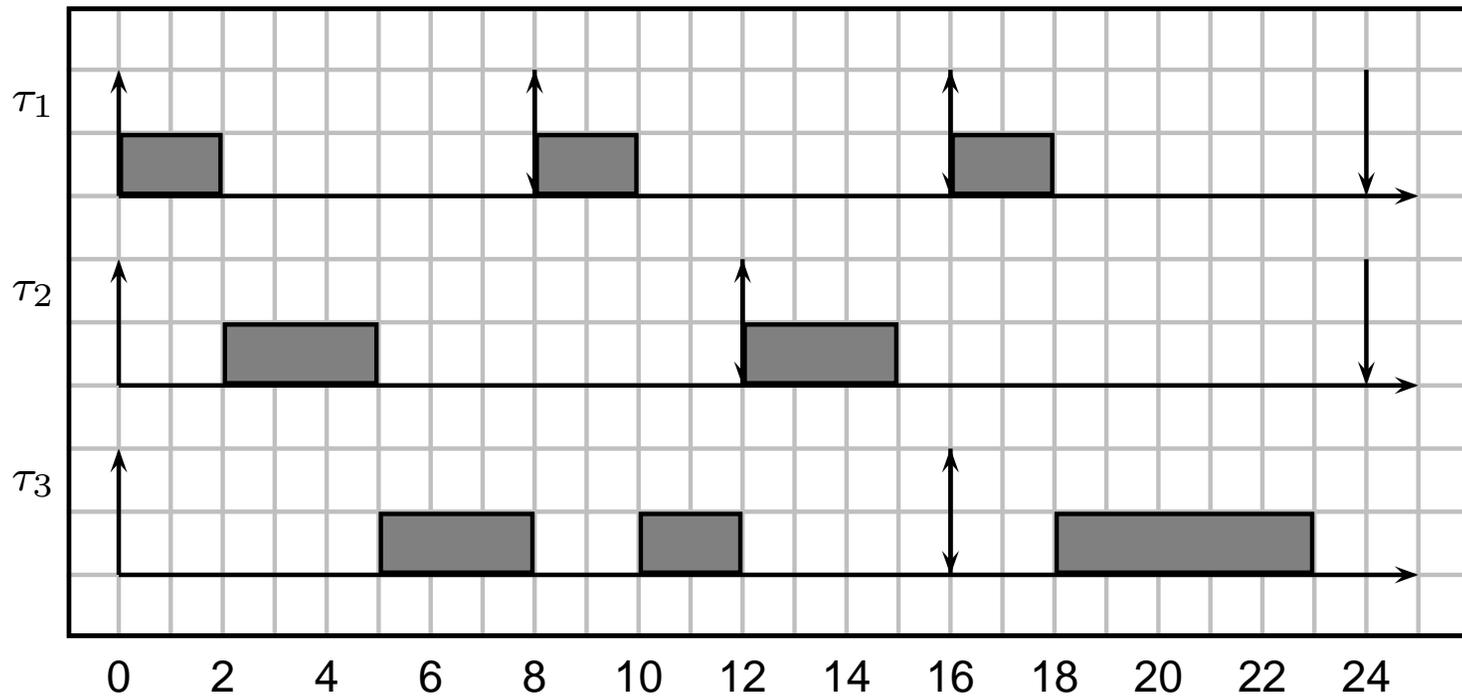
- Both response time analysis and time demand analysis provide a necessary and sufficient schedulability test for fixed priority scheduling
- However, the result is *very* sensitive to the value of the WCET
  - If we are wrong in estimating the WCET (and for example we use a value that is too small), the actual system may be not schedulable
  - For example, in response time analysis a *small* increase in the WCET of a higher priority task makes the response time *jump* to much larger values

# Sensitivity to WCET

- We can formulate response time computation or demanded time computation as a sensitivity analysis problem
- How sensible is the response time (or the demanded time) to variations in the WCET?
- Because in the ceilings ( $\lceil \cdot \rceil$ ) contained in the equations used to compute  $R_i$  and  $L_i$ , the answer is not simple...
  - For example, for response time we have a function  $R_i = f_i(C_1, T_1, C_2, T_2, \dots, C_{i-1}, T_{i-1}, C_i)$  that is non-continuous
  - What happens to  $R_i$  if a WCET  $C_h$  is increased by a small amount  $\delta$ ?

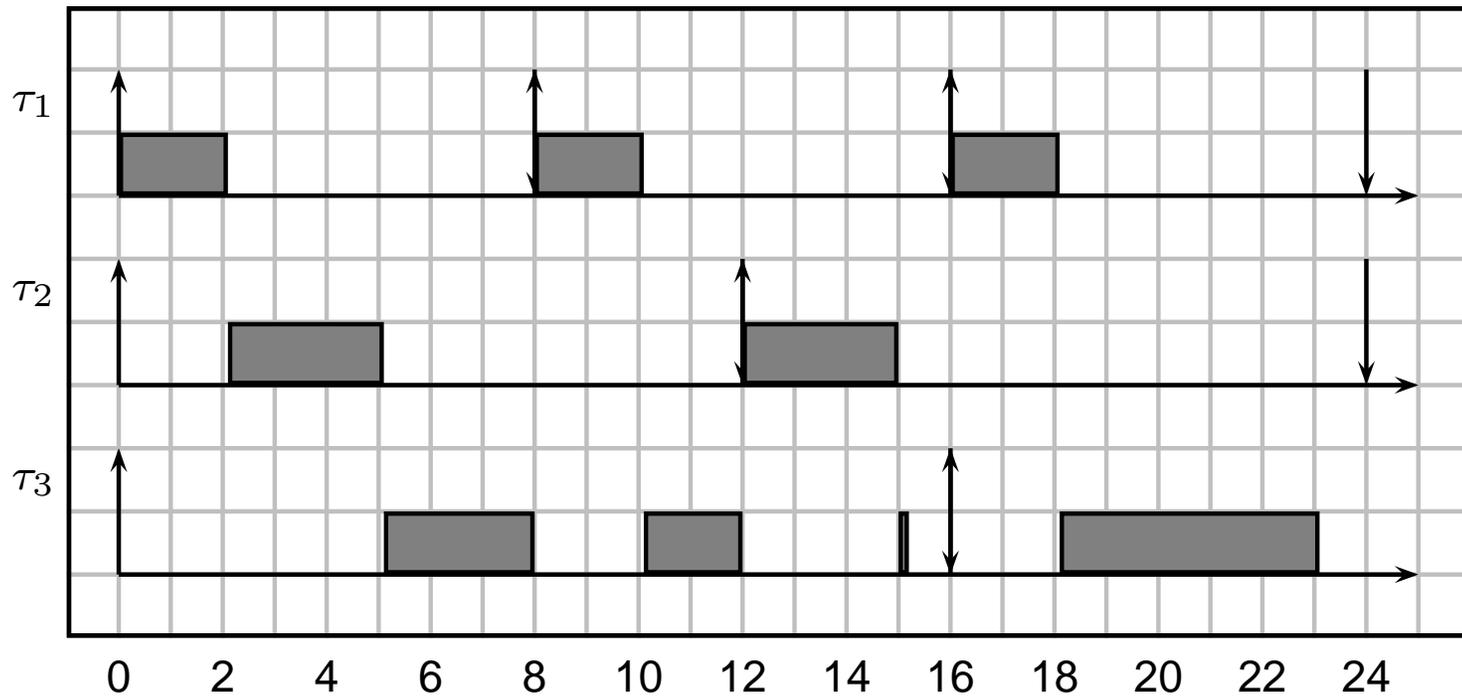
# Example of Discontinuity

- Let's consider again one of the previous examples
- $\mathcal{T} = \{(2, 8), (3, 12), (5, 16)\}$



# Example of Discontinuity

- Let's consider again one of the previous examples
- Increase  $C_1$  by 0.1



$$R_3 = 12 \rightarrow 15.2$$

# What Happened?

- Why did a small increase in  $C_1$  (from 2 to 2.1) cause such a big difference in  $R_3$  (from 12 to 15.2)?
- Let's analyse the problem from the beginning...
  - The response time of a job  $J_{i,j}$  depends on its finishing time  $f_{i,j}$
  - $J_{i,j}$  must be finished, and all the jobs preempting it (from higher priority tasks  $\tau_h | h < i$ ) must be completed
- After  $J_{i,j}$ 's completion,
  - Either a lower priority task  $\tau_j$  ( $p_j < p_i$ ) is scheduled
  - Or the system becomes idle
  - Or a higher priority task  $\tau_h$  arrives immediately ( $f_{i,j} = r_{h,k}$ )

# Singularities

- If the finishing time  $f_{i,j}$  of a job is equal to the arrival time of a job for a higher priority task, time  $t = f_{i,j}$  is called  $i$ -level singularity point
- In the previous example, time  $t = 12$  is a 3-level singularity point, because:
  1. Task  $\tau_3$  has just finished
  2. And task  $\tau_2$  has just been activated

$$f_{3,1} = r_{2,2}$$

- As we have just seen, a singularity is a “dangerous” point!
- In presence of a  $i$ -level singularity point, increasing  $C_h$  (with  $h < i$ ) can generate “strange” effects

# Sensitivity on WCETs

- A rule of thumb is to increase the WCET by a certain percentage before doing the analysis. If the task set is still feasible, be are more confident about the schedulability of the original system.
- There are analytical methods for computing the amount of variation that it is possible to allow to a task's WCET without compromising the schedulability:
  - The analysis looks for possible singularities and computes the amount of time that is needed to obtain a singularity;
  - The analysis is very complex (NP-Hard) but can be done in a few seconds (at most minutes) on a fast computer.