
1 CFL

Let $G = (\{S, A, B, a, b\}, \{a, b\}, S, P)$ where P consists of:

G1 $S \rightarrow AB, A \rightarrow ab, B \rightarrow bb$

G2 $S \rightarrow AB, S \rightarrow aA, A \rightarrow a, B \rightarrow ba$

G3 $S \rightarrow AB, S \rightarrow AA, A \rightarrow aB, A \rightarrow ab, B \rightarrow b$

G4 $S \rightarrow aS, S \rightarrow Sb, S \rightarrow$

G5 $S \rightarrow aS, S \rightarrow A, A \rightarrow bA, A \rightarrow$

(a) find the languages generated by G1, G2 (at home G3)

(b) Construct a derivation of a^2b^4 using G4 (at home G5).

(c) Build the parse trees of a^2b^4 using G4 (at home G5.)

2 CFG

Construct CFGs generating each of the following languages:

1. $L_1 = a^n b^m a^n$ ($0 \leq n, 1 \leq m$)

2. $L_2 = a^n b^n a^m b^m$ ($1 \leq n, m$) (at home)

3 CFG and NL

Write a grammar that recognizes the language (viz. all the sentences) below.

1. Jonh left
2. Jonh knows Mary
3. I will leave Boston in the morning
4. Everybody likes Boston
5. A student likes Boston
6. John gave Mary a red shirt
7. John saw a man with a telescope (at home)

Construct their derivations.