Distributional Semantics

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Acknowledgments

Credits: Some of the slides of today lecture are based on earlier DS courses taught by Marco Baroni, Stefan Evert, Aurelie Herbelot, Alessandro Lenci, and Roberto Zamparelli.

Recall: Frege and Wittgenstein

Frege:

- 1. Linguistic signs have a reference and a sense:
 - (i) "Mark Twain is Mark Twain" [same ref. same sense]
 - (ii) "Mark Twain is Samuel Clemens". [same ref. diff. sense]
- 2. Both the sense and reference of a sentence are built compositionaly.

Lead to the Formal (or Denotational) Semantics studies of natural language that focused on "meaning" as "reference". [Seen last time]

Wittgenstein's claims brought philosophers of language to focus on "meaning" as "sense" leading to the "language as use" view.

Content vs. Grammatical words

The "language as use" school has focused on content words meaning. vs. Formal semantics school has focused mostly on the grammatical words and in particular on the behaviour of the "logical words".

- content words: are words that carry the content or the meaning of a sentence and are open-class words, e.g. noun, verbs, adjectives and most adverbs.
- grammatical words: are words that serve to express grammatical relationships with other words within a sentence; they can be found in almost any utterance, no matter what it is about, e.g. such as articles, prepositions, conjunctions, auxiliary verbs, and pronouns.

Among the latter, one can distinguish the **logical words**, viz. those words that correspond to logical operators

Recall: Formal Semantics: reference

The main questions are:

- 1. What does a given *sentence* mean?
- 2. How is its meaning built?
- 3. How do we infer some piece of information out of another?

Logic view answers: The meaning of a sentence 1. is its truth value, 2. is built from the meaning of its words; 3. is represented by a FOL formula, hence inferences can be handled by logic entailment. Moreover,

- The meaning of words is based on the *objects* in the domain it's the set of entities, or set of pairs/triples of entities, or set of properties of entities.
- Composition is obtained by function-application and abstraction
- Syntax guides the building of the meaning representation.

Distributional Semantics: sense

The main questions have been:

- 1. What is the sense of a given word?
- 2. How can it be induced and represented?
- 3. How do we relate word senses (synonyms, antonyms, hyperonym etc.)?

Well established answers:

- 1. The sense of a word can be given by its use, viz. by the *contexts* in which it occurs;
- 2. It can be induced from (either raw or parsed) corpora and can be represented by *vectors*.
- 3. *Cosine similarity* captures synonyms (as well as other semantic relations).

Distributional Semantics

pioneers

- 1. Intuitions in the '50:
 - Wittgenstein (1953): word usage can reveal semantics flavor (context as physical activities).
 - Harris (1954): words that occur in similar (linguistic) context tend to have similar meanings.
 - Weaver (1955): co-occurrence frequency of the context words near a given target word is important for WSD for MT.
 - Firth (1957): "you shall know a word by the company it keeps"
- 2. Deerwster et al. (1990): put these intuitions at work.

The distributional hypothesis in everyday life

McDonald & Ramscar (2001)

- He filled the wampimuk with the substance, passed it around and we all drunk some
- We found a little, hairy wampimuk sleeping behind the tree

Just from the contexts a human could guess the meaning of "wampimuk".

Distributional Semantics

weak and strong version: Lenci (2008)

- Weak: a quantitative method for semantic analysis and lexical resource induction
- Strong: A cognitive hypothesis about the form and origin of semantic representations

Distributional Semantics

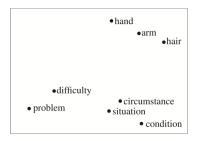
Main idea in a picture: The sense of a word can be given by its use (context!).

hotels . 1. God of the morning star 5. How does your garden , or meditations on the morning star . But we do , as a matte sing metaphors from the morning star , that the should be pla ilky Way appear and the morning star rising like a diamond be and told them that the morning star was up in the sky , they ed her beauteous as the morning star , Fixed in his purpose g star is the brightest morning star . Suppose that ' Cicero radise on the beam of a morning star and drank it out of gold ey worshipped it as the morning star , and certain animals su

flower , He lights the evening star . " Daisy 's eyes filled he planet they call the evening star , the morning star . Int fear it . The punctual evening star , Worse , the warm hawth of morning star and of evening star . And the fish worship t are Fair sisters of the evening star . But wait -- if not tod ie would shine like the evening star . But Richardson 's own na . As the morning and evening star , the planet Venus was u l appear as a brilliant evening star , a star has also been d il it reappears as an ' evening star ' at the end of May . Tr

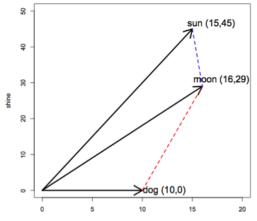
It's a quadruple $\langle B, A, S, V \rangle$, where:

- ► *B* is the set of "basis elements" the dimensions of the space.
- A is a lexical association function that assigns co-occurrence frequency of words to the dimensions.
- V is an optional transformation that reduces the dimensionality of the semantic space.
- S is a similarity measure.



Toy example: vectors in a 2 dimensional space

- $B = \{shadow, shine, \}; A = co-occurrency frequency;$
- S: Euclidean distance. Target words: "moon", "sun", and "dog".





Two dimensional space representation

 \overrightarrow{moon} =(16,29), \overrightarrow{sun} = (15,45), \overrightarrow{dog} =(10,0) together in a space representation (a matrix dimensions × target-words):

16	15	10
29	45	0

The most commonly used representation is the transpose matrix (A^{T}): target-words \times dimensions:

	shine	shadow
moon	16	29
sun	15	45
dog	10	0

The dimensions are also called "features" or "context".

A distributional cat (from the British National Corpus)

0.124 pet-N 0.123 mouse-N 0.099 rat-N 0.097 owner-N 0.096 dog-N 0.092 domestic-A 0.090 wild-A 0.090 duck-N 0.087 tail-N 0.084 leap-V 0.084 prey-N 0.083 breed-N 0.080 rabbit-N 0.078 female-A 0.075 fox-N 0.075 basket-N 0.075 animal-N 0.074 ear-N 0.074 chase-V 0.074 smell-V

0.074 tiger-N 0.073 jump-V 0.073 tom-N 0.073 fat-A 0.071 spell-V 0.071 companion-N 0.070 lion-N 0.068 breed-V 0.068 signal-N 0.067 bite-V 0.067 spring-V 0.067 detect-V 0.067 bird-N 0.066 friendly-A 0.066 odour-N 0.066 hunting-N 0.066 ghost-N 0.065 rub-V 0.064 predator-N 0.063 pig-N

0.063 hate-V 0.063 asleep-A 0.063 stance-N 0.062 unfortunate-A 0.061 naked-A 0.061 switch-V 0.061 encounter-V 0.061 creature-N 0.061 dominant-A 0.060 black-A 0.059 chocolate-N 0.058 giant-N 0.058 sensitive-A 0.058 canadian-A 0.058 toy-N 0.058 milk-N 0.057 human-N 0.057 devil-N 0.056 smell-N

0.115 english-N 0.114 written-A 0.109 grammar-N 0.106 translate-V 0.102 teaching-N 0.097 literature-N 0.096 english-A 0.096 acquisition-N 0.095 communicate-V 0.093 native-A 0.089 everyday-A 0.088 learning-N 0.084 meaning-N 0.083 french-N 0.082 description-N 0.079 culture-N 0.078 speak-V 0.078 foreign-A 0.077 classroom-N 0.077 command-N

0.075 teach-V 0.075 communication-N 0.074 knowledge-N 0.074 polish-A 0.072 speaker-N 0.071 convey-V 0.070 theoretical-A 0.069 curriculum-N 0.068 pupil-N 0.068 level-A 0.067 assessment-N 0.067 use-N 0.067 tongue-N 0.067 medium-N 0.067 spanish-A 0.066 speech-N 0.066 learn-V 0.066 interaction-N 0.065 expression-N 0.064 sign-N

0.064 universal-A 0.064 aspect-N 0.064 german-N 0.063 artificial-A 0.063 logic-N 0.061 understanding-N 0.061 official-A 0.061 formal-A 0.061 complexity-N 0.060 gesture-N 0.060 african-A 0.060 eq-A 0.060 express-V 0.059 implication-N 0.058 distinction-N 0.058 barrier-N 0.057 cultural-A 0.057 literary-A 0.057 variation-N

0.129 chocolate-N 0.122 slice-N 0.109 tin-N 0.109 pie-N 0.103 sandwich-N 0.103 decorate-V 0.099 cream-N 0.098 fruit-N 0.097 recipe-N 0.097 bread-N 0.096 oven-N 0.094 birthdav-N 0.090 wedding-N 0.087 sugar-N 0.086 cheese-N 0.086 tea-N 0.085 butter-N 0.085 eat-V 0.084 apple-N 0.083 wrap-V

0.083 sweet-A 0.081 mix-N 0.080 mixture-N 0.079 rice-N 0.078 nut-N 0.076 tomato-N 0.076 knife-N 0.075 potato-N 0.075 oz-N 0.075 cook-N 0.075 top-V 0.074 coffee-N 0.073 christmas-N 0.073 ice-N 0.073 orange-N 0.073 layer-N 0.072 packet-N 0.072 roll-N 0.071 brush-V 0.071 meat-N

0.071 salad-N 0.071 piece-N 0.070 line-V 0.070 dry-V 0.069 round-A 0.068 egg-N 0.068 cooking-N 0.066 lb-N 0.066 fat-N 0.064 top-N 0.063 spread-V 0.063 chip-N 0.063 cut-V 0.062 sauce-N 0.062 turkev-N 0.061 milk-N 0.061 plate-N 0.060 remaining-A 0 060 hint-N

0.093 coloured-A 0.092 paper-N 0.089 stroke-N 0.089 margin-N 0.089 tip-N 0.085 seize-V 0.077 pig-N 0.077 ltd-A 0.076 drawing-N 0.074 electronic-A 0.072 concrete-A 0.072 portrait-N 0.071 sheep-N 0.068 pocket-N 0.066 code-N 0 066 flow-V 0.066 gardener-N 0.066 sheet-N 0.066 straw-N 0.066 outline-N

0.065 pick-V 0.065 co-N 0.064 palm-N 0.064 writing-N 0.064 jean-N 0.064 literary-A 0.063 writer-N 0.063 write-V 0.063 script-N 0.063 ash-N 0.062 desk-N 0.062 elegant-A 0.061 pause-V 0.061 brush-N 0.060 marine-A 0.060 infant-N 0.059 tape-N 0.059 collapse-N 0.058 cry-N 0.057 delighted-A 0.057 hand-V 0.057 phil-N 0.056 wilson-N 0.056 silver-N 0.056 terror-N 0.055 lower-V 0.055 tap-V 0.055 light-A 0.055 packet-N 0.055 load-V 0.054 cigarette-N 0.054 anxiety-N 0.054 program-N 0.054 complex-N 0.054 ball-N 0.053 rabbit-N 0.053 precious-A 0.052 ea-A 0.052 thanks-N

The components of distributional representations

- Contexts: other words in the close vicinity of the target (*eat, mouse, sleep*), or syntactic/semantic relations (*eat(x), chase(x,mouse), like(x,sleep)*).
- Weights: usually a measure of how characteristic the context is for the target (e.g. Pointwise Mutual Information).
- A semantic space: a vector space in which dimensions are the contexts with respect to which the target is expressed. The target word is a vector in that space (vector components are given by the weights of the distribution).

The notion of context

- Context: if the meaning of a word is given by its context, what does 'context' mean?
 - Word windows (unfiltered): n words on either side of the lexical item under consideration (unparsed text).
 Example: n=2 (window of size 2):

... the prime minister acknowledged that ...

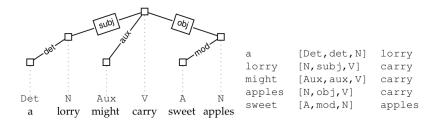
Word windows (filtered): n words on either side of the lexical item under consideration (unparsed text). Some words are not considered part of the context (e.g. function words, some very frequent content words). The stop list for function words is either constructed manually, or the corpus is POS-tagged.

Example: n=2 (window of size 2):

... the prime minister acknowledged that ...

The notion of context

Dependencies: syntactic or semantic. The corpus is converted into a list of directed links between heads and dependents. Context for a lexical item is the dependency structure it belongs to. The length of the dependency path can vary according to the implementation (Padó and Lapata, 2007).



Parsed vs unparsed data: examples

word (unparsed)

meaning_n derive_v dictionary_n pronounce_v phrase_n latin_j ipa_n verb_n mean_v hebrew_n usage_n literally_r

word (parsed)

or_c+phrase_n and_c+phrase_n syllable_n+of_p play_n+on_p etymology_n+of_p portmanteau_n+of_p and_c+deed_n meaning_n+of_p from_p+language_n pron_rel_+utter_v for_p+word_n in_p+sentence_n

Context weighting

Binary model: if context c co-occurs with word w, value of vector w for dimension c is 1, 0 otherwise.

... [a long long long **example** for a distributional semantics] model... (n=4)

... {a 1} {dog 0} {long 1} {sell 0} {semantics 1}...

Basic frequency model: the value of vector w for dimension c is the number of times that c co-occurs with w.

... [a long long long **example** for a distributional semantics] model... (n=4)

... {a 2} {dog 0} {long 3} {sell 0} {semantics 1}...

Context weighting

- Characteristic model: the weights given to the vector components express how *characteristic* a given context is for w. Functions used include:
 - Pointwise Mutual Information (PMI):

$$pmi_{wc} = \log \frac{p(x, y)}{p(x)p(y)} = \log(\frac{f_{wc} * f_{total}}{f_w * f_c})$$
(1)

Derivatives such PPMI, PLMI, etc.

What semantic space?

Entire vocabulary.

- + All information included even rare, but important contexts
- Inefficient (100,000s dimensions). Noisy (e.g. 002.png—thumb—right—200px—graph_n)
- Top n words with highest frequencies.
 - + More efficient (5000-10000 dimensions). Only 'real' words included.
 - May miss out on infrequent but relevant contexts.

What semantic space?

- Singular Value Decomposition (LSA Landauer and Dumais, 1997): the number of dimensions is reduced by exploiting redundancies in the data. A new dimension might correspond to a generalisation over several of the original dimensions (e.g. the dimensions for *car* and *vehicle* are collapsed into one).
 - + Very efficient (200-500 dimensions). Captures generalisations in the data.
 - SVD matrices are not interpretable.
- Other, more esoteric variants...

Corpus choice

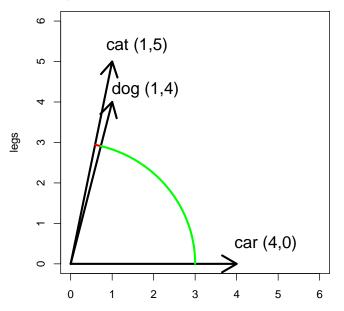
As much data as possible?

- British National Corpus (BNC): 100 m words
- Wikipedia: 897 m words
- UKWac: 2 bn words

▶ ...

- In general preferable, but:
 - More data is not necessarily the data you want.
 - More data is not necessarily realistic from a psycholinguistic point of view. We perhaps encounter 50,000 words a day. BNC = 5 years' text exposure.

Similarity measure: Angle



Similarity measure: cosine similarity

Cosine is the most common similarity measure in distributional semantics. The similarity of two words is computed as the cosine similarity of their corresponding vectors \vec{x} and \vec{y} or, equivalently, the cosine of the angle between \vec{x} and \vec{y} is:

$$cos(\vec{x}, \vec{y}) = rac{\vec{x}}{|\vec{x}|} \cdot rac{\vec{y}}{|\vec{y}|} = rac{\sum_{i=1}^{n} x_i y_i}{\sqrt{\sum_{i=1}^{n} x_i^2} \sqrt{\sum_{i=1}^{n} y_i^2}}$$

- x_i is the weight of dimension *i* in *x*.
- y_i is the the weight of dimension *i* in *y*.
- ► $|\vec{x}|$ and $|\vec{y}|$ are the lengths of \vec{x} and \vec{y} . Hence, $\frac{\vec{x}}{|x|}$ and $\frac{\vec{y}}{|y|}$ are the normilized (unit) vectors.

Cosine ranges from 1 for parallel vectors (perfectly correlated words) to 0 for orthogonal (perpendicular) words/vectors.

In sum: Building a DSM The "linguistic" steps

> Pre-process a corpus (to define targets and contexts) \Downarrow Select the targets and the contexts

The "mathematical" steps

Count the target-context co-occurrences ↓ Weight the contexts (optional, but recommended) ↓ Build the distributional matrix ↓ Reduce the matrix dimensions (optional) ↓ Compute the vector distances on the (reduced) matrix

Corpus pre-processing

- Minimally, corpus must be tokenized
- POS tagging, lemmatization, dependency parsing...
- Trade-off between deeper linguistic analysis and
 - need for language-specific resources
 - possible errors introduced at each stage of the analysis
 - more parameters to tune

different pre-processing - Nearest neighbours of walk

tokenized BNC

- stroll
- walking
- walked
- ► go
- path
- drive
- ride
- wander
- sprinted
- sauntered

lemmatized BNC

- hurry
- stroll
- stride
- trudge
- amble
- wander
- walk-nn
- walking
- retrace
- scuttle

different window size - Nearest neighbours of dog

2-word window in BNC

- cat
- horse
- fox
- pet
- rabbit
- pig
- animal
- mongrel
- sheep
- pigeon

30-word window in BNC

- kennel
- puppy
- pet
- bitch
- terrier
- rottweiler
- canine
- cat
- to bark
- Alsatian

Syntagmatic relations uses

Syntagmatic relations as (a) context-filtering functions: only those words that are linked to the targets by a certain relation are selected, or as (b) context-typing functions: relation define the dimensions. E.g.:

"A dog bites a man. A man bites a dog. A dog bites a man."

		dog	man
(a) window-based	bite	3	3
(b) dependency based	bite _{sub}	2	1
	bite _{obj}	1	2

- (a) Dimension-filtering based on (a1) window: e.g. Rapp, 2003, Infomap NLP; (a2) dependency: Padó & Lapata 2007.
- (b) Dimension-typing based on (b1) window: HAL; (b2) dependency: Grefenstette 1994, Lin 1998, Curran & Moens 2002, Baroni & Lenci 2009.

Evaluation on Lexical meaning

Developers of semantic spaces typically want them to be "general-purpose" models of semantic similarity

- Words that share many contexts will correspond to concepts that share many attributes (*attributional similarity*), i.e., concepts that are taxonomically similar:
 - Synonyms (*rhino/rhinoceros*), antonyms and values on a scale (*good/bad*), co-hyponyms (*rock/jazz*), hyper- and hyponyms (*rock/basalt*)
- Taxonomic similarity is seen as the fundamental semantic relation, allowing categorization, generalization, inheritance
- Evaluation focuses on tasks that measure taxonomic similarity

Evaluation on Lexical meaning

synonyms

DSM captures pretty well synonyms. DSM used over TOEFL test:

- ► Foreigners average result: 64.5%
- Macquarie University Staff (Rapp 2004):
 - Ave. not native speakers: 86.75%
 - Ave. native speakers: 97.75%
- DM:
 - DM (dimension: words): 64.4%
 - Padó and Lapata's dependency-filtered model: 73%
 - Rapp's 2003 SVD-based model trained on lemmatized BNC: 92.5%
- Direct comparison in Baroni and Lenci 2010
 - Dependency-filtered: 76.9%
 - Dependency-typing: 75.0%
 - Co-occurrence window: 69.4%

Evaluation on Lexical meaning

Other classic semantic similarity tasks

Also used for:

- The Rubenstein/Goodenough norms: modeling semantic similarity judgments
- The Almuhareb/Poesio data-set: clustering concepts into categories
- The Hodgson semantic priming data
- Baroni & Lenci 2010: general-purpose model for:
 - concept categorization (car ISA vehicle),
 - selectional preferences (eat chocolate vs *eat sympathy),
 - relation classification (exam-anxiety CAUSE-EFFECT relation),
 - salient properties (car-wheels).
 - ▶ ...

Distributional semantics in 2016

Linguistic representation:

disambiguation, adjective semantics, quantifiers, phrasal composition, *meaning* of words.

Cognitive representa-

tion: simulates language acquisition, priming, fMRI measurements.

Useful hack: representation of the lexicon for NLP applications.

A cognitive representation: Possible Topics for projects

- Landauer & Dumais (1997): knowledge acquisition.
- Lund, Burgess & Atchley (1995): priming.
- Anderson et al (2013): multimodal distributional representations simulate brain activation.

Do distributions model meaning?

A model of word meaning:

- Cats are robots from Mars that chase mice.
- Dogs are robots from Mars that chase cats.
- Trees are 3D holograms from Jupiter.
- A similarity-based evaluation of this model would find that cats and dogs are very similar, but both are much less similar to trees.
- A good model of language?

Do distributions model meaning?

- A theory of meaning has to say how language relates to the world. For instance, model-theoretic semantics says that the meaning of *cat* is the set of all cats in a world.
- In distributionalism, meaning is the way we use words to talk *about* the world. No metaphysical assumptions.
- So if we use the words 'robots from Mars' to talk about cats, all is fine (see whales and fish).

Some online softwares

- To query already built distributional semantics spaces: http://clic.cimec.unitn.it/infomap-query/
- To build semantic spaces http: //clic.cimec.unitn.it/composes/toolkit/
- Semantic space based on distributional similarity and Latent Semantic Analysis (LSA), further complemented with semantic relations extracted from WordNet: http://swoogle.umbc.edu/SimService/

From counting co-occurrences to predicting the word Skip-Gram (T. Mikolov)

Nowadays most renowned model Word2Vec. Main change: From counting co-occourences to predict the word in the context.

Word2Vec

Word2vec is a particularly computationally-efficient predictive model for learning word embeddings from raw text. It comes in two flavors:

- the Skip-Gram model: predicts source context-words from the target words [better for larger datasets]
- the Continuous Bag-of-Words model (CBOW): predicts target words (e.g. 'mat') from source context words ('the cat sits on the')
 [useful for smaller datasets]

Word2Vec

Skip-Gram

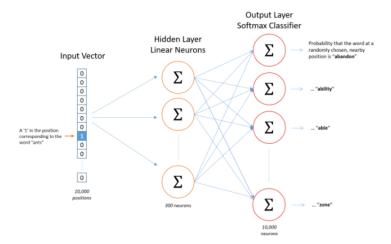
Given a specific word in the middle of a sentence (the input word), look at the words nearby and pick one at random. The network is going to tell us the probability for every word in our vocabulary of being the nearby word that we chose.

- 1. build the vocabulary, e.g .10K unique words
- 2. each word is represented as a "one-hot vector": 10K-d, all 0 and one 1.
- 3. output: a 10K-d vector whose value are the probability that a randomly selected nearby word is that vocabulary word.

When training this network on word pairs, the input is a one-hot vector representing the input word and the training output is also a one-hot vector representing the output word. But when you evaluate the trained network on an input word, the output vector will actually be a probability distribution

Word2Vec

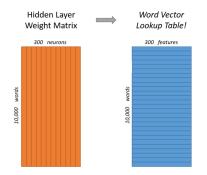
Skip-Gram: architecture



Word2Vec: Skip-Gram

Word Vectors

E.g., we are learning word vectors with 300 features. So the hidden layer is going to be represented by a weight matrix with 10K rows (one for every word in our vocabulary) and 300 columns (one for every hidden neuron).



If you look at the rows of this weight matrix, these are actually what will be our *word vectors* (or *word embeddings*)!

Online query tool

- Snaut http://meshugga.ugent.be/snaut/. It allows to measure semantic distance between words or documents and explore distributional semantics models through a convenient interface.
- Available count/predict spaces: http://clic.cimec. unitn.it/composes/semantic-vectors.html

References

Tutorials

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Conclusion

- Distributional semantics is one possible semantic theory, which has experimental support – both in linguistics and cognitive science.
- Various models for distributional systems, with various consequences on the output.
- Known issues: corpus-dependence (which notion of concept is at play here?), word senses are collapsed (perhaps not such a bad thing...), fixed expressions create noise in the data.

Conclusion

- Evaluation against psycholinguistic data shows that DS can model at least *some* phenomena.
- A powerful computational semantics tool, with surprising results.
- But a tool without a fully-fledged theory...

Applications

- IR: Semantic spaces might be pursued in IR within the broad topic of "semantic search"
- DSM as supplementary resource in e.g.,:
 - Question answering (Tomás & Vicedo, 2007)
 - Bridging coreference resolution (Poesio et al., 1998, Versley, 2007)
 - Language modeling for speech recognition (Bellegarda, 1997)
 - Textual entailment (Zhitomirsky-Geffet and Dagan, 2009)

Conclusion

So far

The main questions have been:

- 1. What is the sense of a given word?
- 2. How can it be induced and represented?
- 3. How do we relate word senses (synonyms, antonyms, hyperonym etc.)?

Well established answers:

- 1. The sense of a word can be given by its use, viz. by the *contexts* in which it occurs;
- 2. It can be induced from (either raw or parsed) corpora and can be represented by *vectors*.
- 3. *Cosine similarity* captures synonyms (as well as other semantic relations).

Conclusion

Next time

- Can vectors representing phrases be extracted too?
- What about compositionality of word sense?
- How do we "infer" some piece of information out of another?

Vector Space

A vector space is a mathematical structure formed by a collection of vectors: objects that may be added together and multiplied ("scaled") by numbers, called scalars in this context.

Vector an n-dimensional vector is represented by a column:

$$\begin{bmatrix} v_1 \\ \cdots \\ v_n \end{bmatrix}$$

or for short as $\vec{v} = (v_1, \dots, v_n)$.

Operations on vectors

Vector addition:

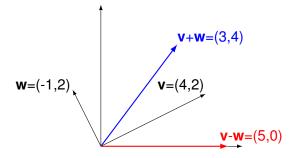
$$\vec{\mathbf{v}}+\vec{\mathbf{w}}=(\mathbf{v}_1+\mathbf{w}_1,\ldots,\mathbf{v}_n+\mathbf{w}_n)$$

similarly for the -.

Scalar multiplication: $c\vec{v} = (cv_1, \dots cv_n)$ where *c* is a "scalar".

Vector visualization

Vectors are visualized by arrows. They correspond to points (the point where the arrow ends.)



vector addition produces the diagonal of a parallelogram.

Background: Vectors

Dot product or inner product

$$\vec{\mathbf{v}}\cdot\vec{\mathbf{w}}=(\mathbf{v}_1\,\mathbf{w}_1+\ldots+\mathbf{v}_n\,\mathbf{w}_n)=\sum_{i=1}^n\,\mathbf{v}_i\,\mathbf{w}_i$$

Example We have three goods to buy and sell, their prices are (p_1, p_2, p_3) (price vector \vec{p}). The quantities we are buy or sell are (q_1, q_2, q_3) (quantity vector \vec{q} , their values are positive when we sell and negative when we buy.) Selling the quantity q_1 at price p_1 brings in q_1p_1 . The total income is the *dot product*:

$$ec{q} \cdot ec{p} = (q_1, q_2, q_3) \cdot (p_1, p_2, p_3) = q_1 p_1 + q_2 p_2 + q_3 p_3$$

Background: Vector

Length and Unit vector

Length
$$||\vec{v}|| = \sqrt{\vec{v} \cdot \vec{v}} = \sqrt{\sum_{i=1}^{n} v_i^2}$$

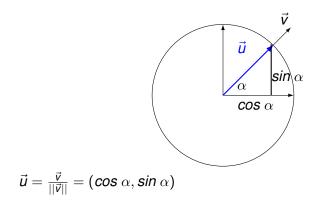
Unit vector is a vector whose length equals one.

$$\vec{u} = rac{\vec{v}}{||\vec{v}||}$$

is a unit vector in the same direction as \vec{v} . (normalized vector)

Background: Vector

Unit vector

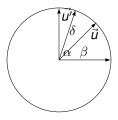


Background: Vector

Cosine formula

Given δ the angle formed by the two unit vectors \vec{u} and $\vec{u'}$, s.t. $\vec{u} = (\cos \beta, \sin \beta)$ and $\vec{u'} = (\cos \alpha, \sin \alpha)$

 $\vec{u} \cdot \vec{u'} = (\cos \beta)(\cos \alpha) + (\sin \beta)(\sin \alpha) = \cos(\beta - \alpha) = \cos \delta$



Given two arbitrary vectors v and w:

$$\cos \delta = \frac{\vec{v}}{||\vec{v}||} \cdot \frac{\vec{w}}{||\vec{w}||}$$

The bigger the angle δ , the smaller is $\cos \delta$; $\cos \delta$ is never bigger than 1 (since we used unit vectors) and never less than -1. It's 0 when the angle is 90°

Background: Matrix

Matrices multiplication

A matrix is represented by [nr-rows x nr-columns]. Eg. for a 2×3 matrix, the notation is:

$${m A} = \left[egin{array}{ccc} {a_{11}} & {a_{12}} & {a_{13}} \ {a_{21}} & {a_{22}} & {a_{23}} \end{array}
ight]$$

 a_{ij} i stands for the row nr, and j stands for the column nr.

The multiplication of two matrices is obtained by

Rows of the 1st matrix x columns of the 2nd.

A matrix with m-columns can be multiplied only by a matrix of m-rows:

 $[n \times m] \times [m \times k] = [n \times k].$

A matrix acts on a vector

Example of 2 x 2 matrix multiplied by a 2 x 1 matrix (viz. a vector). Take A and \vec{x} to be as below.

$$A \vec{x} = \begin{bmatrix} 1 & 0 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} (1,0) \cdot (x_1, x_2) \\ (-1,1) \cdot (x_1, x_2) \end{bmatrix} = \begin{bmatrix} 1(x_1) + 0(x_2) \\ -1(x_1) + 1(x_2) \end{bmatrix} = \begin{bmatrix} x_1 \\ x_2 - x_1 \end{bmatrix} = \vec{b}$$

A is a "difference matrix": the output vector \vec{b} contains differences of the input vector \vec{x} on which "the matrix has acted."