Compositionality in DS

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Next Steps

- Reading Groups:

06.11 Sahlgren and Lenci (2016) (lead by Nicola Sartorato and Francesca Pase) and Baroni, Dinu and Kruszewski (2014) (lead by Nhut Truong and Zhuolun)

11.11 Conneau et al. ACL 2018 lead by Duygu Buga (ALL: BRING YOUR IDEA!)

18.11 Baroni In press lead by Alex Eperon and Valentino Penasa

20.11 (Reddy, S. et al 2011) (TBC) lead by Abdel-akram Anis Saidi and Ludovica Panifto will present her Thesis on DS and events.

21.11 TBD (exercises + info on evaluation metrics? or ask Luca to use this class as a computational lab??)

- Sample Written Exam: 28.11,
- Project Proposal presentation 04.12 and 05.12.
- Final exam: 03.02.2020

Acknowledgments

Credits: Some of the slides of today lecture are based on earlier DS courses taught by Marco Baroni and Aurelie Herbelot.

Distributional Semantics

Recall

The main questions have been:

1. What is the sense of a given *word*?
2. How can it be induced and represented?
3. How do we relate word senses (synonyms, antonyms, hyperonym etc.)?

Well established answers:

1. The sense of a word can be given by its use, viz. by the *contexts* in which it occurs;
2. It can be induced from (either raw or parsed) corpora and can be represented by *vectors*.
3. *Cosine similarity* captures synonyms (as well as other semantic relations).

Compositional Distributional Semantics: motivation

- Formal semantics gives an elaborate and elegant account of the productive and systematic nature of language.
- The formal account of compositionality relies on:
  - *words* (the minimal parts of language, with an assigned meaning)
  - *syntax* (the theory which explains how to make complex expressions out of words)
  - *semantics* (the theory which explains how meanings are combined in the process of particular syntactic compositions).

Compositional Distributional Semantics: motivation

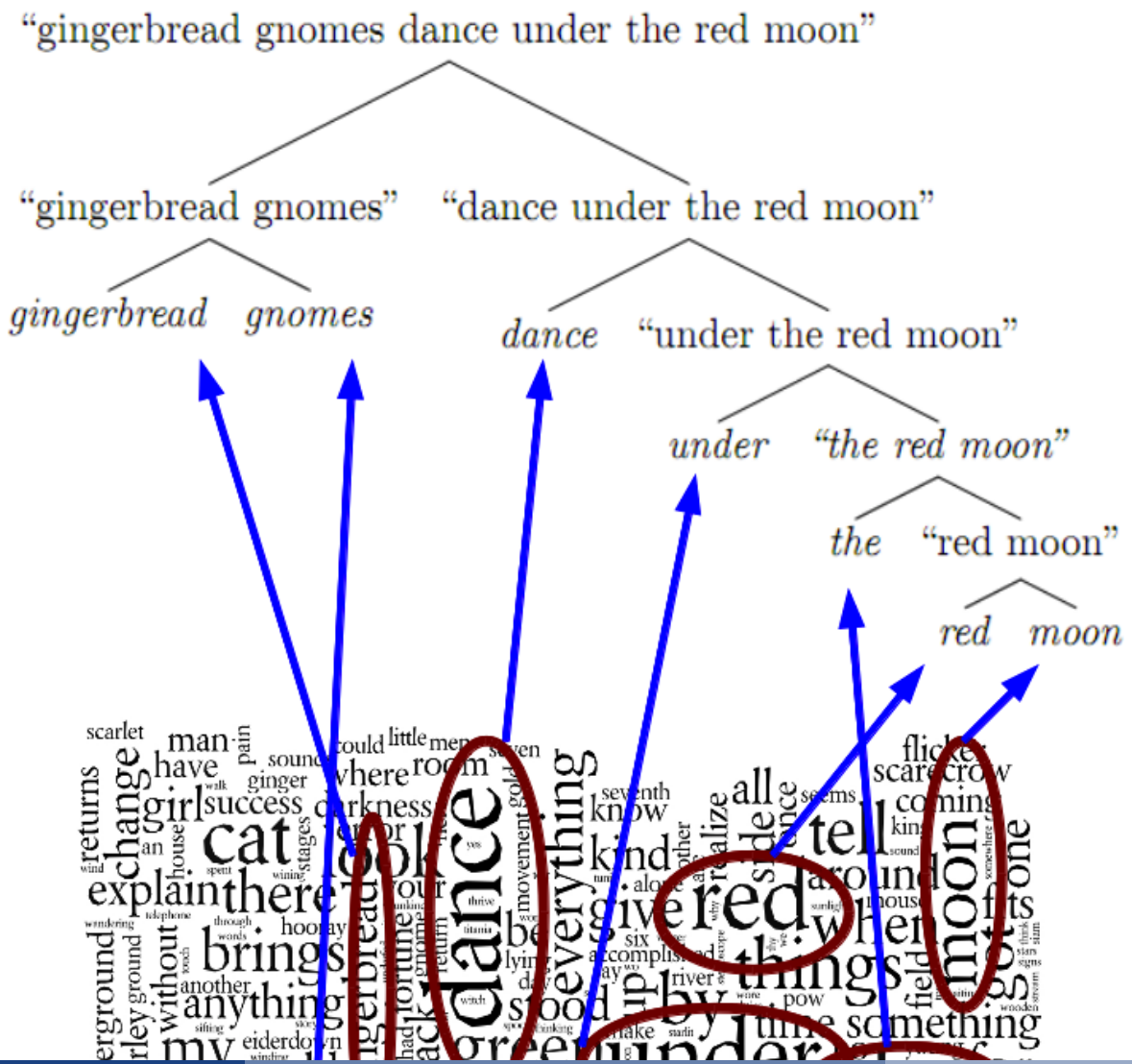
- But formal semantics does not actually say anything about lexical semantics (the meaning of *president*, *president′*, is the set of all presidents in particular world).
- Who is to say that being a president is being important, and that being ‘president of the United States is being super-important?
- Distributions a potential solution. But if we make the approximation that distributions are ‘meaning’, then we need a way to account for *compositionality* in a distributional setting.

Why not just look at the distribution of phrases?

- The distribution of phrases – even sentences – can be obtained from corpora, but...
  - those distributions are very sparse;
  - observing them does not account for productivity in language.
- Some models assume that corpus-extracted phrasal distributions are irrelevant data.
- Some models assume that, given enough data, corpus-extracted phrasal distributions have the status of gold standard.

Compositionality in FS and DS

Syntax and semantics



From Formal to Distributional Semantics

New research questions in DS

1. Do all words live in the same space?
2. What about compositionality of word sense?
3. How do we “infer” some piece of information out of another?

From Formal Semantics to Distributional Semantics

Recent results in DS

1. From one space to multiple spaces, and from only vectors to vectors and matrices.
2. Several Compositional DS models have been tested so far.
3. New “similarity measures” have been defined to capture lexical entailment and tested on phrasal entailment too.

Multiple semantics spaces

Phrases

All the expressions of the same syntactic category live in the same semantic space.
For instance, ADJ N ("special collection") live in the same space of N ("archives").

important route	*nice girl*	*little war*
important transport	good girl	great war
important road	big girl	major war
major road	guy	small war
red cover	*special collection*	*young husband*
black cover	general collection	small son
hardback	small collection	small daughter
red label	archives	mistress

Multiple semantics spaces

Problem of one semantic space model

	and	of	the	valley	moon
planet	$> 1K$	$> 1K$	$> 1K$	20.3	24.3
night	$> 1K$	$> 1K$	$> 1K$	10.3	15.2
space	$> 1K$	$> 1K$	$> 1K$	11.1	20.1

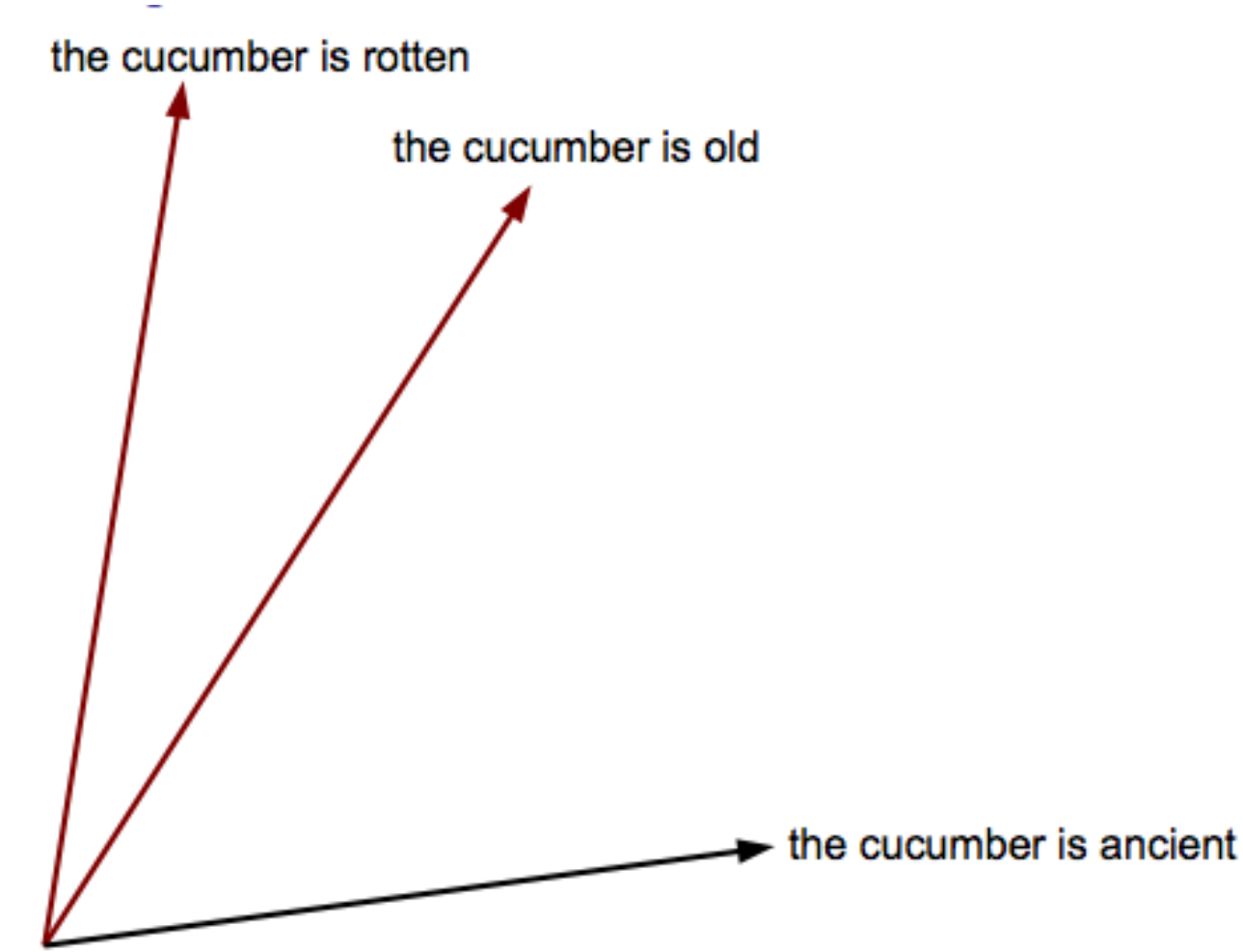
"and", "of", "the" have similar distribution but a very different meaning:

"the valley of the moon" vs. "the valley and the moon"

the semantic space of these words must be different from those of eg. nouns ("valley', "moon").

Compositionality in DS: Expectation

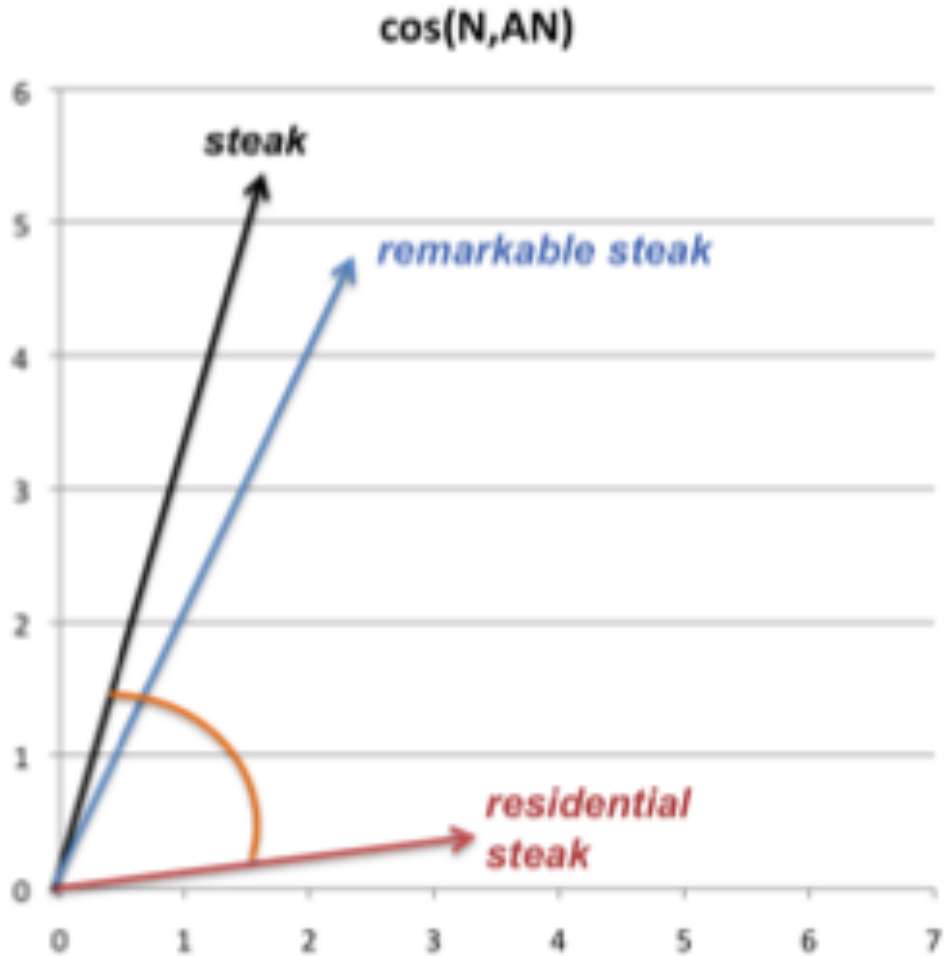
Disambiguation



Mitchell and Lapata 2008, Erk and Padó 2008

Compositionality in DS: Expectation

Semantic deviance



Compositionality: DP IV

Kintsch (2001)

Kintsch (2001): The meaning of a predicate varies depending on the argument it operates upon:

The horse run vs. the color run

Hence, take "gallop" and "dissolve" as landmarks of the semantic space,

- "the horse run" should be closer to "gallop" than to "dissolve".
- "the color run" should be closer to "dissolve" than to "gallop"

(or put it differently, the verb acts differently on different nouns.)

Compositionality: ADJ N

Pustejovsky (1995)

- red Ferrari [the outside]
- red watermelon [the inside]
- red traffic light [only the signal]
- ..

Similarly, “red” will reinforce the concrete dimensions of a concrete noun and the abstract ones of an abstract noun.

Some distributional compositionality models

- Pointwise models: word-based model, task-evaluated.
- Lexical function model: word-based, evaluated against phrasal distributions.
- Pregroup grammar model: CCG-based model, task-evaluated. [not covered here*]
- Neural Network [not covered here. ML for NLP]

Pregroup: `http://coling2016.anlp.jp/doc/tutorial/slides/T1/KartsaklisSadrzadeh.pdf`

Background: Vector and Matrix

Operations on vectors

Vector addition:

$$\vec{v} + \vec{w} = (v_1 + w_1, \ldots v_n + w_n)$$

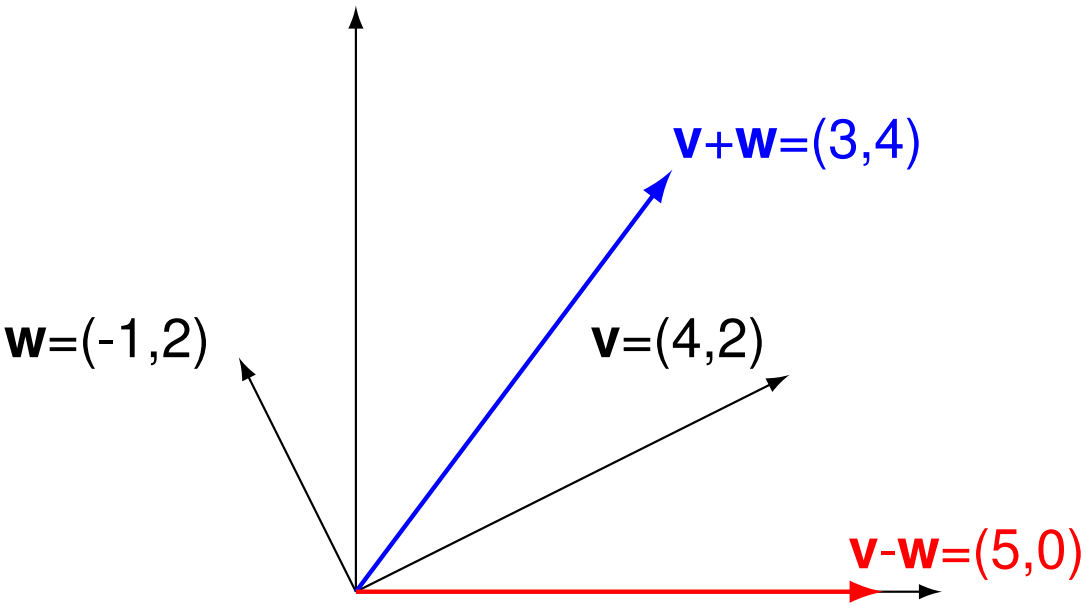
similarly for the $-$.

Scalar multiplication: $c\vec{v} = (cv_1, \ldots cv_n)$ where c is a "scalar".

Background: Vector and Matrix

Vector visualization

Vectors are visualized by arrows. They correspond to points (the point where the arrow ends.)



vector addition produces the diagonal of a parallelogram.

Compositionality in DS

Different Models

	horse	run	horse + run	horse $\odot$ run	run(horse)
gallop	15.3	24.3	39.6	371.8	24.6
jump	3.7	15.2	18. 9	56.2	19.3
dissolve	2.2	20.1	22.3	44.2	12.4

- Additive and/or Multiplicative Models: Mitchell & Lapata (2008), Guevara (2010)
- Function application: Baroni & Zamparelli (2010), Grefenstette & Sadrzadeh (2011)
- For others, see Mitchell and Lapata (2010) overview, and Frege in Space related work section.

Compositionality as vectors composition

Mitchell and Lapata (2008,2010): Class of Models

General class of models:

$$\vec{p} = f(\vec{u}, \vec{v}, R, K)$$

- $\vec{p}$ can be in a different space than $\vec{u}$ and $\vec{v}$.
- K is background knowledge
- R syntactic relation.

Putting constraints will provide us with different models.

Mitchell and Lapata (2010)

- Word-based (5 words on either side of the lexical item under consideration).
- The composition of two vectors $\vec{u}$ and $\vec{v}$ is some function $f(\vec{u}, \vec{v})$. M & L try:
  - addition $p_i = \vec{u}_i + \vec{v}_i$
  - multiplication $p_i = \vec{u}_i . \vec{v}_i$
  - tensor product $p_{ij} = \vec{u}_i . \vec{v}_j$
  - circular convolution $p_{ij} = \sigma_j \vec{u}_j . \vec{v_{i-j}}$
  - ... etc
- Task-based evaluation: similarity ratings (noun noun, adj noun, verb object phrases.). Sperman correlation human and models.

Compositionality as vectors composition

SKIP: Mitchell and Lapata (2008,2010): Constraints on the models

1. Not only the *i*th components of $\vec{u}$ and $\vec{v}$ contribute to the *i*th component of $\vec{p}$. Circular convolution:

$$p_i = \Sigma_j u_j \cdot v_{i-j}$$

2. Role of K, e.g. consider the argument's distributional neighbours Kitsch 2001:

$$\vec{p} = \vec{u} + \vec{v} + \Sigma\vec{n}$$

3. Asymmetry weights pred and arg differently:

$$p_i = \alpha u_i + \beta v_i$$

4. the *i*th component of $\vec{u}$ should be scaled according to its relevance to $\vec{v}$ and vice versa. multiplicative model

Discussion: the meaning of f

- How do we interpret $f(\vec{u}, \vec{v})$ linguistically?
- Intersection in formal semantics has a clear interpretation:
  $\exists x[cat'(x) \wedge black'(x)]$
  There is a cat in the set of all cats which is also in the set of black things.
- But what with addition, multiplication?

Multiplication

- Multiplication is intersective.
- But it is commutative in a word-based model:

$$\overrightarrow{\text{The cat chases the mouse}} = \overrightarrow{\text{The mouse chases the cat}}$$

- Note that in a syntax-based model, things could work out:

$$\overrightarrow{\text{cat}_{subj}\ \text{chase}_{head}\ \text{mouse}_{obj}} \neq \overrightarrow{\text{mouse}_{subj}\ \text{chase}_{head}\ \text{cat}_{obj}}$$

Multiplying to zero

- Multiplication has issues retaining information when composing several words. Most dimensions become 0 or close to 0:

$$\begin{pmatrix}0.45\\0.23\\0.00\\0.14\\0.76\end{pmatrix} \text{x} \begin{pmatrix}0.11\\0.43\\0.54\\0.00\\0.39\end{pmatrix} = \begin{pmatrix}0.05\\0.10\\0.00\\0.00\\0.30\end{pmatrix} \quad \begin{pmatrix}0.05\\0.10\\0.00\\0.00\\0.30\end{pmatrix} \text{x} \begin{pmatrix}0.00\\0.89\\0.57\\0.23\\0.42\end{pmatrix} = \begin{pmatrix}0.00\\0.09\\0.00\\0.00\\0.13\end{pmatrix}$$

Addition

- Addition is not intersective: the whole meaning of both $\vec{u}$ and $\vec{v}$ are included in the resulting phrase.
- Commutativity is a problem, as with multiplication.
- No sense disambiguation and no indication as to how an adjective, for instance, modifies a particular noun (i.e. the distributions of *red car* and *red cheek* both include high weights on the *blush* dimension).
- Too much information.
- Still, in practice, simple addition has shown good performance on a variety of tasks...

Scottish castles in a DS space

- 20 nearest neighbours of “Scottish castle” (additive model): ’castle’, ’scottish’, ’scotland’, ’castles’, ’dunkeld’, ’huntly’, ’perthshire’, ’linlithgow’, ’gatehouse’, ’crieff’, ’inverness’, ’covenanters’, ’haddington’, ’moray’, ’jacobites’, ’atholl’, ’holyrood’, ’jedburgh’, ’braemar’, ’lanark’

Compositionality: DP IV

Mitchell and Lapata (2008,2010): Evaluation data set

- 120 experimental items consisting of 15 reference verbs each coupled with 4 nouns and 2 (high- and low-similarity) landmarks
- Similarity of sentence with reference vs. landmark rated by 49 subjects on 1-7 scale

	Noun	Reference	High	Low
The	fire	glowed	burned	beamed
The	face	glowed	beamed	burned
The	child	strayed	roamed	digressed
The	discussion	strayed	digressed	roamed
The	sales	slumped	declined	slouched
The	shoulders	slumped	slouched	declined

Table 1: Example Stimuli with High and Low similarity landmarks

Compositionality: DP IV

Mitchell and Lapata (2008,2010): Evaluation results

Models vs. Human judgment: different ranging scale.
Additive model, Non compositional baseline, weighted additive and Kintsch (2001) don't distinguish between High (close) and Low (far) landmarks.
Multiplicative and combined models are closed to human ratings. The former does not require parameter optimization.

Model	High	Low	ρ
NonComp	0.27	0.26	0.08
Add	0.59	0.59	0.04
Weight Add	0.35	0.34	0.09
Kintsch	0.47	0.45	0.09
Multiply	0.42	0.28	0.17
Combined	0.38	0.28	0.19
Human Judg	4.94	3.25	0.40

Compositionality as vector combination: problems

Grammatical words: highly frequent

	planet	night	space	color	blood	brown
the	>1K	>1K	>1K	>1K	>1K	>1K
moon	24.3	15.2	20.1	3.0	1.2	0.5
the moon	??	??	??	??	??	??

Composition as vector combination: problems

Grammatical words variation

	car	train	theater	person	movie	ticket
few	>1K	>1K	>1K	>1K	>1K	>1K
a few	>1K	>1K	>1K	>1K	>1K	>1K
seats	24.3	15.2	20.1	3.0	1.2	0.5
few seats	??	??	??	??	??	??
a few seats	??	??	??	??	??	??

- There are few seats available. negative: hurry up!
- There are a few seats available. positive: take your time!

Compositionality in Formal Semantics

Verbs

Recall:

- an intransitive verb is a set entities, hence it's a one argument function. $e \rightarrow t$
- transitive verb: set of pairs of entities, hence it's a two argument function: $e \rightarrow (e \rightarrow t)$

The function "walk" selects a subset of D_e.

Compositionality in Formal Semantics

Adjectives

Syntax:

ADJ is a function that modifies a noun:

$$[\![\text{Red}]\!] \cap [\![\text{Moon}]\!]$$

Background: Matrix

Matrices multiplication

A matrix is represented by [nr-rows x nr-columns].
Eg. for a 2 x 3 matrix, the notation is:

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \end{bmatrix}$$

a_{ij} i stands for the row nr, and j stands for the column nr.

The multiplication of two matrices is obtained by

Rows of the 1st matrix x columns of the 2nd.

A matrix with m-columns can be multiplied only by a matrix of m-rows:

[n x m] x [m x k] = [n x k].

Background: Vector and Matrix

A matrix acts on a vector

Example of 2 x 2 matrix multiplied by a 2 x 1 matrix (viz. a vector). Take A and $\vec{x}$ to be as below.

$$A\,\vec{x} = \begin{bmatrix} 1 & 0 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} (1,0)\cdot(x_1,x_2) \\ (-1,1)\cdot(x_1,x_2) \end{bmatrix} = \begin{bmatrix} 1(x_1)+0(x_2) \\ -1(x_1)+1(x_2) \end{bmatrix} =$$

$$= \begin{bmatrix} x_1 \\ x_2 - x_1 \end{bmatrix} = \vec{b}$$

A is a "difference matrix": the output vector $\vec{b}$ contains differences of the input vector $\vec{x}$ on which "the matrix has acted."

Background: Vector and Matrix

A matrix acts on a vector: Exercise

Given the matrix A and the vector v below, compute the multiplication Av

$$A = \begin{bmatrix} 3 & 5 & 6 \\ 4 & 7 & 10 \end{bmatrix}$$

$v = (2, 4, 5)$

Baroni and Zamparelli (2010)

- Functional model for adjective-noun composition.
- Composition is the multiplication of vectors/matrices **learned** from access to phrasal distributions.
- 'Internal' evaluation: composition is evaluated against phrasal distributions.

Assumptions

- Given enough data, distributions for phrases should be obtained in the same way as for single words.
- I.e. it is fair to assume that if we have seen enough instances of *black cat*, the context of the phrase should give us an indication of its meaning (perhaps it is more related to witches than *cat* and *ginger cat*).
- Let's say we have a vector $\vec{a}$ (*black*) and a $\vec{n}$ (*cat*), and also a $\vec{an}$ (*black cat*), we can hypothesise a composition method which combines $\vec{a}$ and $\vec{n}$ to get $\vec{an}$ (standard machine learning).

Assumptions

- There is no single composition operation for adjectives. Each adjective acts on nouns in a different way:
  - *red car*: the outside of the car is evenly painted with the colour red (visual);
  - *fast car*: the engine of the car is powerful (functional);
  - *expensive car*: the price of the car is high (abstract/relational).
- Even single adjectives will combine with various nouns in different ways:
  - *red car*: outside of the car, even paint;
  - *red watermelon*: inside of the watermelon, probably not as red as the car;
  - *red nose*: a little redder than usual, probably due to a cold.

Baroni and Zamparelli's 2010 proposal

Implementing the idea of function application in a vector space

- Functions as **linear maps** between vector spaces
- Functions are matrices, function application is function-by-vector multiplication

Compositionality in DS: Function application

Baroni and Zamparelli (2010)

Distributional Semantics (e.g. 2 dimensional space):

N/N: matrix

red	d1	d2
d1	$n1$	$n2$
d2	$m1$	$m2$

N: vector

	moon
d1	$k1$
d2	$k2$

Function app. by the matrix product and returns a vector:
$red(\overrightarrow{moon}) = \sum_{i=1}^{n} red_i \; moon_i$

N: vector

	red moon
d1	$(n1, n1) \cdot (k1, k2)$
d2	$(m1, m2) \cdot (k1, k2)$

=

N: vector

	red moon
d1	$(n1k1) + (n2k2)$
d2	$(m1k1) + (m2k2)$

Compositionality in DS: Function application

Learning methods

- Vectors are induced from the corpus by a lexical association co-frequency function. [Well established]
- Matrices are learned by regression (Baroni & Zamparelli (2010)). E.g.: “red” is learned, using linear regression, from the pairs (N, red-N).

n and the moon shining i
with the moon shining s
rainbowed moon . And the
crescent moon , thrille
in a blue moon only , wi
now , the moon has risen
d now the moon rises , f
y at full moon , get up
crescent moon . Mr Angu

...

f a large red moon , Campana
, a blood red moon hung over
glorious red moon turning t
The round red moon , she ’s
l a blood red moon emerged f
n rains , red moon blows , w
monstrous red moon had climb
. A very red moon rising is
under the red moon a vampire

...

Compositionality in DS: Function application

Learning matrices

red (R) is a matrix whose values are unknown (I use capitol letters for unknown):

$$\begin{bmatrix} R_{11} & R_{12} \\ R_{21} & R_{22} \end{bmatrix}$$

We have harvested the vectors $\vec{moon}$ and $\vec{army}$ representing "moon" and "army", resp. and the vectors $\vec{n_1} = (n_{11}, n_{12})$ and $\vec{n_2} = (n_{21}, n_{22})$ representing "red moon", "red army". Since we know that e.g.

$$R\ \vec{moon} = \begin{bmatrix} R_{11}moon_1 + R_{12}moon_2 \\ R_{21}moon_1 + R_{22}moon_2 \end{bmatrix} = \begin{bmatrix} n_{11} \\ n_{12} \end{bmatrix} = \vec{n_1}$$

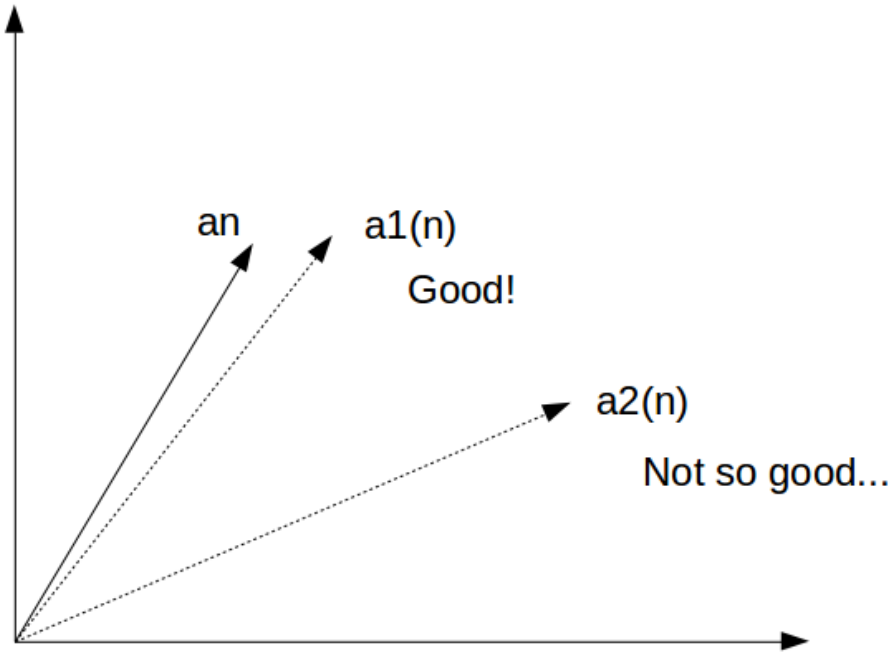
taking all the data together, we end up having to solve the following multiple regression problems to determine the R values (r_{11}, r_{12} etc.)

$$\begin{aligned} R_{11}moon_1 + R_{12}moon_2 &= n'_{11} \\ R_{11}army_1 + R_{12}army_2 &= n'_{21} \\ \\ R_{21}moon_1 + R_{22}moon_2 &= n'_{12} \\ R_{21}army_1 + R_{22}army_2 &= n'_{22} \end{aligned}$$

which are solved by assigning weights to the unknown

System

- Test by measuring distance between a given adjective-noun combination and the corresponding phrasal distribution on unseen data.



Compositionality in DS: ADJ N

Comparison Compositional DS models

Summing up, Baroni & Zamparelli 2010 have

- trained separate models for each adjective;
- (a) composed the learned matrix (function) with a noun vector (argument) by matrix product ($\cdot$) – the adjective weight matrix with the noun vector value;
- composed adjectives with nouns using: (b) additive and (c) multiplicative model –starting from adjective and noun vectors;
- harvested vectors for "adjective-noun" from the corpus;
- compared (a) "learned_matrix $\cdot$ vector_noun" ("function application") vs. (b) "vector_adj + vector_noun" vs. (c) "vector_adj $\odot$ vector_noun";
- shown that – among (a), (b), (c) – (a) gives results more similar to the "harvested vector_adj-noun" than the other two methods.

Compositionality in DS: ADJ N

Observed ADJ N vs. Composed ADJ(N): (a) when observed and composed are close

Comparison observed vector (induced from corpus) with the result of the matrix product by comparing their neighbour:

adj N	*observed neighbor*	*predicted neighbor*
common understanding	common approach	common vision
different authority	different objective	different description
different partner	different organisation	different department
general question	general issue	general issue
historical introduction	historical background	historical background
necessary qualification	necessary experience	necessary experience
new actor	new cast	new case
recent request	recent enquiry	recent enquiry
small drop	droplet	drop
young engineer	young designer	young engineering

Compositionality in DS: ADJ N

Observed ADJ N vs. Composed ADJ(N): (b) when observed and composed are far

adj N	*observed neighbor*	*predicted neighbor*
American affair	American development	American policy
current dimension	left (a)	current element
good complaint	current complaint	good beginning
great field	excellent field	great distribution
historical thing	different today	historical reality
important summer	summer	big holiday
large pass	historical region	large dimension
special something	little animal	special thing
white profile	chrome (n)	white show
young photo	important song	young image

From Formal to Distributional Semantics

FS domains and DS spaces

- FS:
  - Atomic vs. functional types
  - Typed denotational domains
  - Correspondence between syntactic categories and semantic types
- Could we import these ideas in DS?
  - Vectors vs. matrices
  - Typed semantic spaces
  - Correspondence between syntactic categories and semantic types

Truth and DS

- A fundamental difference between formal and distributional semantics:
  - Formal semantics encodes truth in a model (and just doesn't know where the model comes from...)
  - Distributional semantics encodes usage (including lies).

Truth and DS

- At best, we can hope to measure consistency/contradictions.
- If *Obama* is found in many contexts related to being born in Africa *and* to being born in America, both
  $\overrightarrow{\text{Obama born in Kenya}}$ and $\overrightarrow{\text{Obama born in Hawaii}}$
  will end up with mediocre weights.

Entailment

Entailment in FS

FS starting point is logical entailment between propositions, hence it's based on the referential meaning of sentences ($D_t = \{0, 1\}$).

All domains are partially ordered, e.g.:

- $D_t = \{0, 1\}$ and $0 \leq_t 1$,
- $D_{e \to t} : \{\mathit{student}, \mathit{person}\}$,
  s.t. $[\![\mathit{student}]\!] = \{a, b\}$ and $[\![\mathit{person}]\!] = \{a, b, c\}$,
  by def: $[\![\mathit{student}]\!] \leq_{e \to t} [\![\mathit{person}]\!]$ since
  $\forall \alpha \in D_e \; [\![\mathit{student}]\!]([\![\alpha]\!]) \leq_t [\![\mathit{person}]\!]([\![\alpha]\!])$,

Entailment

Entailment in DS

- Lexical entailment: already some successful results.
- Phrase entailment: a few studies done.
- Sentential entailment: vd. SICK and SNLI

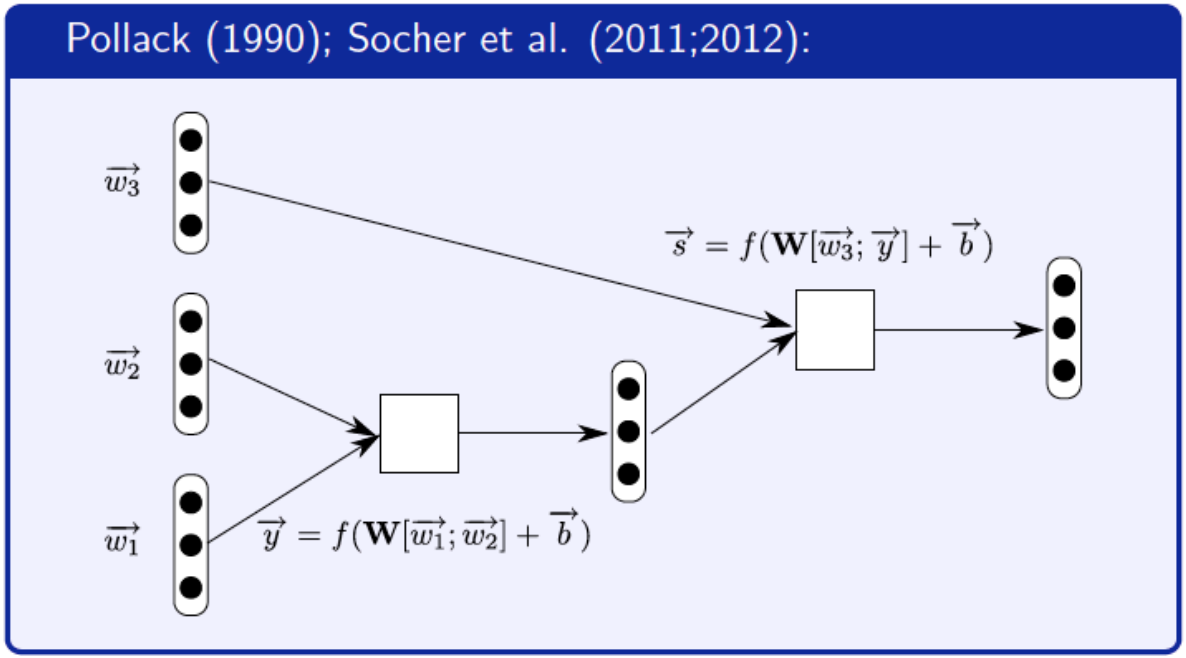
A few references

- M. Baroni and R. Zamparelli (2010). Nouns are vectors, adjectives are matrices: Representing adjective-noun constructions in semantic space. Proceedings of EMNLP
- E. Guevara (2010). A regression model of adjective-noun compositionality in in distributional semantics. Proceedings of GEMS.
- Kintsch Predication. (2001) Cognitive Science, 25(2): 173–202.
- J. Mitchell and M. Lapata (2008). Vector-based models of semantic composition. Proceedings of ACL.
- J. Mitchell and M. Lapata (2010). Composition in distributional models of semantics. Cognitive Science 34(8): 1388–1429

COMPOSES `http://clic.cimec.unitn.it/composes/`

Neural Network and CDSM

(Socher et al., 2012, Kalchbrenner et al., 2014, Cheng and Kartsaklis, 2015)



NN models, in particular RNN, in which the compositional operator is part of a neural network and is usually optimized against a specific objective. You will learn them in ML for NLP.

Back to our Goals

1. provide students with an overview of the field with focus on the syntax-semantics interface;
2. bring students to be aware on the one hand of **several lexicalized formal grammars**, on the other hand of **computational semantics models** and be able to combine some of them to capture the natural language syntax-semantics interface;
3. evaluate several applications [Started] with a special focus to DSM and Language and Vision Models;
4. make students acquainted with writing scientific reports. [Started]